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JOINT ASSIMILATION OF SURFACE SOIL MOISTURE AND LAI OBSERVATIONS INTO A LAND SURFACE MODEL

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ABSTRACT

Land Surface Models (LSM) offer a description of land surface processes and set the lower boundary conditions for meteorological models. In particular the accurate description of those surface variables which display a slow response in time, like root zone soil moisture or vegetation biomass, is of great importance. Errors in their estimation yield significant inaccuracies in the estimation of heat and water fluxes in Numerical Weather Prediction (NWP) models. In the present study, the ISBA-A-gs LSM is used decoupled from the atmosphere. In this configuration, the model is able to simulate the vegetation growth, and consequently LAI. A simplified 1D-VAR assimilation method is applied to observed surface soil moisture and LAI observations of the SMOSREX site near Toulouse, in south-western France, from 2001 to 2004. This period includes severe droughts in 2003 and 2004. The data are jointly assimilated into ISBA-A-gs in order to analyse the root zone soil moisture and the vegetation biomass. It is shown that the 1D-VAR improves the model results. The efficiency score of the model (Nash criterion) is increased from 0.79 to 0.86 for root-zone soil moisture and from 0.17 to 0.23 for vegetation biomass.

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1. Introduction

The Land Surface Models (LSM) used in meteorology have been developed in order to simulate continuous land surface processes, such as plant transpiration, soil evaporation and the evolution of soil moisture and surface temperature at regional and global scales. A number of CO₂-responsive LSMS, like the ISBA-A-gs model of Météo-France (Calvet et al. 1998, Calvet et al. 2004, Gibelin et al. 2006), are able to simulate photosynthesis and plant growth. In particular, the vegetation biomass and the leaf area index (LAI) evolve dynamically in response to climate conditions. These models allow the assimilation of soil moisture and LAI observations.

In the present study, two variables with significant impact on the heat and water fluxes are considered: root zone soil moisture ($w_2$) and above-ground vegetation biomass ($Bio$). Soil moisture regulates the partitioning between latent and sensible heat fluxes, which has a significant influence on the amount of cloud formation, air temperature, and humidity, among others (Segal et al., 1995, Shaw et al., 1997, Seuffert et al., 2002). At the same time, vegetation biomass plays a very important role in the exchange of water vapor and CO₂ between the vegetation canopy and the atmosphere. All aforementioned variables are key input variables into Global Circulation Models (GCM) (Chase et al, 1996, Bounoua et al, 2000). However, as a consequence of different model complexities and surface parameterizations, there is a range of uncertainty in the simulation of these variables by LSMS (Henderson-Sellers et al., 1993, Henderson-Sellers et al., 1995, International GEWEX Project Office, 1995). Data assimilation systems allow to integrate the rich information provided by remotely sensed surface variables into LSMS, in order to improve the model predictions (eg. Entekhabi et al., 1994; Houser et al., 1998, Lakshmi and Susskind, 2001). To achieve this, LSMSs are coupled with Radiative Transfer Models (RTM) to relate remotely sensed quantities to land-surface variables. For example, the L-Band Microwave Emission of the Biosphere (L-
MEB) model (Wigneron et al., 2005) relates L-band brightness temperatures to surface soil moisture ($w_g$) variations. $w_g$ products are already available at global scale through instruments such as the Advanced Microwave Scanning Radiometer for EOS (AMSR-E) sensor (Njoku et al., 2003) or those that will be provided in L-band by the future Soil Moisture and Ocean Satellite (SMOS) mission of the European Space Agency (ESA) (Kerr et al., 2001). These observations can be used to analyze $w_2$ (Entekhabi et al., 1994, Reichle et al., 2001).

Additionally, a large quantity of satellite-derived LAI products is available, such as those from the MODerate-Resolution Imaging Spectroradiometer (MODIS) at 1 km spatial resolution (Tian et al. 2002a, Tian et al. 2002b, Tan et al. 2005) or the POLarization and Directionality of Earth Reflectances (POLDER) sensor (Bicheron and Leroy, 1999, Roujean and Lacaze, 2002). LAI observations have been shown to be useful for the analysis of the vegetation biomass (Cayrol et al., 2000).

This paper is a continuation of the study of Muñoz Sabater et al. (2007) (henceforth called MU07). In MU07, $w_g$ observations were assimilated using four different assimilation approaches. The simplified 1D-VAR method demonstrated to be the most suitable for an implementation in an operational configuration. Although the results for the $w_2$ analyses were generally satisfactory, the LSM was forced with a prescribed LAI obtained from in-situ measurements. In the present paper, a step forward is made, and the LAI is simulated by the surface scheme using the parameterization for the plant photosynthesis and growth model of ISBA-A-gs (Gibelin et al. 2006). The main objective is the analysis of $w_2$ and vegetation biomass through the joint assimilation of LAI and $w_g$ observations. The experimental data originates from the SMOSREX experimental site (De Rosnay et al., 2006). The period under investigation extends over four years from 2001 to 2004, during which very contrasting meteorological conditions were observed.
In section 2, the experimental site, the data set, the ISBA-A-gs LSM, and the data assimilation scheme are described. Also, the choice of the assimilation parameters is discussed through sensitivity and Monte-Carlo based methods. In section 3, the results are presented for the 4-year period and discussed for two configurations of the assimilation (fixed and time-variant wilting point) and for different accuracies of the atmospheric forcing. Finally, section 4 discusses and summarizes the main conclusions.
2. Methodology

2.1. Experimental site and data set

The SMOSREX site is situated within the ONERA (French National Aerospace Research Establishment) centre of Fauga-Mauzac, located 40 km south-west of Toulouse (43°23’N, 1°17’E, 188 m altitude). SMOSREX (De Rosnay et al., 2006) is a field scale experiment, operative since 2001. In this study, the southern part of the site, covered by vegetation (natural fallow) is studied. An estimation of $w_g$ is obtained through the measurements provided by four probes (ThetaProbe, Delta T Devices) vertically installed at the surface at different locations within the experimental field site. They provide continuous observations over the first 6 cm of the soil surface layer. Daily mean $w_g'$ values are obtained by averaging the measurements of the four probes and their standard deviation permits to estimate the uncertainty of the observations. The root-zone soil moisture is obtained by calculating an average bulk soil water content from the surface probes and additional soil moisture sensors horizontally installed at depths of 10, 20, 30, 40, 50, 60, 70, 80 and 90 cm. From the individual measurements, a mean and a standard deviation are computed on a daily basis, and the daily standard deviation averaged over the year 2001 is assumed to represent the observation error: $\sigma(w_g^{\text{OBS}}) = 0.03 \ m^3 m^{-3}$ and $\sigma(w_2^{\text{OBS}}) = 0.02 \ m^3 m^{-3}$. Due to a lack of sufficient spatial sampling at the field site, the spatial averaging is replaced by a temporal one (ergodicity principle). These uncertainties are attributed to the moisture observations in subsequent years (2002-2004). The atmospheric forcing (precipitation, atmospheric pressure, wind speed and direction, air humidity, air temperature, and incident solar and infrared radiation) is obtained from a meteