

# **Ensemble Forecasting**

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# Outline

## ➤ Introduction

- Why do forecast go wrong?
- Observations, model, “chaos”

## ➤ The ECMWF ensemble

- How does the ENS represent uncertainties?
- Configuration of the ENS

## ➤ ENS products

- Very short overview – much more in rest of course

## ➤ Use of ENS

- Probabilities and decision support

# Why are forecasts sometimes wrong?

## ➤ Initial condition uncertainties

- Lack of observations
- Observation error
- Errors in the data assimilation

## ➤ Model uncertainties

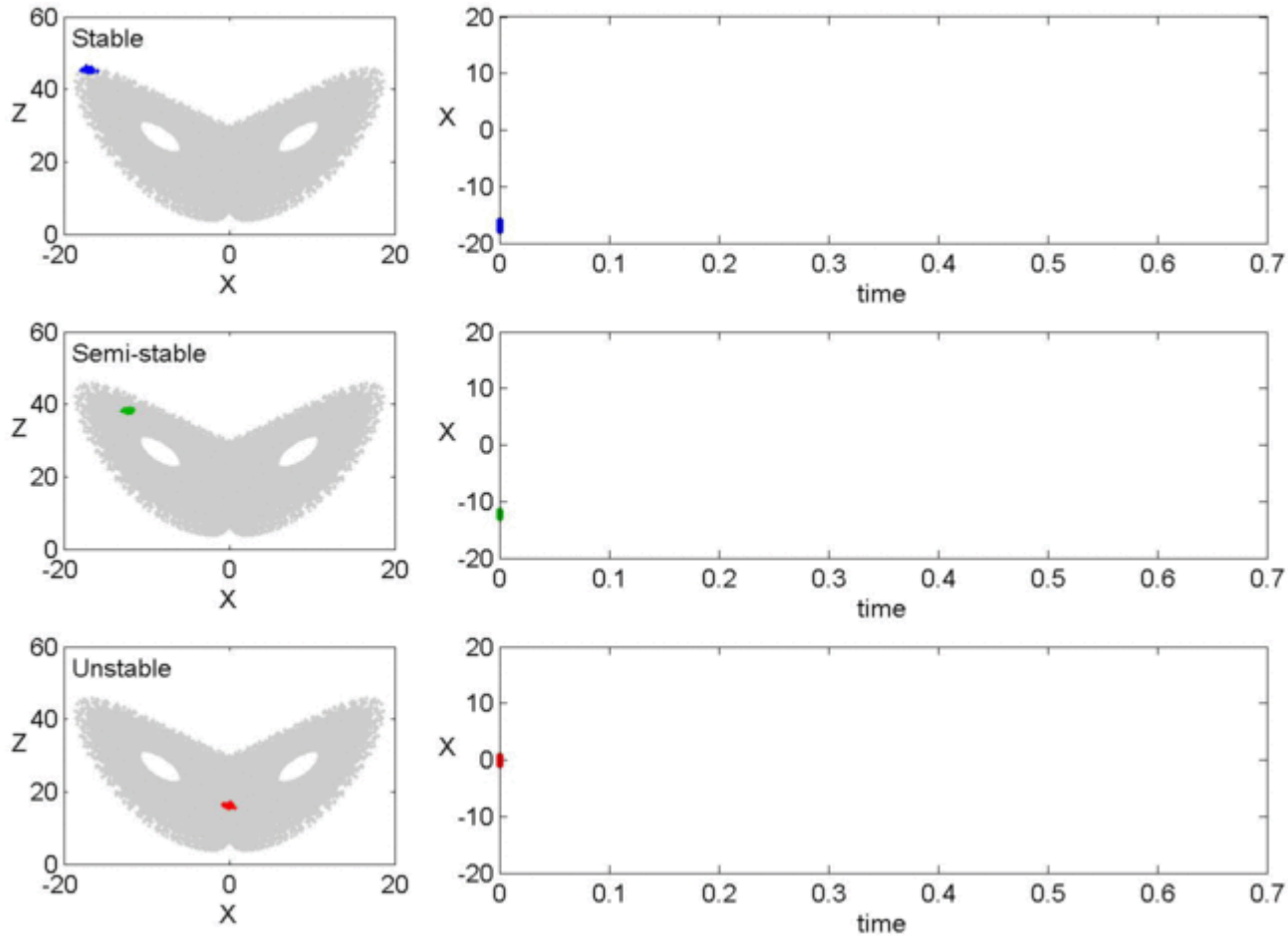
- Limited resolution
- Parameterisation of physical processes

## ➤ The atmosphere is chaotic

- small uncertainties grow to large errors (unstable flow)
- small scale errors will affect the large scale (non-linear dynamics)
- error-growth is flow dependant

## ➤ Even very good analyses and forecast models are prone to errors

# Chaos - the Lorenz attractor



Tim Palmer, Oxford University

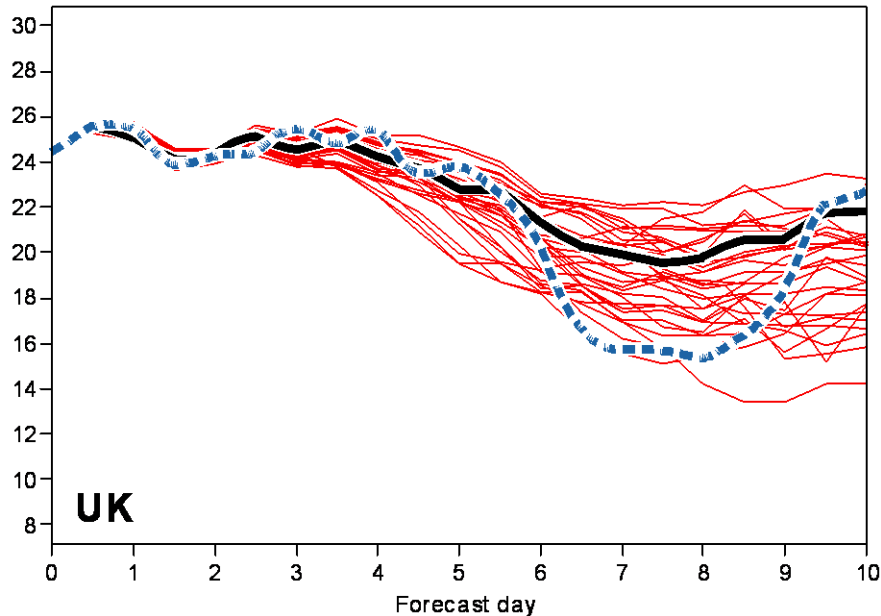
# Flow dependence of forecast errors

26<sup>th</sup> June 1995

ECMWF ensemble forecast - Air temperature

Date: 26/06/1995 London Lat: 51.5 Long: 0

— Control    - - - Analysis    - - - Ensemble

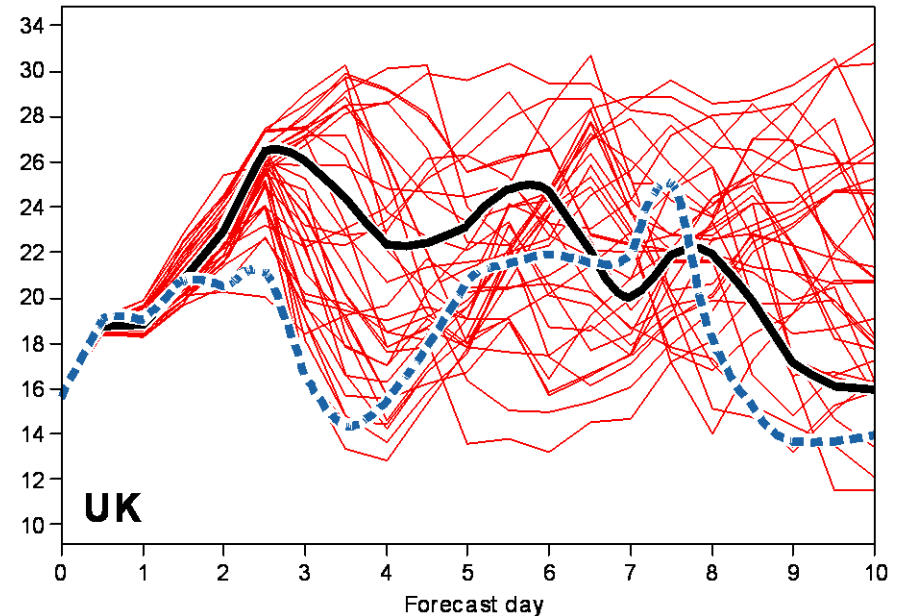


26<sup>th</sup> June 1994

ECMWF ensemble forecast - Air temperature

Date: 26/06/1994 London Lat: 51.5 Long: 0

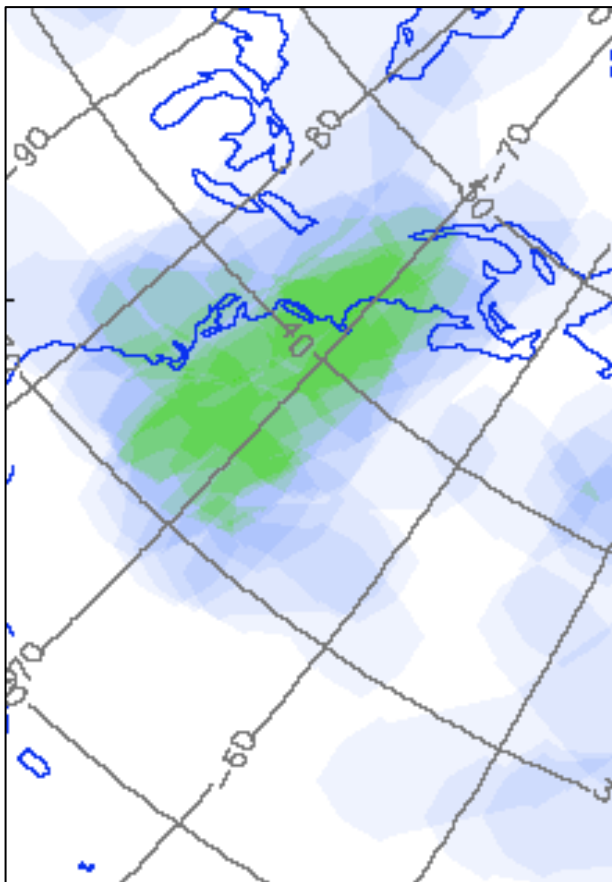
— Control    - - - Analysis    - - - Ensemble



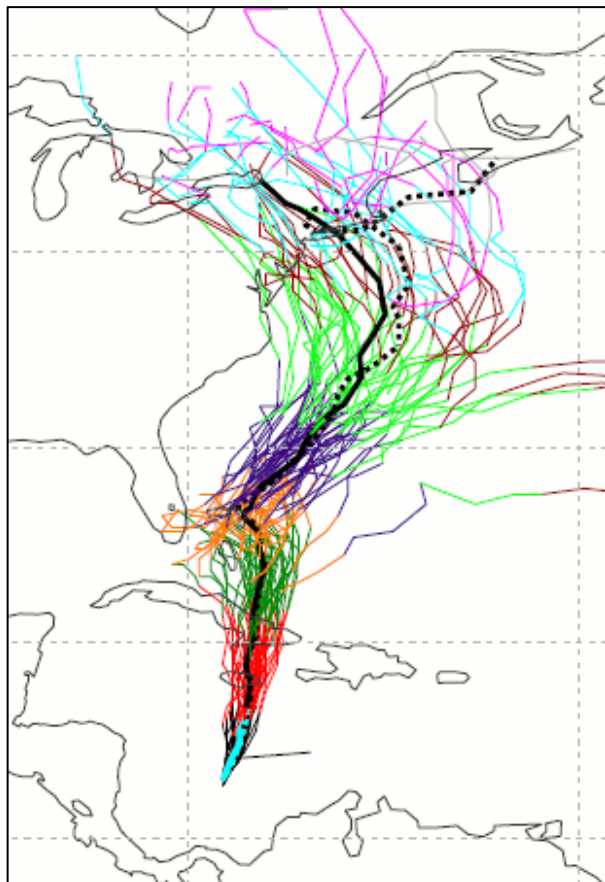
If the forecasts are coherent (small spread) the atmosphere is in a more predictable state than if the forecasts diverge (large spread)

# Superstorm Sandy

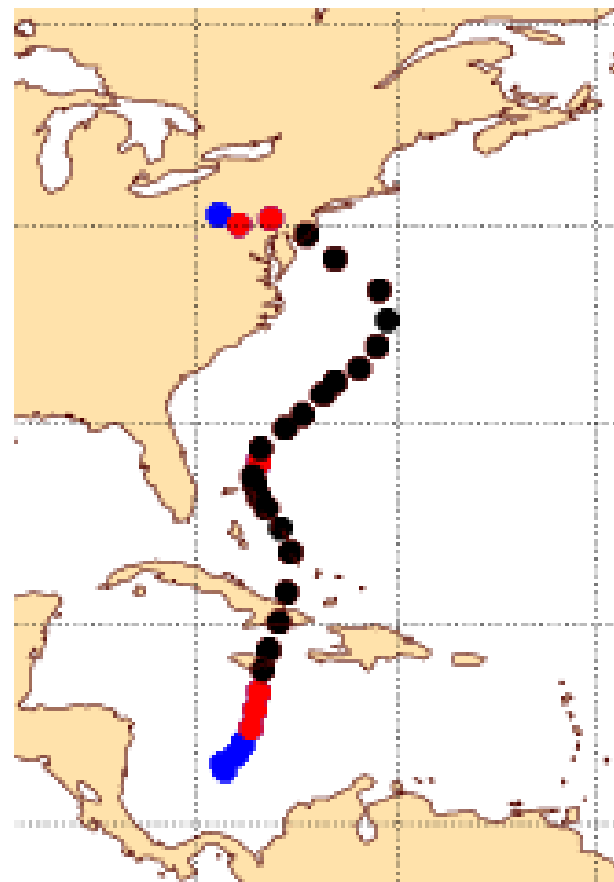
**First indications  
9.5 days before  
landfall**



**Track forecasts  
6.5 days before  
landfall**



**Observed track  
of Sandy**



**2 days before Sandy formed (9.5 days before landfall in New Jersey) there was already a significant probability (25%) of a severe wind storm affecting NE USA**

# Sandy: ENS PV evolution

Forecast from 0 UTC on 25 October

three ensemble members:

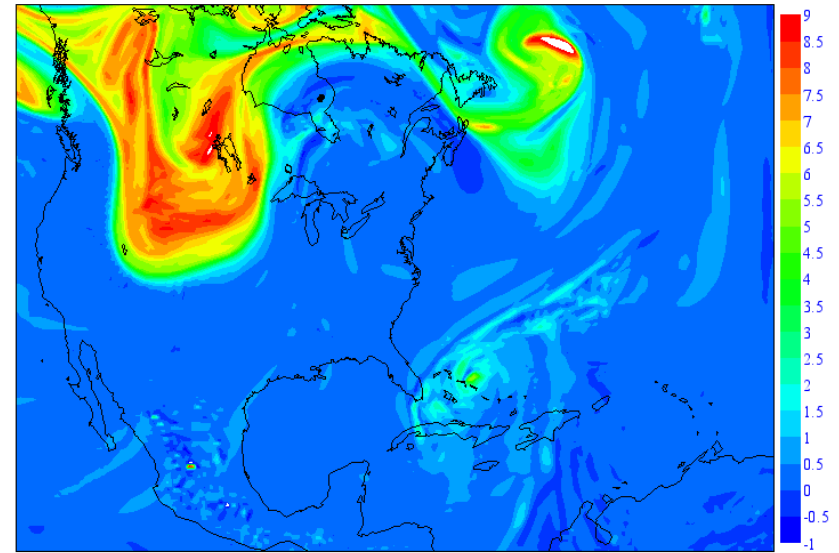
control (top)

M09 (bottom L) “caught” too late

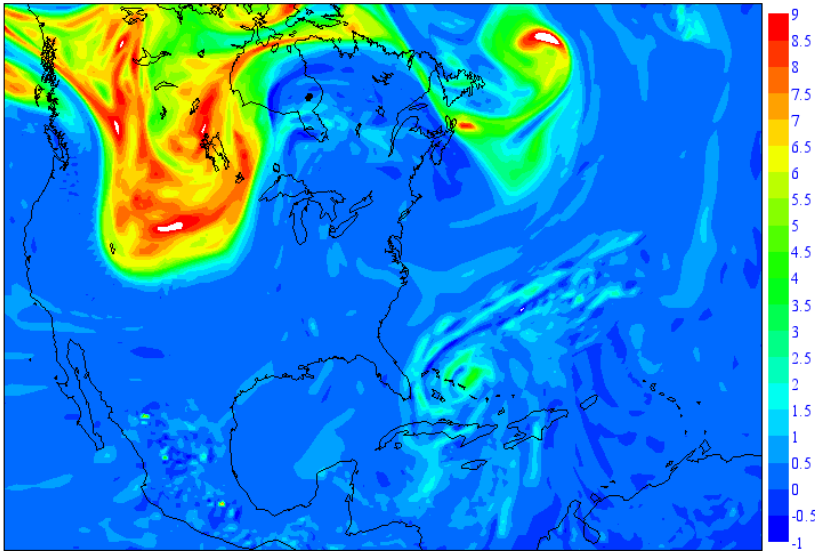
M19 (bottom R) “escaped”

PV on 320K (6h steps)

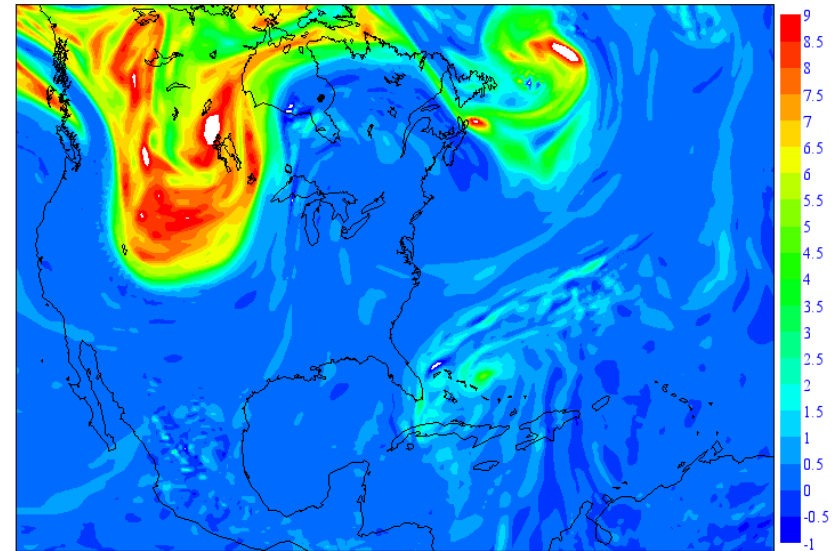
Thursday 25 October 2012 00UTC ECMWF EPS Control Forecast t+24 VT: Friday 26 October 2012 00UTC  
320K Potential vorticity



Thursday 25 October 2012 00UTC ECMWF EPS Perturbed Forecast t+24 VT: Friday 26 October 2012 00UTC  
320K Potential vorticity - Ensemble member number 9 of 51



Thursday 25 October 2012 00UTC ECMWF EPS Perturbed Forecast t+24 VT: Friday 26 October 2012 00UTC  
320K Potential vorticity - Ensemble member number 19 of 51



# What is an ensemble?

- **A set of forecasts run from slightly different initial conditions to account for initial uncertainties**
  - **At ECMWF perturbations are generated using singular vectors and an ensemble of data assimilations**
- **The forecast model also contains approximations that can affect the forecast evolution**
  - **Model uncertainties are represented using “stochastic physics”**
- **The ensemble of forecasts provides a range of future scenarios consistent with our knowledge of the initial state and model capability**
  - **Provides explicit indication of uncertainty in today’s forecast**



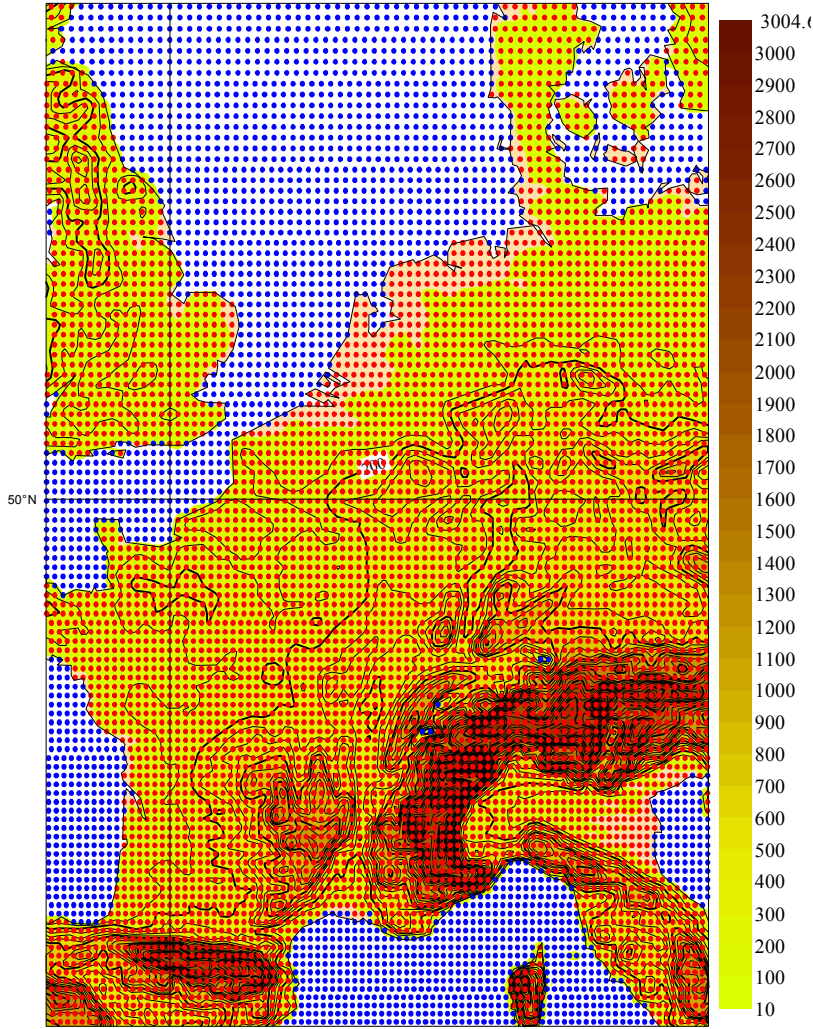
# ECMWF medium-range forecasts

- **High-resolution forecast (16 km grid, 137 levels) runs twice every day to 10 days**
- **Ensemble: same model but run at lower resolution (32 km, 91 levels; 64 km after day 10)**
  - **ensemble control (run from high-resolution analysis, no perturbation)**
  - **50 perturbed members (account for initial and model uncertainties)**
  - **Ensemble coupled to ocean model from start of forecast**

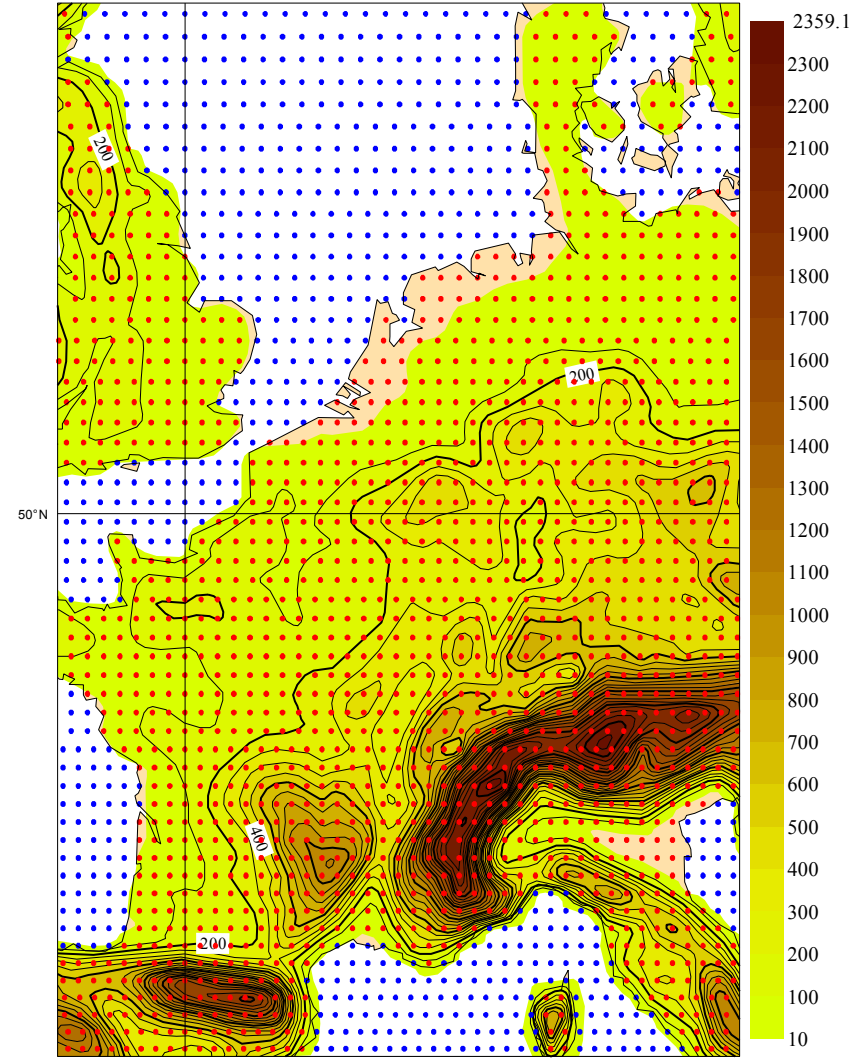
# Model grids: HRES (16km, T1279)

# ENS (32 km, T639)

OROGRAPHY, GRID POINTS AND LAND SEA MASK IN TL 1279 (OP 2010) ECMWF MODEL  
orography shaded (height in m), land grid points (red), sea grid points (blue)

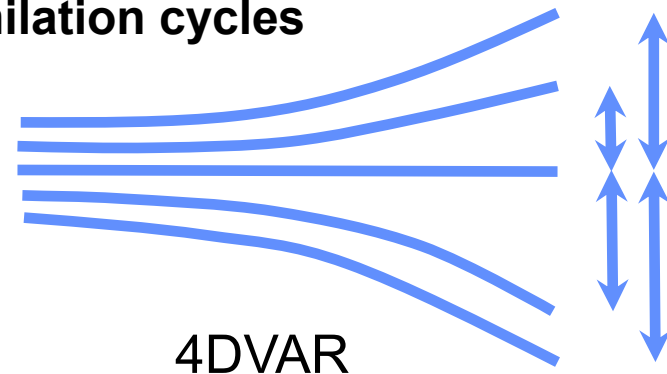


OROGRAPHY, GRID POINTS AND LAND SEA MASK IN TL 639 (EPS 2010) ECMWF MODEL  
orography shaded (height in m), land grid points (red), sea grid points (blue)



# Initial uncertainties

- **Combination of 2 types of perturbations**
- **Ensemble of data assimilations (EDA)**
  - **Randomly perturbed observations and SST fields**
  - **Run 25 independent data assimilation cycles**



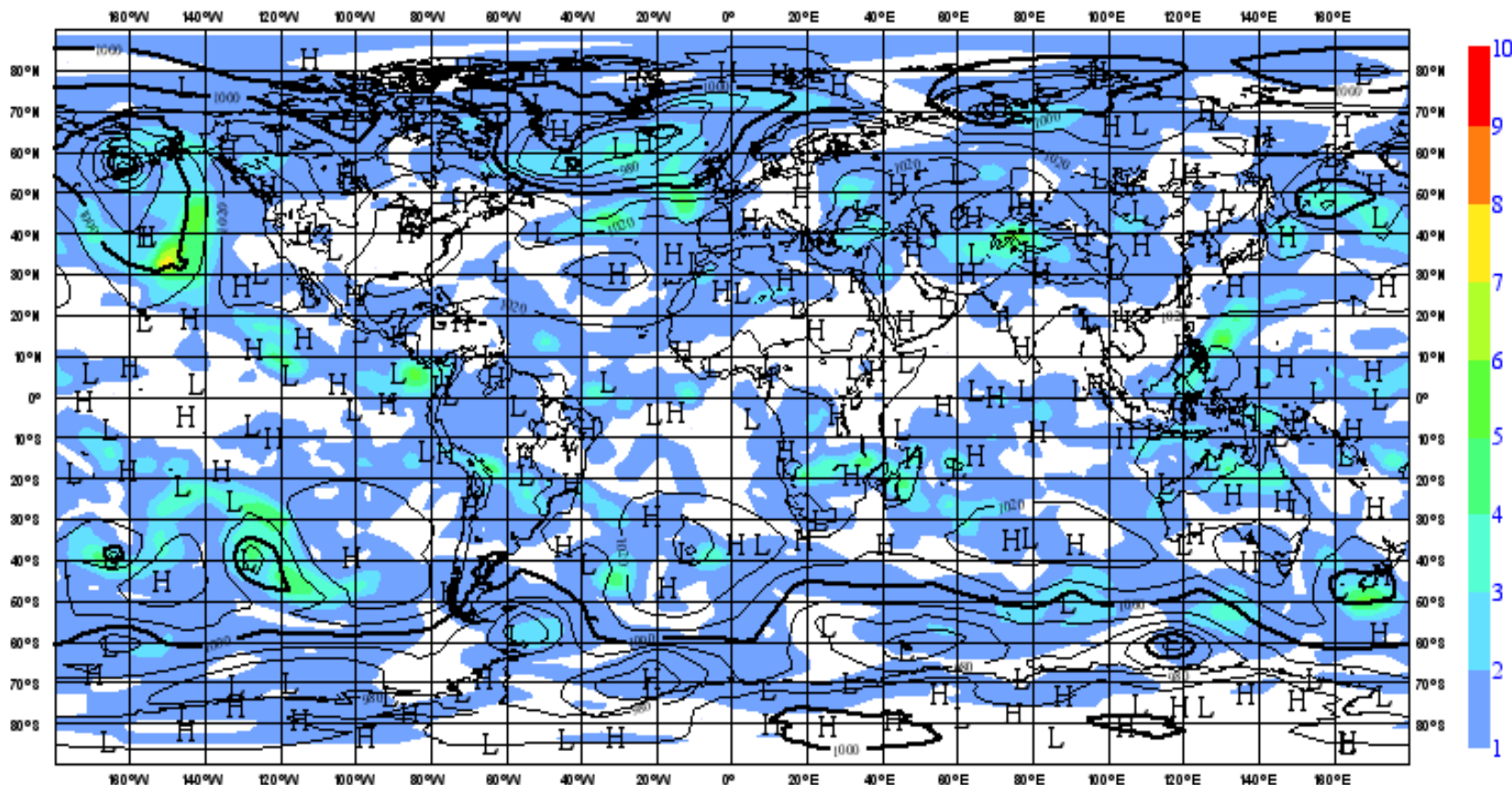
- **Singular vectors: perturbations that grow quickly over the first 48 hours of the forecast**
- **Best approach given limited available computer resources**

# ENS initial perturbations

- **SV- and EDA-based perturbations have different characteristics:**
  - **EDA-based perturbations are less localized than SV-based perturbations and have a smaller scale. They have a larger amplitude over the tropics. EDA-perturbations are more barotropic than SV-based perturbations, and grow less rapidly.**
  - **At initial time, SV-based perturbations have a larger amplitude in potential than kinetic energy, while EDA-based perturbations have a similar amplitude in potential and kinetic energy**
- **Since June 2010 SV- and EDA-based perturbations are used together to construct the initial perturbations for the EPS**
- **The perturbations are constructed so that all perturbed members are equally likely**
- **All perturbations are flow-dependent: they are different from day to day**

# Ensembles of Data Assimilation (EDA)

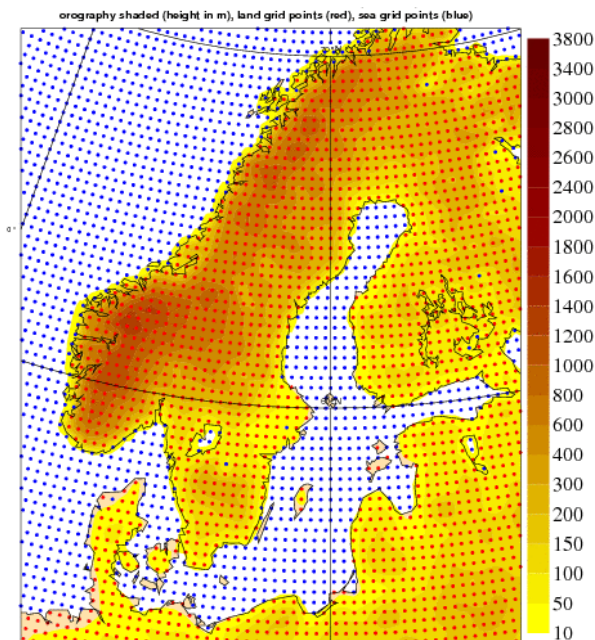
The ensemble spread is flow-dependent but noisy. A filter is applied to remove it. This plot shows the EDA std in terms of vorticity at 500 hPa, +9h after filtering.



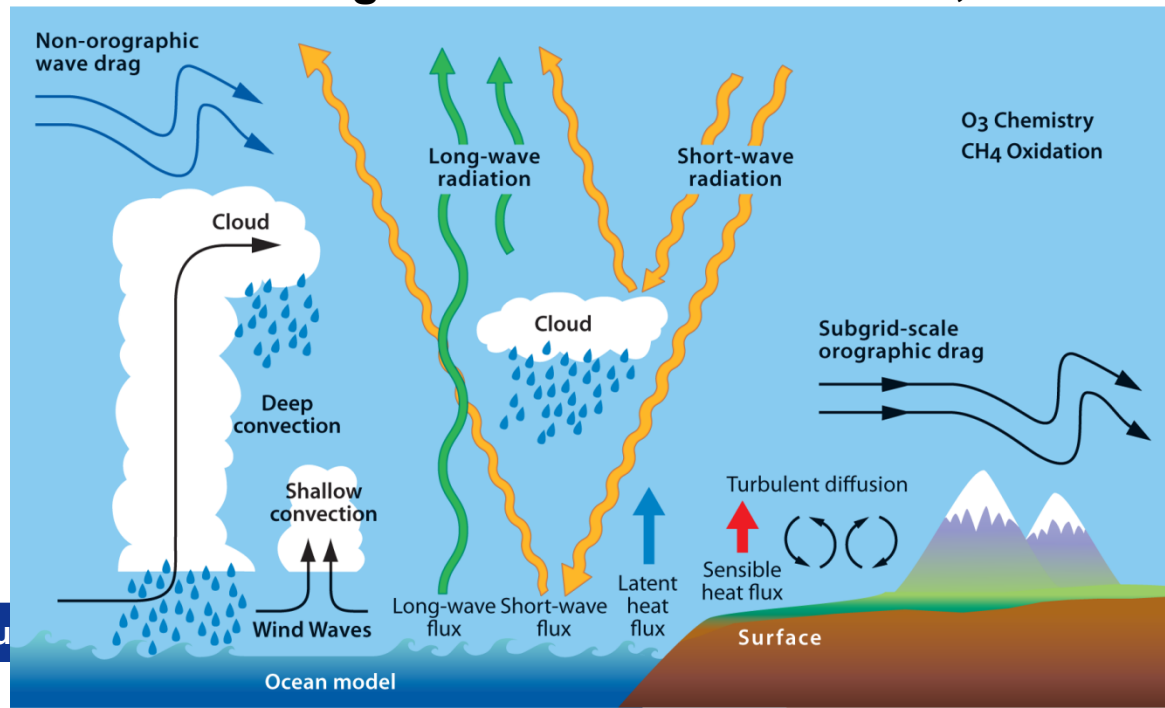


# Model uncertainties – stochastic physics

- Parametrization – represent effects of unresolved (or partly resolved) processes on the resolved model state
- Statistical ensemble of sub-grid scale processes within a grid box; in equilibrium with grid-box mean flow
- Stochastic physics represents statistical uncertainty
  - allows for energy transfer from sub-grid scale to resolved flow, non-local effects

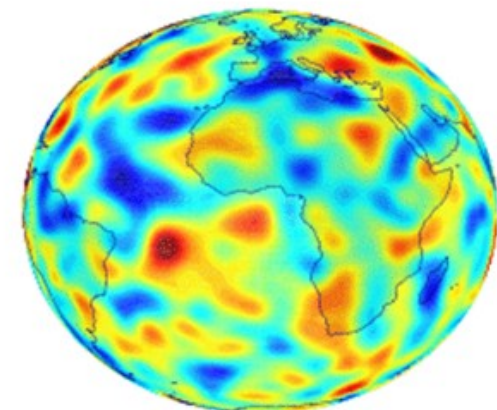
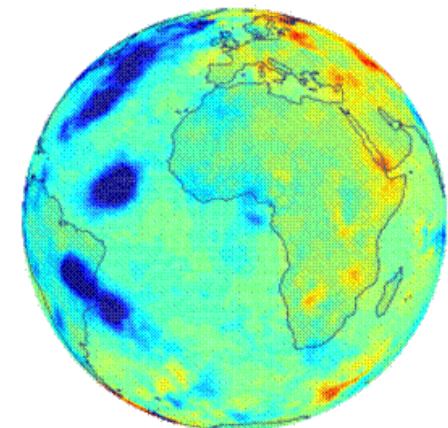
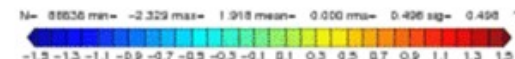
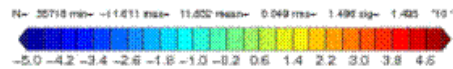


WF Produ



# Model uncertainties – stochastic physics

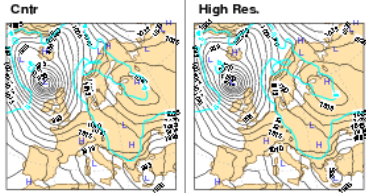
- 2 components
- Stochastically Perturbed Parametrization Tendencies (SPPT)
  - Random pattern of perturbation to model fields
  - Initial scheme introduced 1999, revised 2009 (cycle 35r3)
- Spectral stochastic backscatter scheme (SPBS)
  - A fraction of the dissipated energy is backscattered upscale and acts as streamfunction forcing for the resolved-scale flow
  - Introduced in addition to SPPT in November 2010 (cycle 36r4)



# The ECMWF ensemble

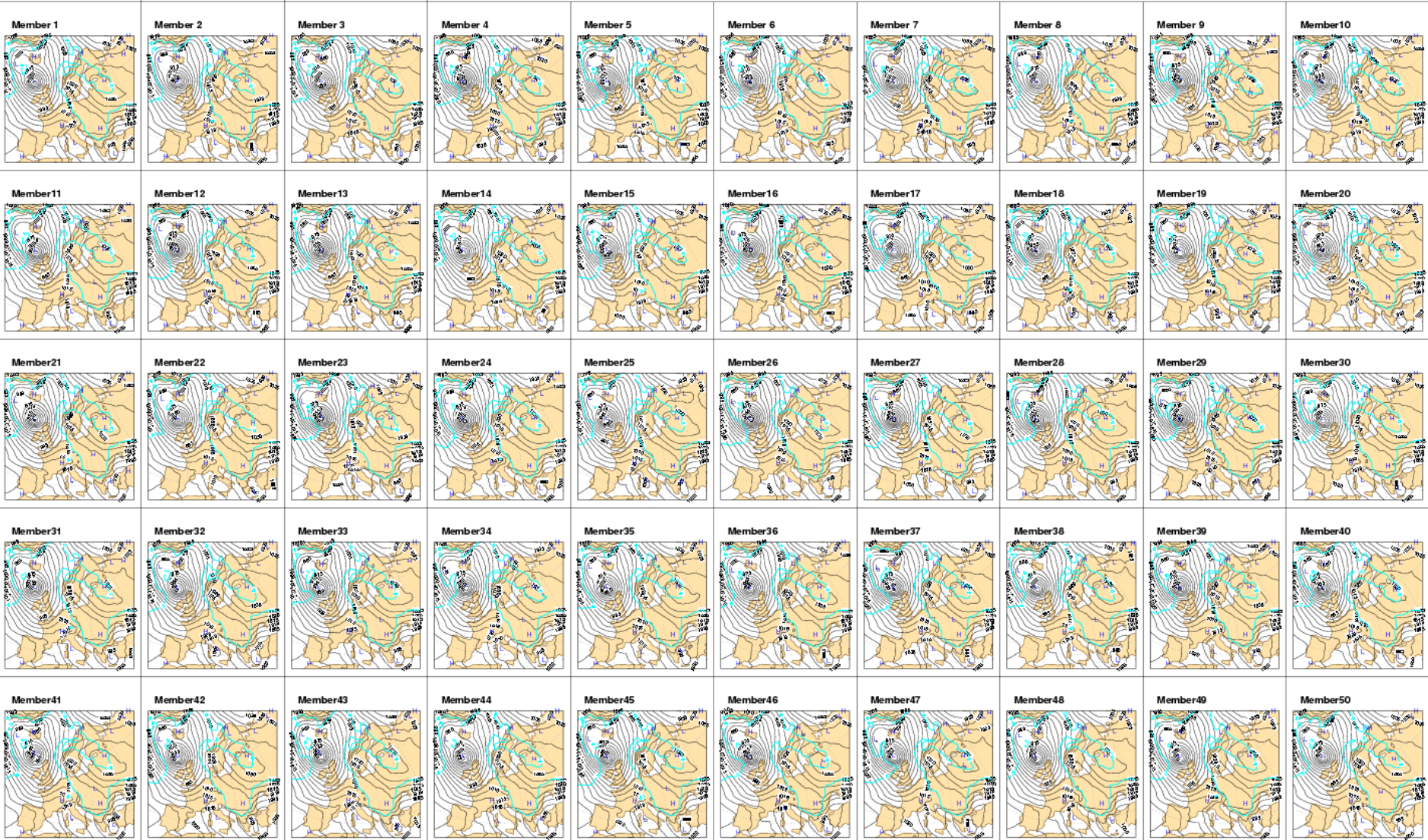
- **91 levels, 32km (T639) to day 10, then 65km (T319) to day 15**
- **1 control + 50 perturbed members**
- **Runs twice per day (00 and 12)**
- **Coupled to ocean model from start of forecast**
- **Extended to 32 days twice per week for monthly forecast (00 Thursday, Monday)**





## ECMWF ENSEMBLE FORECASTS

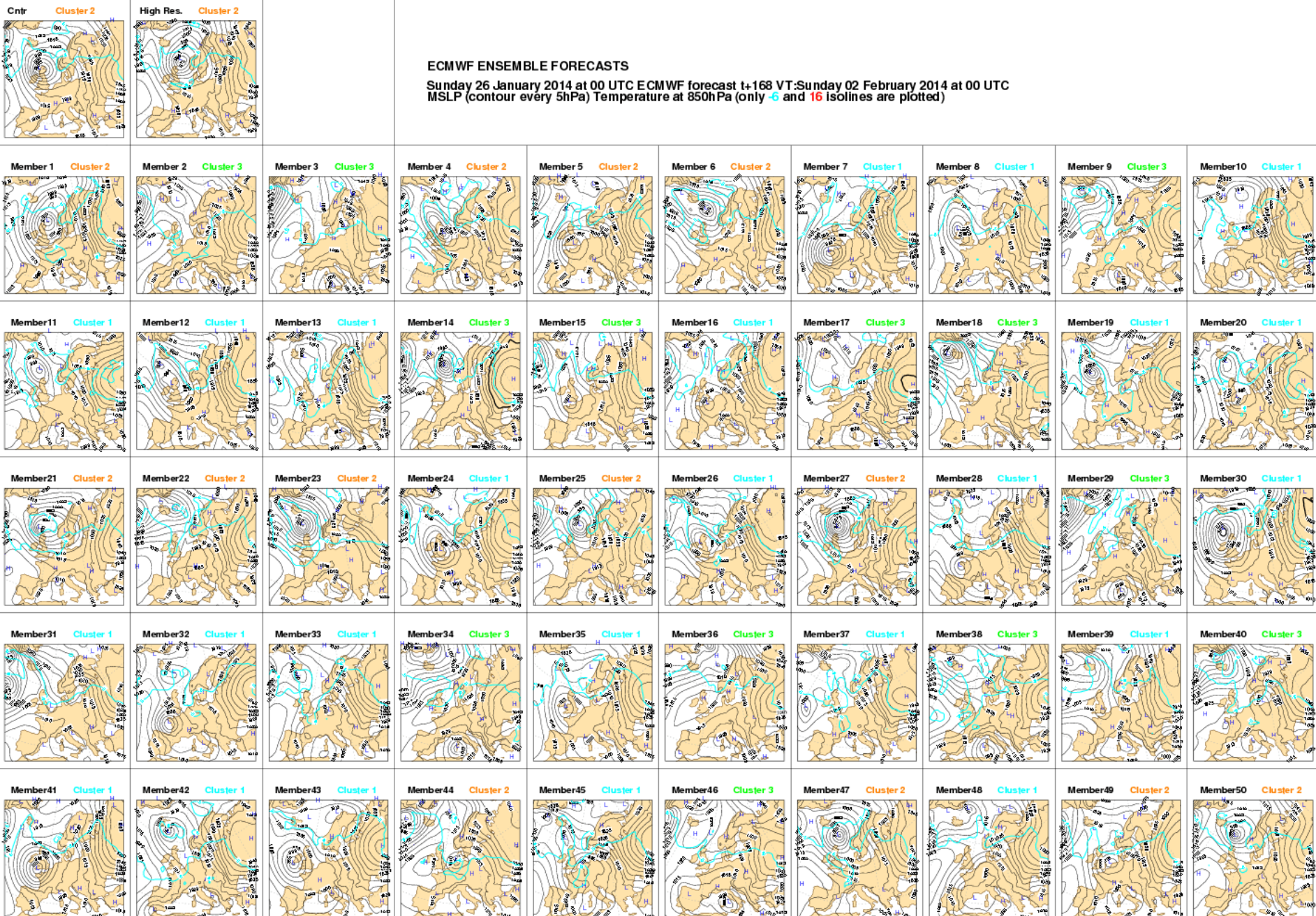
Sunday 26 January 2014 at 00 UTC ECMWF forecast t+12 VT: Sunday 26 January 2014 at 12 UTC  
MSLP (contour every 5hPa) Temperature at 850hPa (only -6 and 16 isolines are plotted)



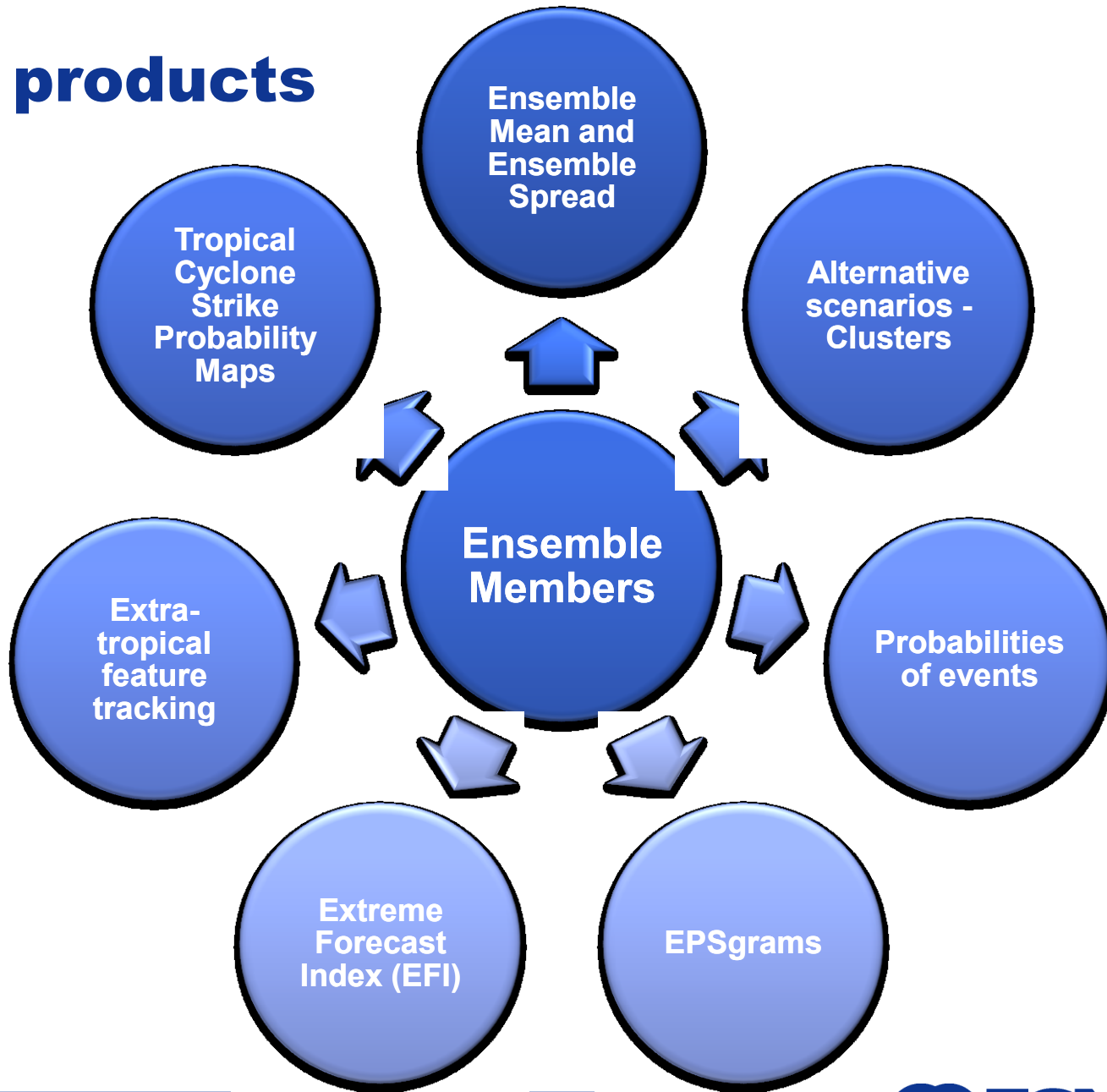


## ECMWF ENSEMBLE FORECASTS

Sunday 26 January 2014 at 00 UTC ECMWF forecast t-168 VT: Sunday 02 February 2014 at 00 UTC  
MSLP (contour every 5hPa) Temperature at 850hPa (only -6 and 16 Isolines are plotted)

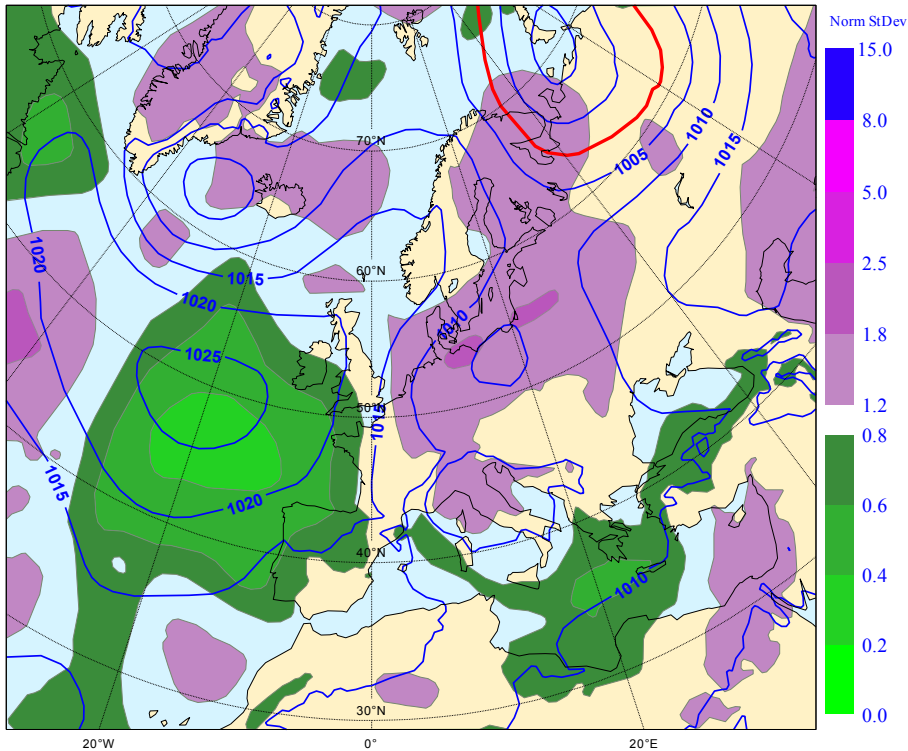


# ENS products

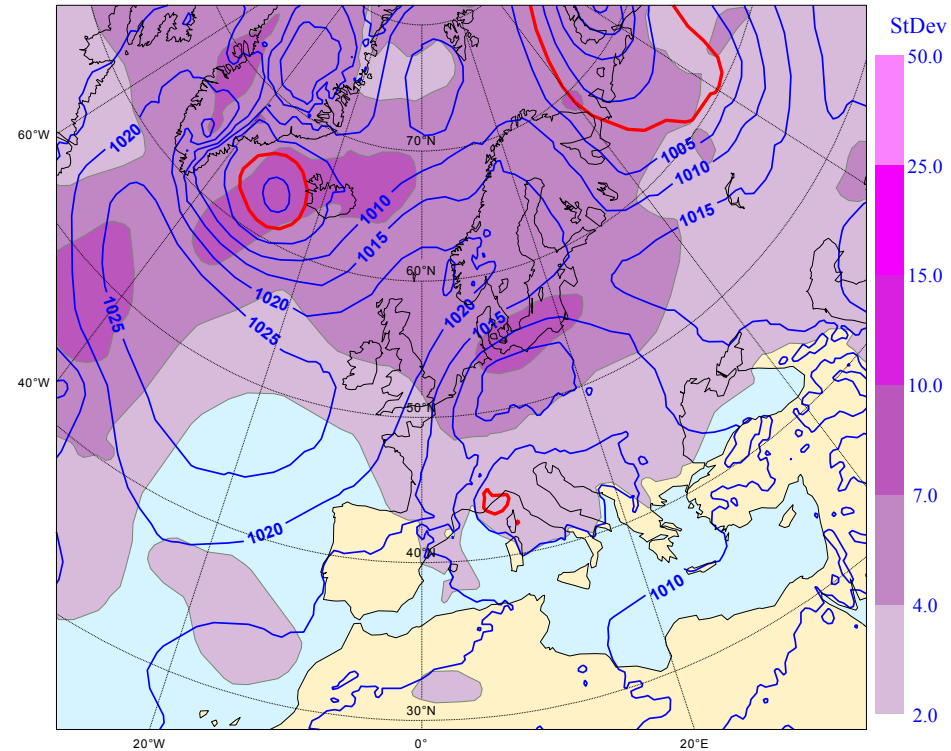


# Ensemble mean and spread

Monday 11 October 2010 12UTC ECMWF Forecast t+120 VT: Saturday 16 October 2010 12UTC  
Mean sea level pressure (MSLP) Ensemble Mean and Normalised Standard Deviation (shaded)



Monday 11 October 2010 12UTC ECMWF Forecast t+120 VT: Saturday 16 October 2010 12UTC  
Mean sea level pressure (MSLP) Deterministic Forecast and Standard Deviation (shaded)





# ENS forecasts: timeseries (EPSgram)

Highest value of all members

90<sup>th</sup> centile

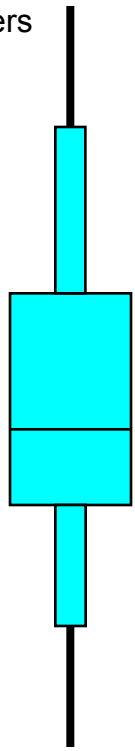
75<sup>th</sup> centile

Median

25<sup>th</sup> centile

10<sup>th</sup> centile

Lowest value of all members

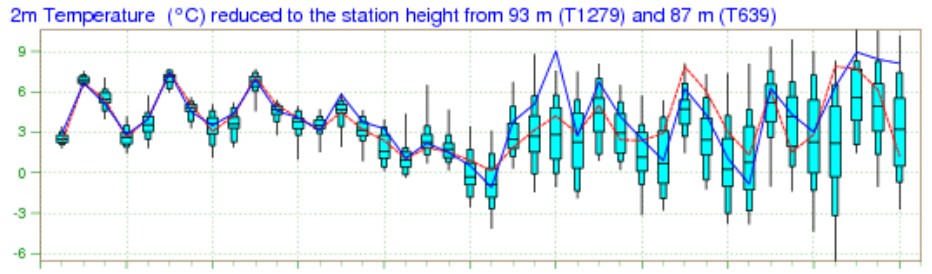
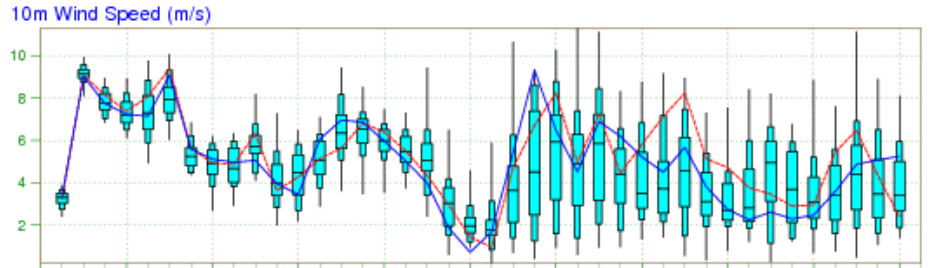
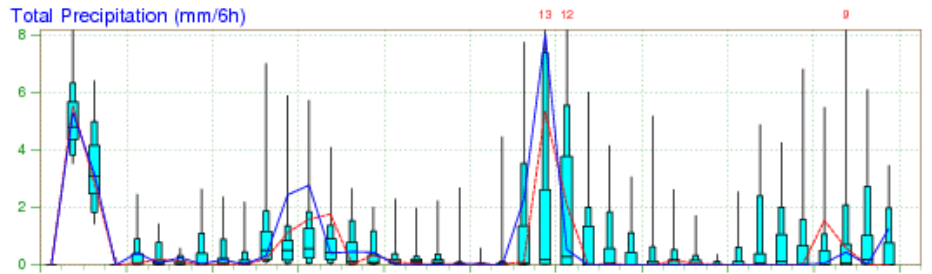
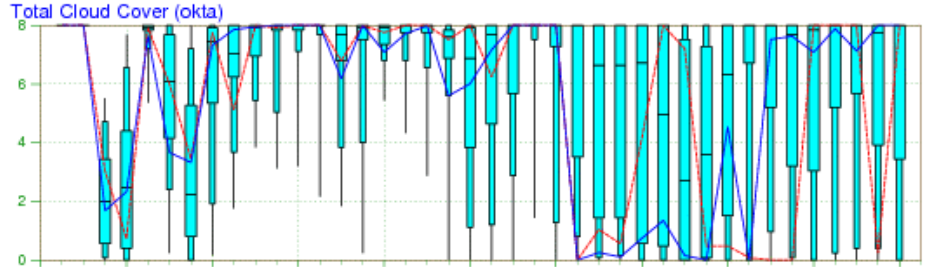


## EPSgram for Reading

Start Sun 26/01/14 00 UTC

Use and Interpretation of ECMWF Products Janu

EPS Meteogram  
Reading 51.57°N 0.83°W (EPS land point) 48 m  
Deterministic Forecast and EPS Distribution Sunday 26 January 2014 00 UTC



Sun 26 Mon 27 Tue 28 Wed 29 Thu 30 Fri 31 Sat 1 Sun 2 Mon 3 Tue 4  
January 2014 February 2014

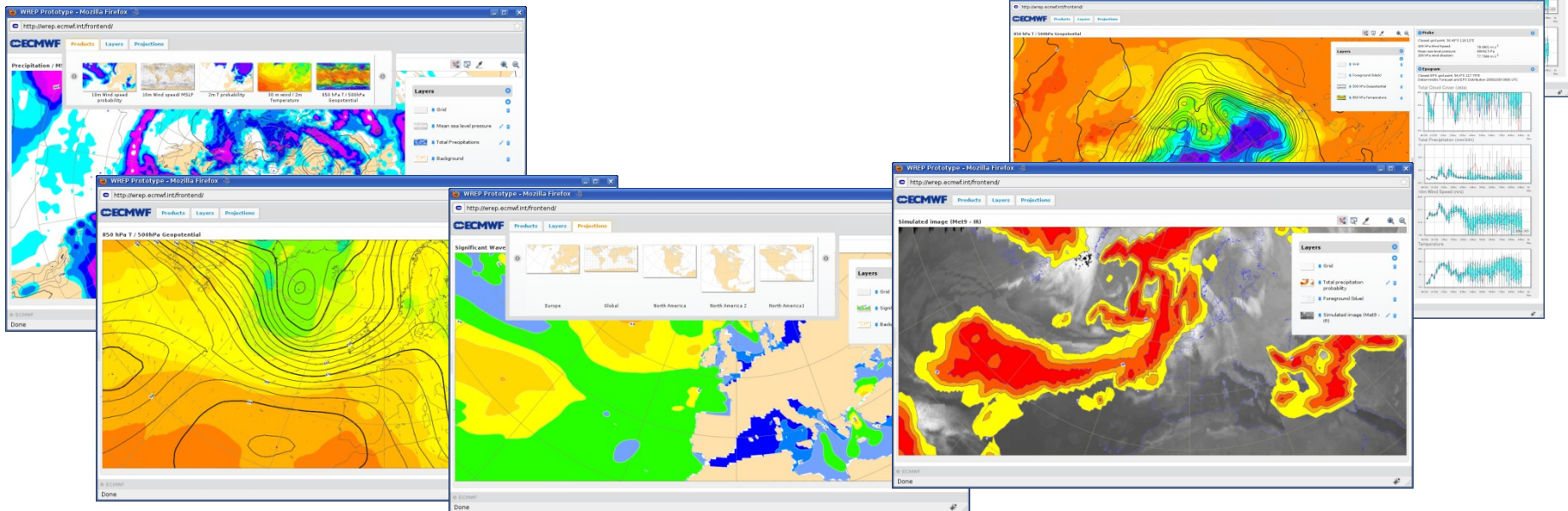
max 90% 75% median 25% 10% min

EPS Control(31 km) High Resolution Deterministic(16 km)

Magnits++ 2.5.1

# ecCharts

- Interactivity: zooming, panning, ...
- Customisation:
  - Probabilities threshold, ...
  - Show/hide, add/remove layers
- Related products: Meteograms



# Ensemble skill Z500 Europe

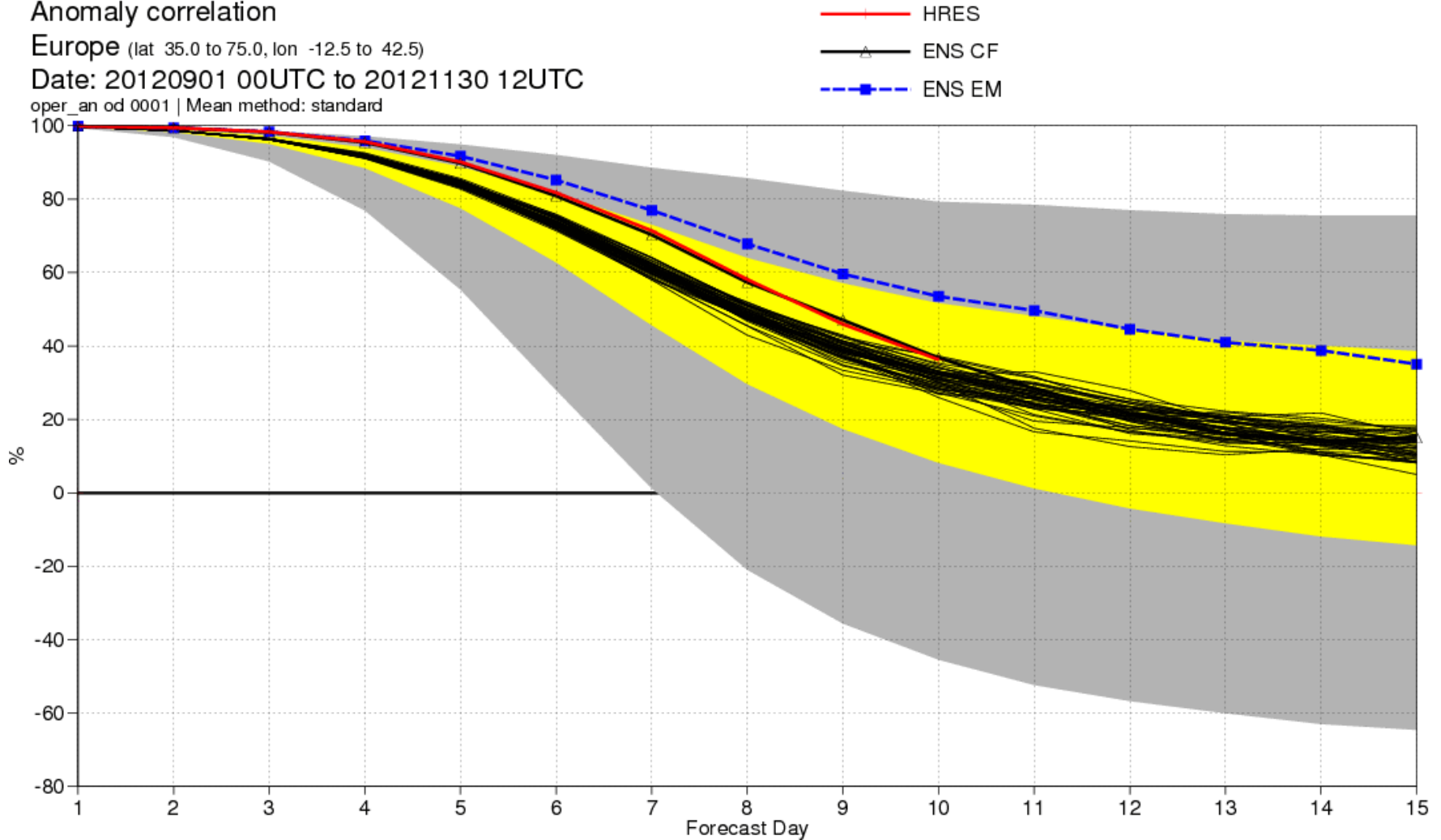
500hPa geopotential

Anomaly correlation

Europe (lat 35.0 to 75.0, lon -12.5 to 42.5)

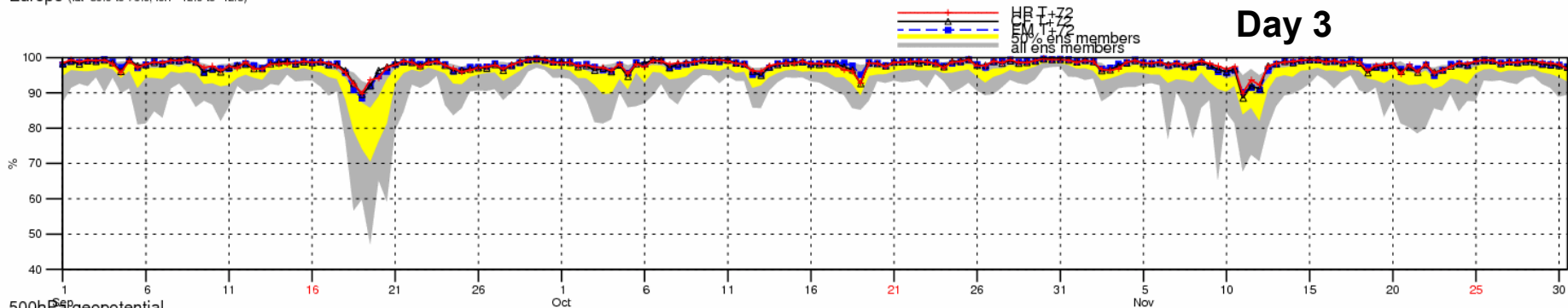
Date: 20120901 00UTC to 20121130 12UTC

oper\_an od 0001 | Mean method: standard

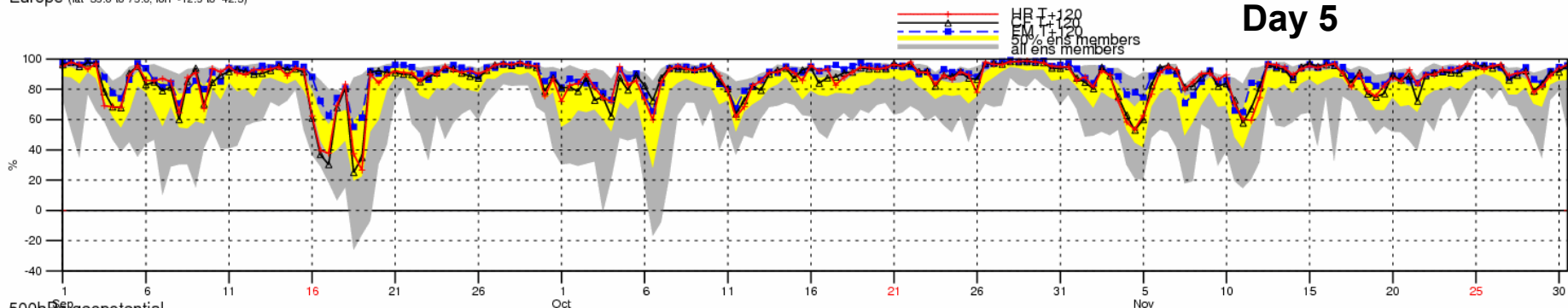


# Ensemble: Z500 Europe

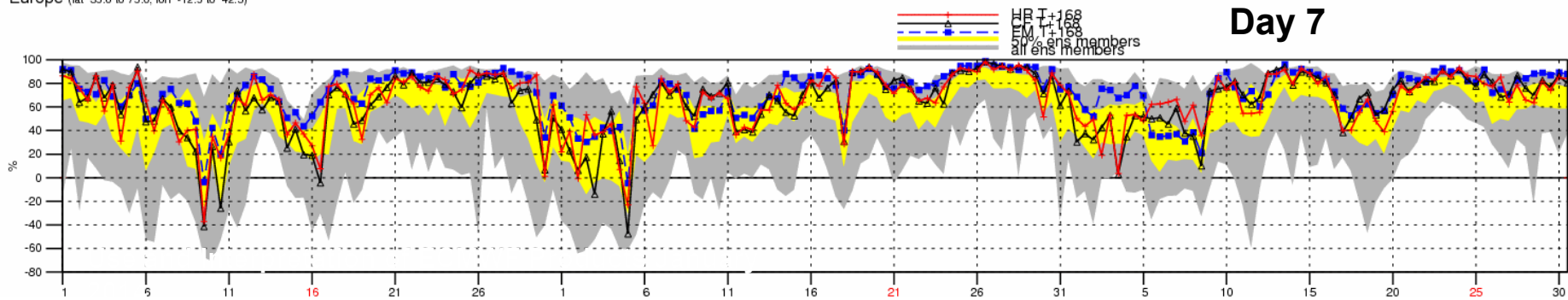
500hPa geopotential  
Anomaly correlation  
Europe (lat 35.0 to 75.0, lon -12.5 to 42.5)



500hPa geopotential  
Anomaly correlation  
Europe (lat 35.0 to 75.0, lon -12.5 to 42.5)

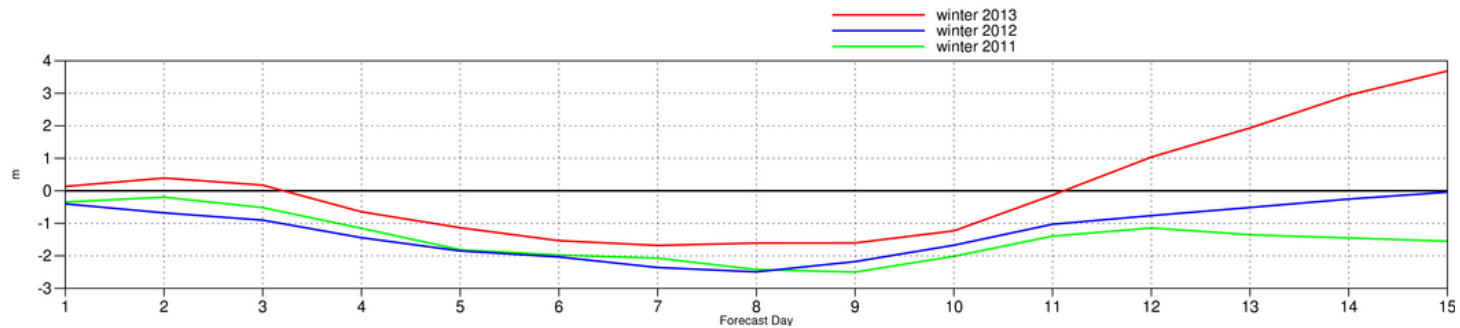
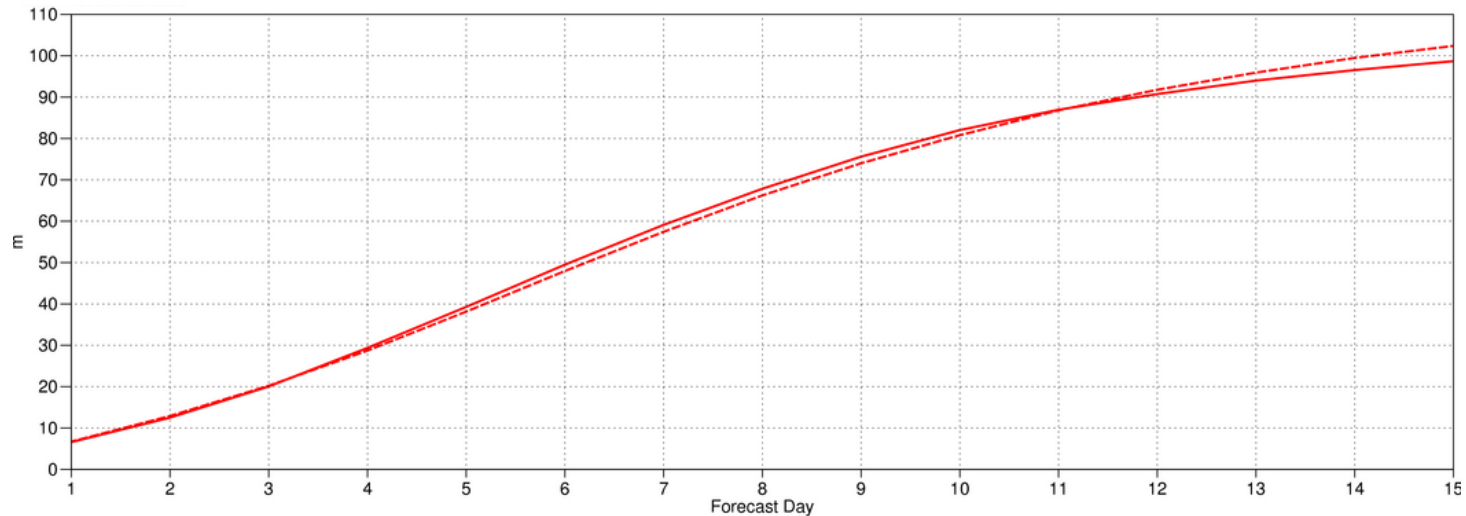


500hPa geopotential  
Anomaly correlation  
Europe (lat 35.0 to 75.0, lon -12.5 to 42.5)





# ENS spread and error, Z500, N.Hem

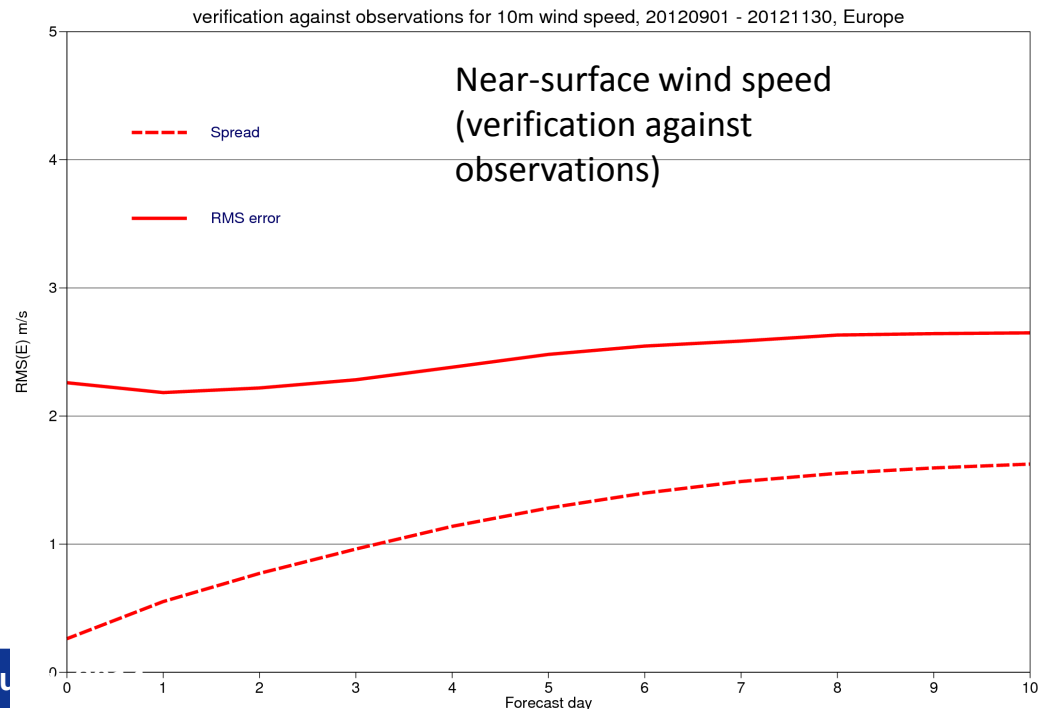


EPS spread (dashed), RMS error of ensemble-mean (full lines), and their difference (below) for Z500 hPa in winter 2010-11 (green), 2011-12 (blue) and 2012-13 (red).

# Surface perturbations

- ENS had too little spread for near surface weather parameters (e.g. 10-m wind)
  - representativeness (an individual observation is not equivalent to a model grid box average) and errors in the observations
  - ENS resolution: difficult to represent small-scale phenomena such as sting jets
  - Additional sources of uncertainty?
- Land-surface perturbations
  - Added November 2013

Ensemble spread (dashed) and root-mean-square error of ensemble-mean (solid) autumn (September-November) 2012 over Europe



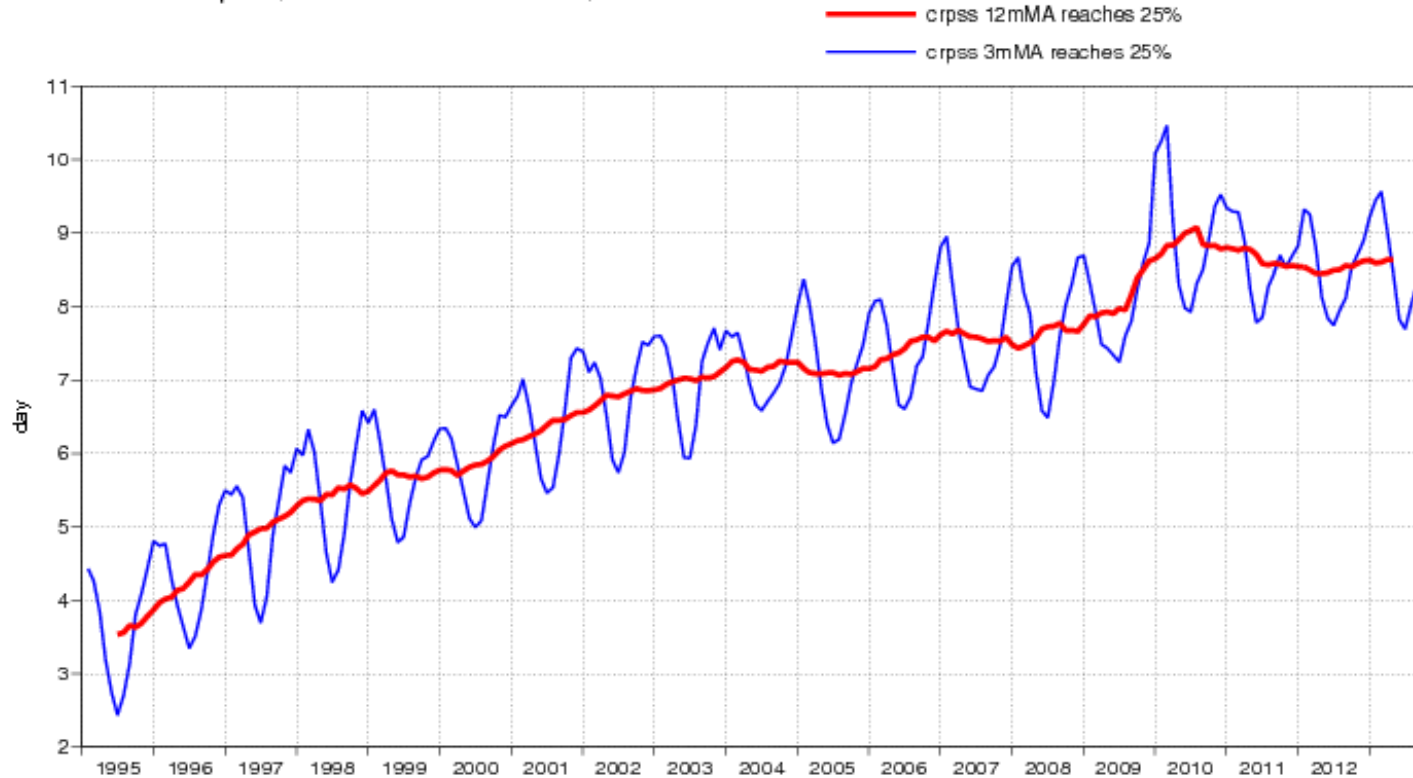
# ENS Probabilistic Score CRPSS, Temperature at 850 hPa N hemisphere

## ECMWF EPS 00,12UTC forecast skill

850hPa temperature

Lead time of Continuous ranked probability skill score reaching 25%

NHem Extratropics (lat 20.0 to 90.0, lon -180.0 to 180.0)

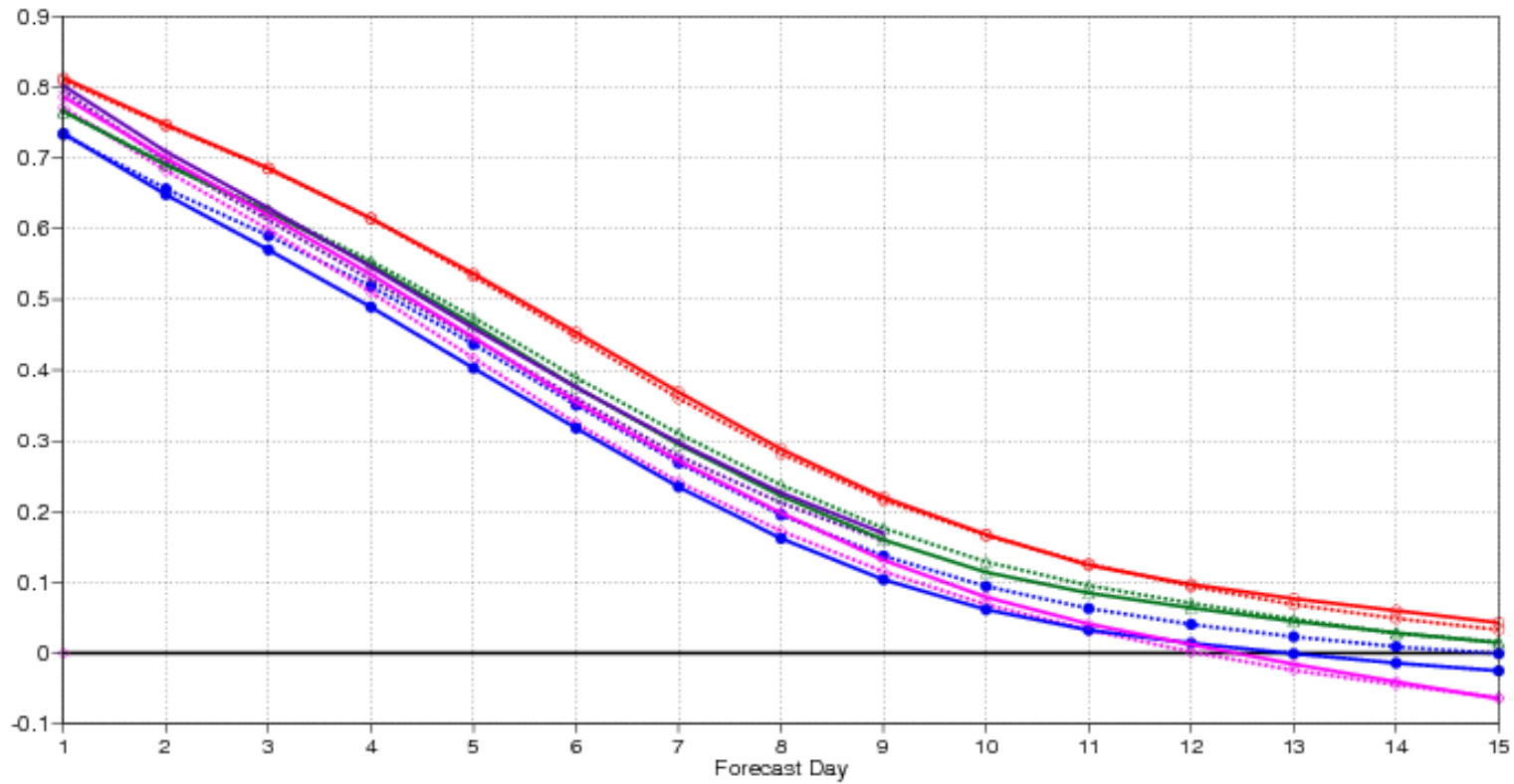
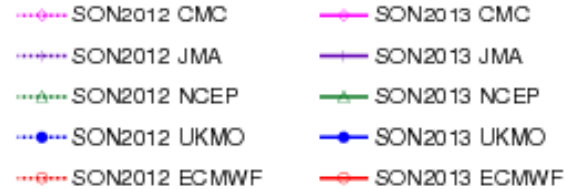


Monthly score (blue), and 12-month running mean (red) of Continuous Ranked Probability Skill Score. Day at which score reaches 25%.

# ENS Probabilistic Score

## CRPSS, Temperature at 850 hPa N hemisphere

850hPa temperature  
Continuous ranked probability skill score  
NHem Extratropics (lat 20.0 to 90.0, lon -180.0 to 180.0)  
SepOctNov



# Extreme forecast index (EFI)

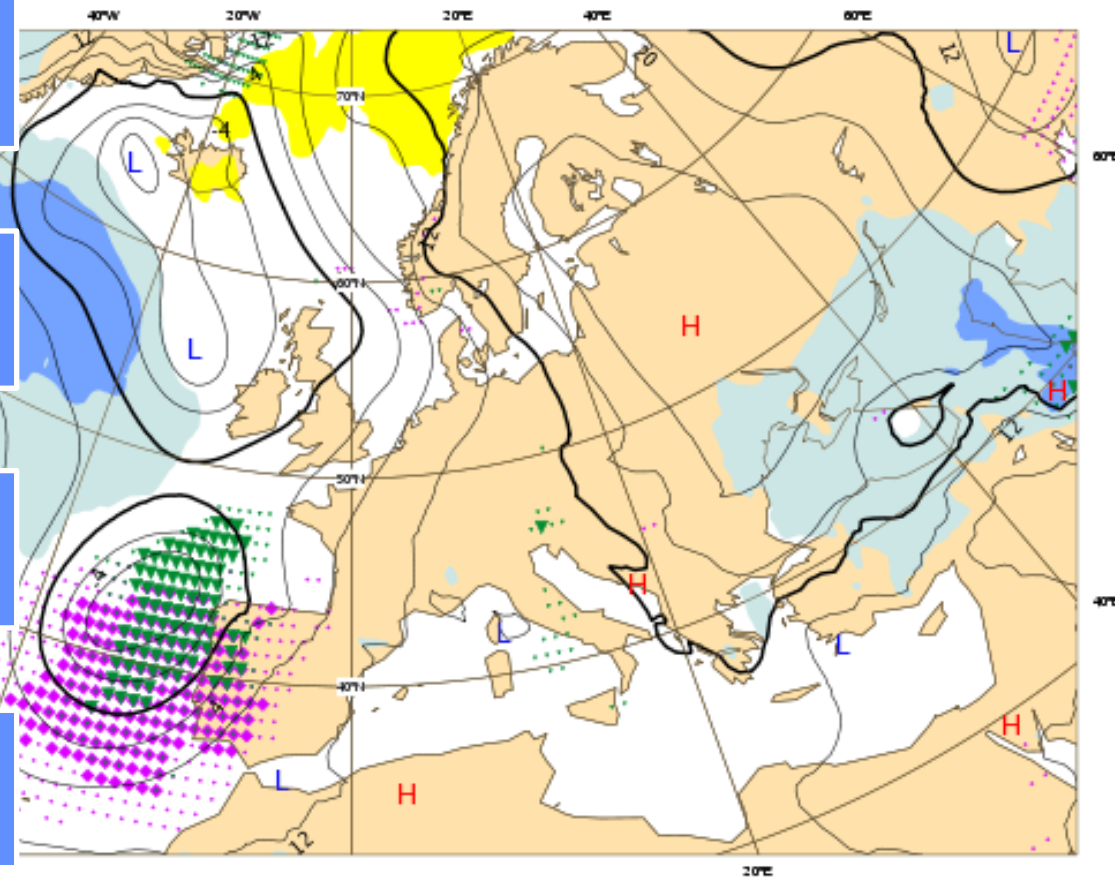
Anomalous weather predicted by EPS: Tuesday 25 October 2011 at 00 UTC  
1000 hPa Z ensemble mean ( Wednesday 26 October 2011 at 12 UTC)  
and EFI values for Total precipitation, maximum 10m wind gust and mean 2m temperature (all 24h)  
valid for 24hours from Wednesday 26 October 2011 at 00 UTC to Thursday 27 October 2011 at 00 UTC

Is computed for temperature, precipitation, wind speed and wind gusts

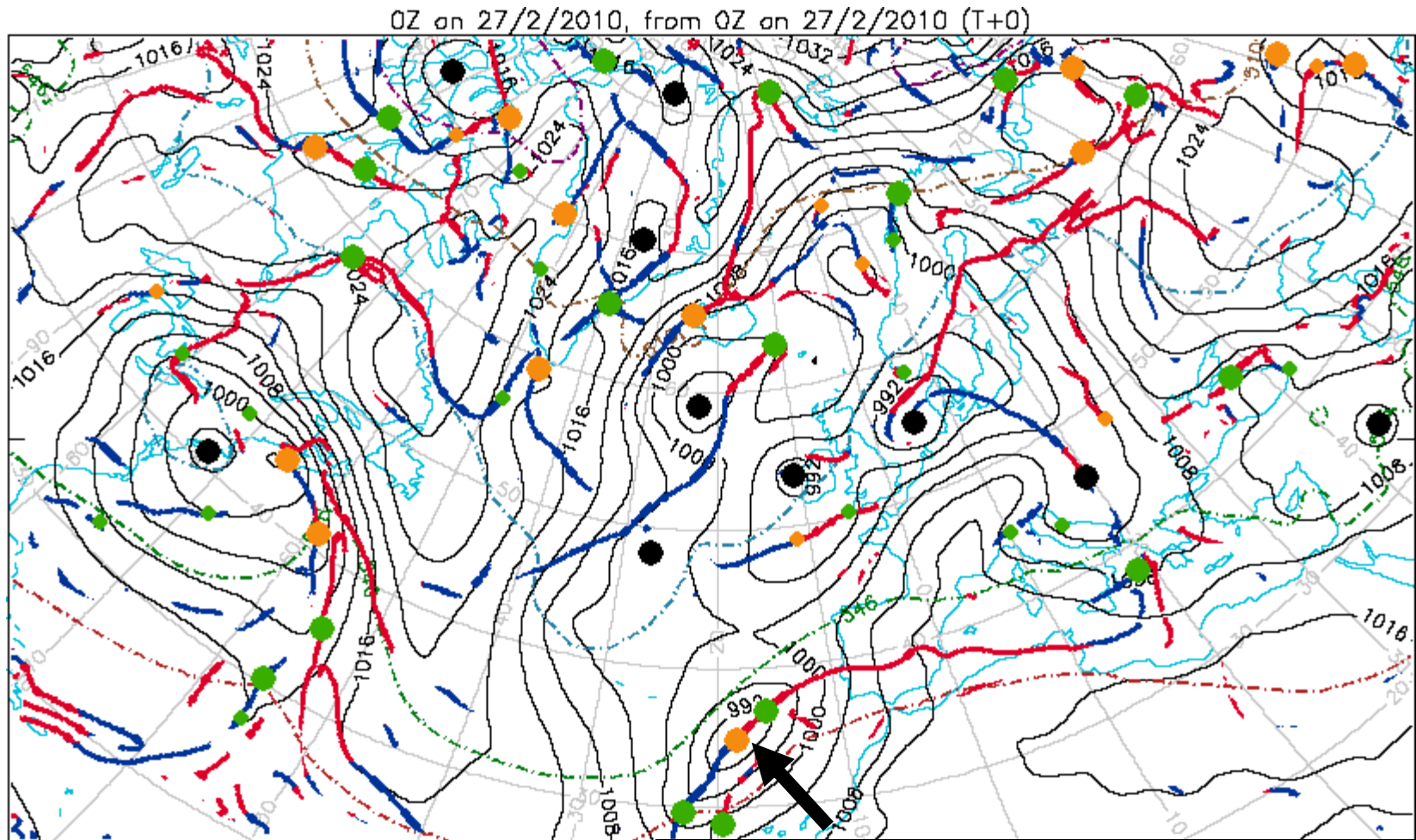
Measures the distance between the EPS cumulative distribution and the model climate distribution

Ranges from -1 (all members break climate minimum records) to +1 (all beyond model climate records)

Indicates places where the EPS distribution is towards the extreme of the climate distribution

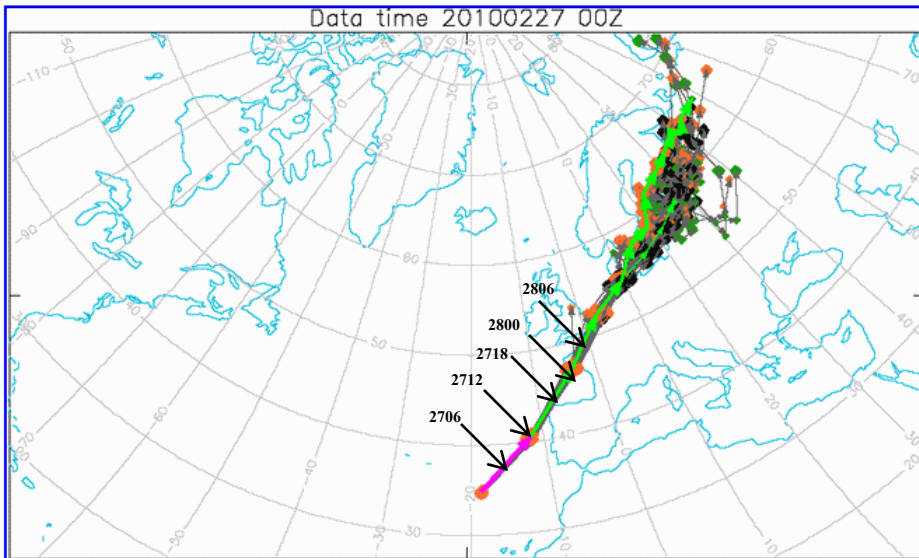


# Extra-tropical feature tracking: Xynthia



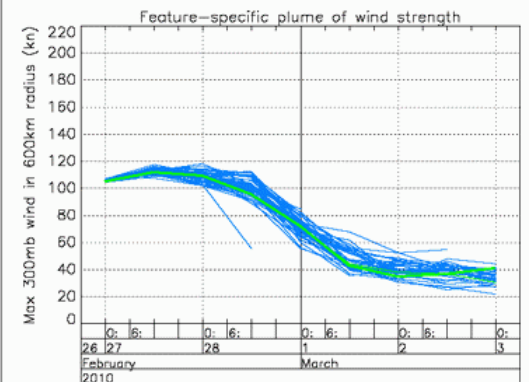
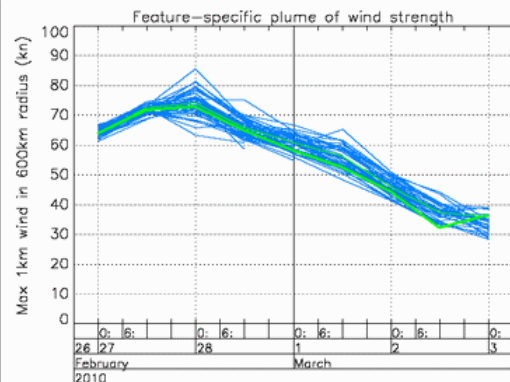
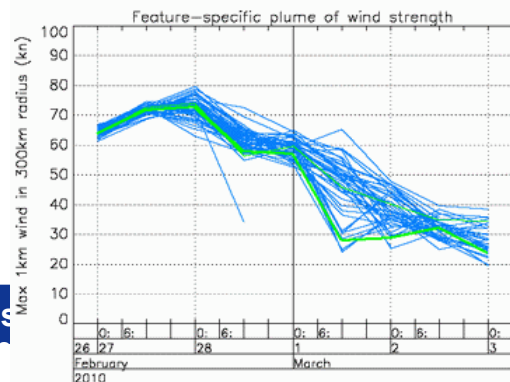
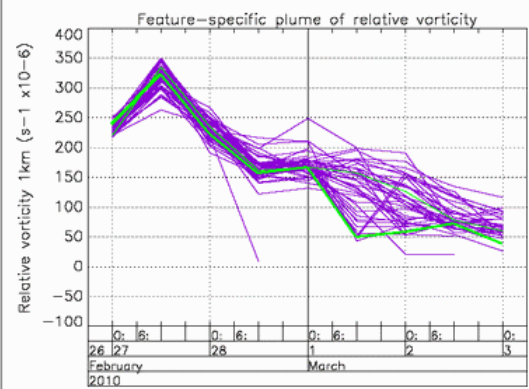
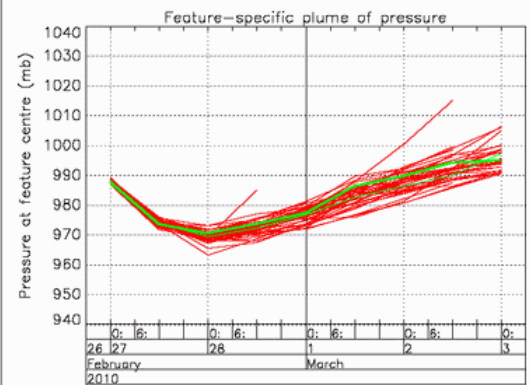
User can click on any spot (= cyclonic feature) to see how that feature evolves in the EPS





Percentage of members in track, and a list of the member numbers:

T+ 0: 100%	Det. 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50
T+ 12: 100%	Det. 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50
T+ 24: 100%	Det. 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50
T+ 36: 100%	Det. 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50
T+ 48: 94%	Det. 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 17, 18, 19, 20, 21, 22, 23, 25, 28, 27, 28, 29, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50
T+ 60: 78%	Det. 0, 1, 3, 4, 5, 6, 7, 8, 9, 11, 12, 14, 15, 17, 18, 19, 21, 25, 26, 27, 28, 29, 31, 32, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 47, 48, 49, 50
T+ 72: 76%	Det. 0, 1, 3, 4, 5, 6, 7, 8, 9, 11, 12, 14, 15, 17, 18, 19, 21, 25, 26, 27, 28, 29, 31, 32, 34, 35, 36, 37, 38, 39, 41, 42, 43, 44, 45, 47, 48, 49, 50
T+ 84: 73%	Det. 0, 1, 3, 4, 5, 6, 7, 8, 9, 11, 12, 14, 17, 18, 19, 21, 25, 26, 27, 28, 31, 32, 34, 35, 36, 37, 38, 39, 41, 42, 43, 44, 45, 47, 48, 49, 50
T+ 96: 61%	Det. 0, 1, 3, 4, 5, 6, 7, 8, 9, 12, 14, 17, 18, 19, 21, 25, 28, 31, 32, 34, 35, 36, 37, 38, 42, 43, 44, 45, 47, 48, 50

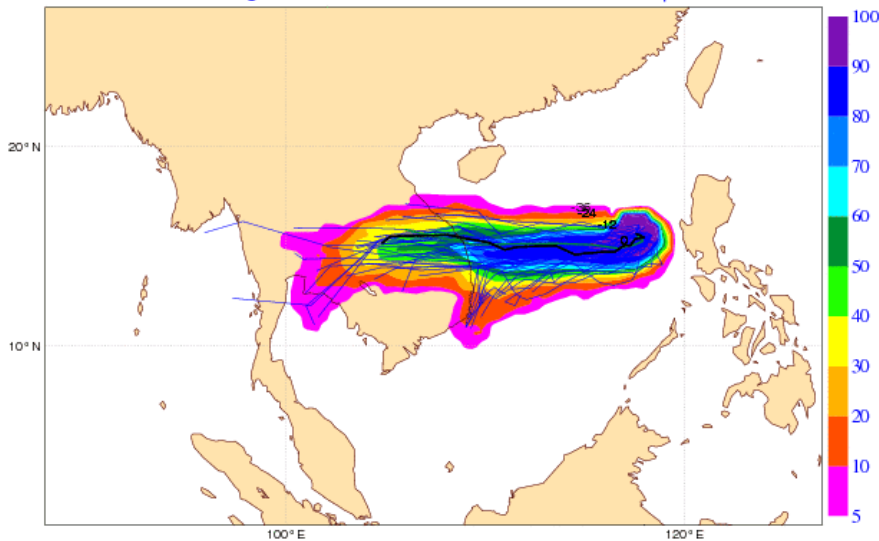


# Tropical cyclone tracks

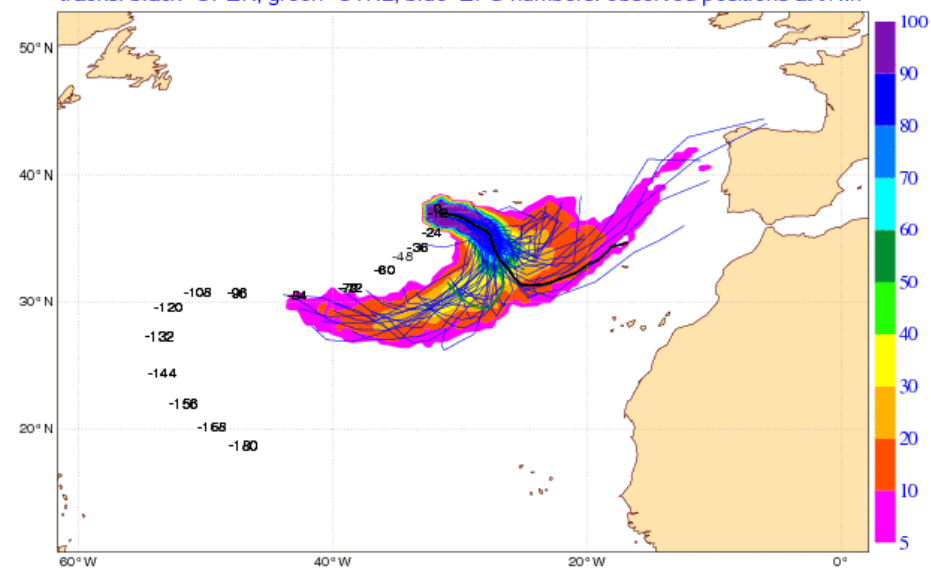
## Gamei

## Nadine

20121003 0 UTC  
Probability that GAEMI will pass within 120km radius during the next 120 hours  
tracks: black=OPER, green=CTRL, blue=EPS numbers: observed positions at t+..h



20120920 0 UTC  
Probability that NADINE will pass within 120km radius during the next 120 hours  
tracks: black=OPER, green=CTRL, blue=EPS numbers: observed positions at t+..h



strike probability

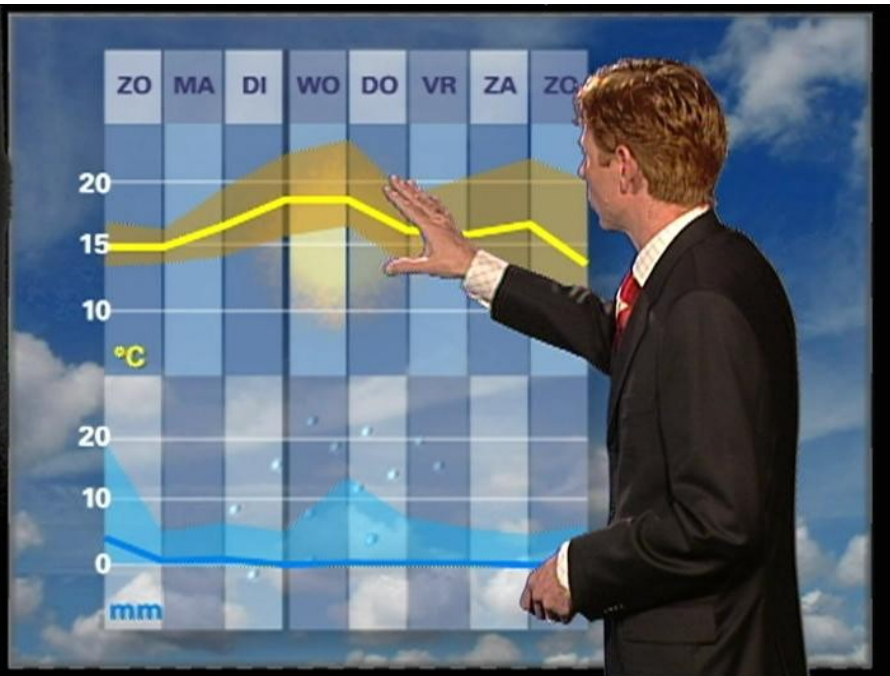


**Great! But how can that help users  
who must make yes/no decisions?**

# ENS – communicating uncertainty

- **All forecasts have errors**
- **It can be important for the user to know about the uncertainty in a forecast**
  - **what else could happen? what is the worst possibility?**
- **This is not a new idea**
  - **Forecasters are used to adjusting their forecast with their experience of model errors (flow dependence, forecast range dependency)**
  - **Inconsistency of the forecasts (in time, from one model to the other) were used as indication of the (un-)predictability of scenarios**
- **Ensembles give more information – they provide an explicit, detailed representation of model uncertainties, and potential of unusual events**

# Uncertainty information to public

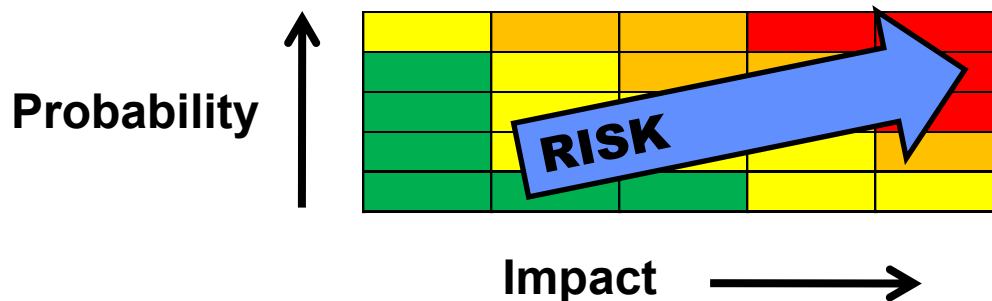


# Uncertainty information to public



# Value: the economic or societal worth of forecasts

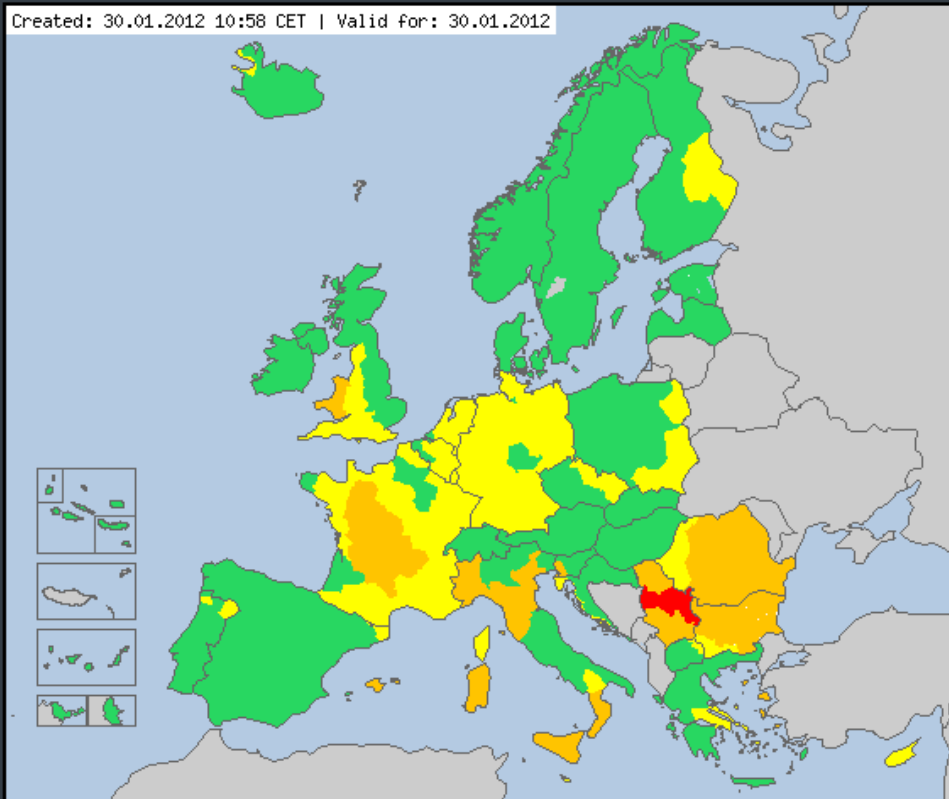
- Forecasts only have value if people use them
  - make a decision or take an action which would not otherwise have been made
- Decisions can be based on deterministic forecasts, but ...
- Decisions involve assessment of risk
- Risk = probability x impact
- To make a good decision need to know the probability and the impact (consequence to the individual user)



# MeteoAlarm

» Europe:

Created: 30.01.2012 10:58 CET | Valid for: 30.01.2012



## Weather warnings: Europe

**Awareness Reports** - You can find detailed information about the warnings in the awareness reports issued for each country. Select the relevant country.

AT		
BE		
BG		
CH		
CY		
CZ		
DE		
DK		
EE		
ES		
FI		
FR		
GR		
HR		
HU		
IE		
IS		
IT		
LU		
LV		
MK		
MT		
NL		
NO		
PL		
PT		
RO		
RS		
SE		
SI		
SK		
UK		

# Summary - why do we run an ensemble?

- The best method we have to produce flow-dependent probabilistic weather forecasts
- The ensemble of forecasts provides a range of future scenarios consistent with our knowledge of the initial state and model capability
  - Provides explicit indication of uncertainty in today's forecast
  - Range of ensemble based products for different users
- Ensembles provide the required input for a range of application models (hydrology, ship routing, energy demand), explicitly propagating the atmospheric uncertainty
- Read more in the ECMWF products User Guide
  - <http://www.ecmwf.int/products/forecasts/guide/>



# Ensemble references

- Berner, J., G. J. Shutts, M. Leutbecher, and T. N. Palmer (2009), A spectral stochastic kinetic energy backscatter scheme and its impact on flow-dependent predictability in the ECMWF ensemble prediction system, *J. Atmos. Sci.*, 66, 603–626.
- Buizza, R., Leutbecher, M., & Isaksen, L., 2008: Potential use of an ensemble of analyses in the ECMWF Ensemble Prediction System. *Q. J. R. Meteorol. Soc.*, 134, 2051-2066.
- Buizza, R., Bidlot, J.-R., Wedi, N., Fuentes, M., Hamrud, M., Holt, G., & Vitart, F., 2007: The new ECMWF VAREPS. *Q. J. Roy. Meteorol. Soc.*, 133, 681-695 (also EC TM 499).
- Buizza, R., 2008: Comparison of a 51-member low-resolution (TL399L62) ensemble with a 6-member high-resolution (TL799L91) lagged-forecast ensemble. *Mon. Wea. Rev.*, 136, 3343-3362 (also EC TM 559).
- Leutbecher, M. 2005: On ensemble prediction using singular vectors started from forecasts. ECMWF TM 462, pp 11.
- Leutbecher, M. & T.N. Palmer, 2008: Ensemble forecasting. *J. Comp. Phys.*, 227, 3515-3539 (also EC TM 514).
- Molteni, F., Buizza, R., Palmer, T. N., & Petroliagis, T., 1996: The new ECMWF ensemble prediction system: methodology and validation. *Q. J. R. Meteorol. Soc.*, 122, 73-119.
- Palmer, T N, Buizza, R., Leutbecher, M., Hagedorn, R., Jung, T., Rodwell, M, Virat, F., Berner, J., Hagel, E., Lawrence, A., Pappenberger, F., Park, Y.-Y., van Bremen, L., Gilmour, I., & Smith, L., 2007: The ECMWF Ensemble Prediction System: recent and on-going developments. A paper presented at the 36th Session of the ECMWF Scientific Advisory Committee (also EC TM 540).
- Palmer, T. N., Buizza, R., Doblas-Reyes, F., Jung, T., Leutbecher, M., Shutts, G. J., Steinheimer M., & Weisheimer, A., 2009: Stochastic parametrization and model uncertainty. ECMWF RD TM 598, Shinfield Park, Reading RG2-9AX, UK, pp. 42.
- Richardson, D. S., 2000. Skill and relative economic value of the ECMWF Ensemble Prediction System. *Q. J. R. Meteorol. Soc.*, 126, 649-668.
- Richardson, D.S., 2003. Economic value and skill. In *Forecast verification: a practitioner's guide in atmospheric science*, Jolliffe, I. T. and Stephenson, D. B., Eds., Wiley, 240pp.
- Vitart, F., Buizza, R., Alonso Balmaseda, M., Balsamo, G., Bidlot, J. R., Bonet, A., Fuentes, M., Hofstadler, A., Molteni, F., & Palmer, T. N., 2008: The new VAREPS-monthly forecasting system: a first step towards seamless prediction. *Q. J. Roy. Meteorol. Soc.*, 134, 1789-1799.
- Zsoter, E., Buizza, R., & Richardson, D., 2009: 'Jumpiness' of the ECMWF and UK Met Office EPS control and ensemble-mean forecasts'. *Mon. Wea. Rev.*, 137, 3823-3836.



# Decision analysis - the cost-loss model

- **Simplest possible case - but shows many important features**
- **There are only two important weather types: weather is either “good” or “bad”**
- **A particular user or decision maker will be affected by bad weather - they have a choice of two actions**
  - **If they do nothing and bad weather occurs they suffer a loss  $L$**
  - **However, they can decide to take some protective action to prevent this possible loss, but it will cost  $C$**

# Why is the probability forecast better?

- **If the cost of protection is high wait until event is more certain**
  - **False alarms are more important**
- **If the loss is greater then protect even at low probability**
  - **Missed events are more important**
- **Changing the probability threshold at which to take action gives different hit rates and false alarm rates**
- **The optimal probability threshold depends on the user:  $p_t = C/L$**
- **Using the probabilities allows decision makers to take decisive action according to their own risks – these are different for each user**
- **Even if the user does not have an explicit cost/loss they are still aware of the relative importance of false alarms and missed events**

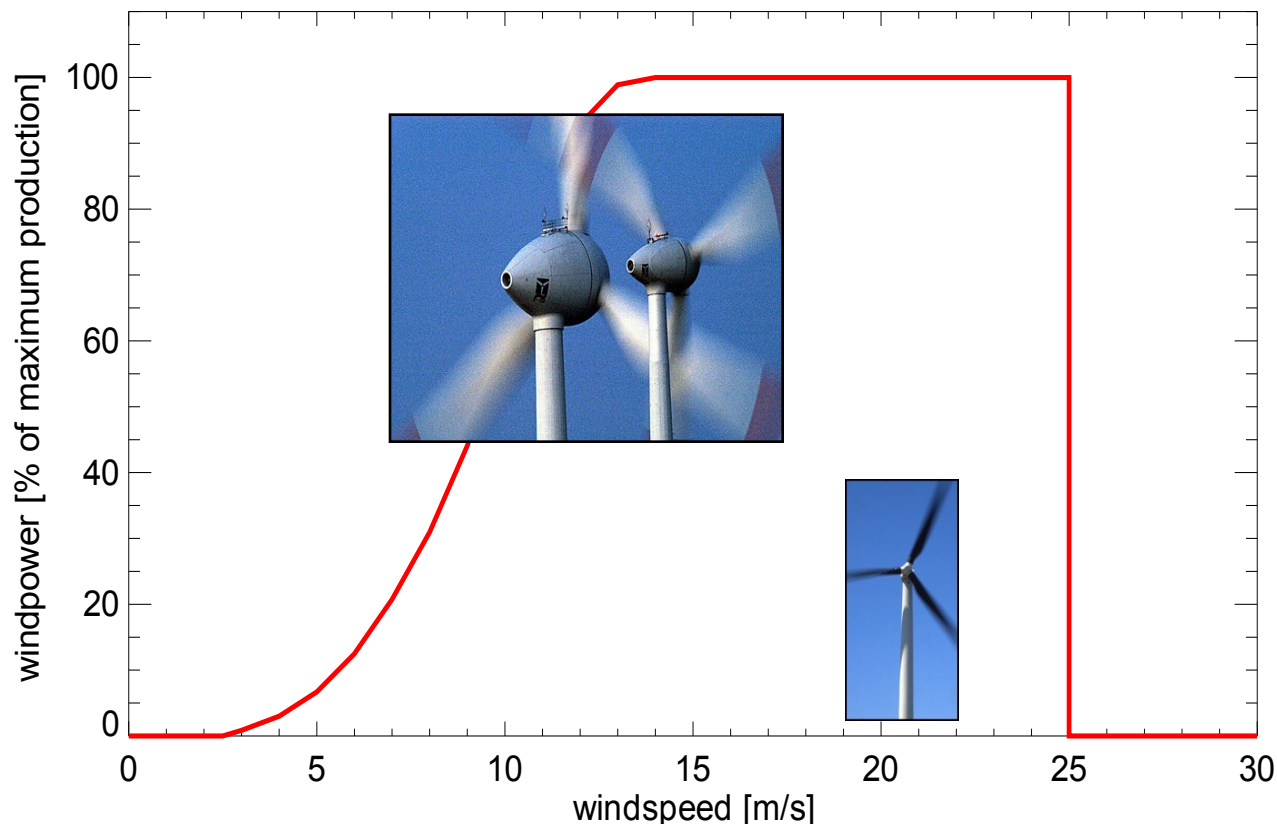
# Wind farm example

turbines must be stopped in high winds

Must continue to supply electricity even if not generating

So may need to buy extra energy

Cheaper to buy in advance



Decision to make:

Should I buy extra energy to protect against  $ff > 25$  m/s, yes or no?

# Financial costs to wind farm manager



	event occurs i.e. $ff \geq 25$ m/s	event does NOT occur i.e. $ff < 25$ m/s
Protection: YES	200 €	200 €
Protection: NO	1000 €	0 €

# Value of deterministic forecasts

- If no forecast just use climatological information
  - Always protect (if often occurs)
  - Never protect (if rarely occurs)
- Using forecast: protect when event is forecast
  - Can save money compared to using climate
- Value
$$V = \frac{\text{saving from using forecast}}{\text{saving from perfect forecast}}$$
- $V = 0$  forecast is no better than climate
- $V = 1$  forecast is perfect (no misses, no false alarms)



# Value of deterministic forecast

Protect when event is forecast

Value of using forecast = saving compared to not using forecast



	event occurs i.e. $ff \geq 25$ m/s	event does NOT occur i.e. $ff < 25$ m/s
<b>Forecast: YES</b> <b>Protect: YES</b>	<b>Hit</b> <b>Cost = 200 €</b>	<b>False alarm</b> <b>Cost = 200 €</b>
<b>Forecast: NO</b> <b>Protect: NO</b>	<b>Miss</b> <b>Loss = 1000 €</b>	<b>Correct reject</b> <b>0 €</b>

# Value, forecast quality and the user

Value can be written in terms of hit rate (H), false alarm rate (F) and the “cost-loss ratio” of the user (C/L):

$$V = (1 - F) - \left( \frac{1 - C/L}{C/L} \right) \left( \frac{\bar{o}}{1 - \bar{o}} \right) (1 - F) \text{ if } C/L < \bar{o}$$

$$V = H - \left( \frac{C/L}{1 - C/L} \right) \left( \frac{1 - \bar{o}}{\bar{o}} \right) F \text{ if } C/L > \bar{o}$$

- Value depends on forecast quality: H and F
- but value also depends on the user (C/L)
- and on the weather event ( $\bar{o}$ )

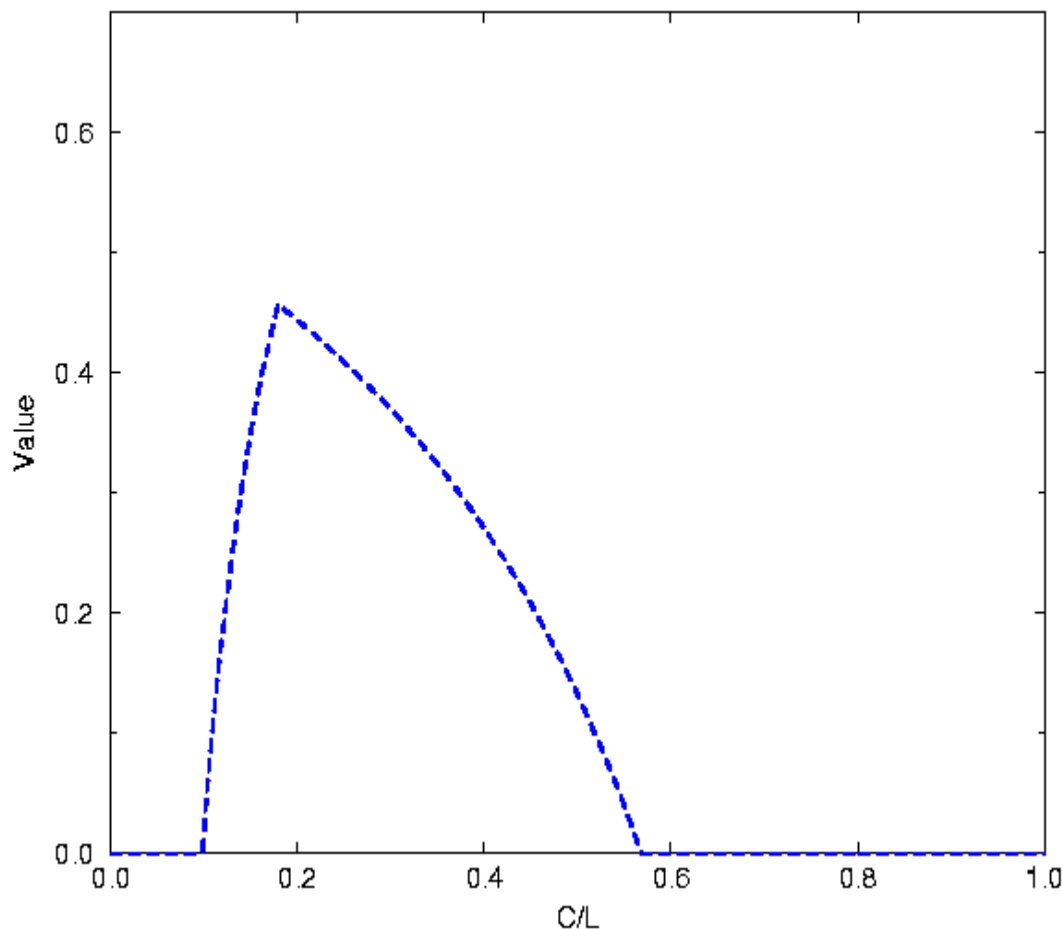
# Cost-loss wind farm manager

Cost-loss ratio =  $200/1000$   
= 0.2



	event occurs i.e. $ff \geq 25$ m/s	event does NOT occur i.e. $ff < 25$ m/s
Protection: YES	200 €	200 €
Protection: NO	1000 €	0 €

# Value for different users



**High loss from missed event (hit rate important)**

**High cost to protect (false alarm rate important)**

# Value of probability forecasts

- Using a deterministic forecast is straightforward: take action if bad weather is forecast, otherwise do nothing
- What if the forecast is given as a probability of bad weather?
- To make a decision the probability forecast must be converted to a yes/no action
- Choose a probability threshold  $p_t$ 
  - if  $p > p_t$  then take action
  - if  $p < p_t$  then do nothing
- Which probability threshold to choose?



# Financial costs to wind farm manager

Probability is 30%

**30**



**70**



	event occurs i.e. $ff \geq 25$ m/s	event does NOT occur i.e. $ff < 25$ m/s
Protection: YES	200 €	200 €
Protection: NO	1000 € <b>30,000 €</b>	0 €

# Financial costs to wind farm manager

Probability is 30%

**30**



**70**



	event occurs i.e. $ff \geq 25$ m/s	event does NOT occur i.e. $ff < 25$ m/s
<b>Protection: YES</b>	200 € <b>6,000 €</b>	200 € <b>14,000 €</b>
<b>Protection: NO</b>	1000 €	0 €

# Financial costs to wind farm manager

Probability is 30%

**30**



**70**



Better to protect (costs €20000) than not protect (costs €30000)

	event occurs i.e. ff $\geq$ 25 m/s	event does NOT occur i.e. ff < 25 m/s
Protection: YES	200 € <b>6,000 €</b>	200 € <b>14,000 €</b>
Protection: NO	1000 € <b>30,000 €</b>	0 €

# Financial costs to wind farm manager

Probability is 10%

**10**



**90**



	event occurs i.e. $ff \geq 25$ m/s	event does NOT occur i.e. $ff < 25$ m/s
Protection: YES	200 €	200 €
Protection: NO	1000 € <b>10,000 €</b>	0 €

# Financial costs to wind farm manager

Probability is 10%

**10**



**90**



	event occurs i.e. $ff \geq 25$ m/s	event does NOT occur i.e. $ff < 25$ m/s
Protection: YES	200 € <b>2,000 €</b>	200 € <b>18,000 €</b>
Protection: NO	1000 €	0 €

# Financial costs to wind farm manager

Probability is 10%

10



90



Better to NOT protect (costs €10000) than protect (costs €20000)

	event occurs i.e. ff $\geq$ 25 m/s	event does NOT occur i.e. ff < 25 m/s
Protection: YES	200 € <b>2,000 €</b>	200 € <b>18,000 €</b>
Protection: NO	1000 € <b>10,000 €</b>	0 €



# Financial costs to wind farm manager

Probability is 20%

20



80



	event occurs i.e. $ff \geq 25$ m/s	event does NOT occur i.e. $ff < 25$ m/s
Protection: YES	200 €	200 €
Protection: NO	1000 € <b>20,000 €</b>	0 €

# Financial costs to wind farm manager

Probability is 20%

20



80



	event occurs i.e. $ff \geq 25$ m/s	event does NOT occur i.e. $ff < 25$ m/s
Protection: YES	200 € <b>4,000 €</b>	200 € <b>16,000 €</b>
Protection: NO	1000 €	0 €

# Financial costs to wind farm manager

Probability is 20%

20



80



Same to  
protect as not  
protect  
(€20000)

	event occurs i.e. $ff \geq 25$ m/s	event does NOT occur i.e. $ff < 25$ m/s
Protection: YES	200 € <b>2,000 €</b>	200 € <b>18,000 €</b>
Protection: NO	1000 € <b>20,000 €</b>	0 €

# Probability threshold depends on user

- If the cost of protection is expensive wait until event is more certain (higher probability)
  - False alarms are more important
- If the loss is greater then protect even at low probability
  - Missed events are more important
- The threshold depends on the user:  $p_t = C/L$

# Value of probability and deterministic forecasts compared

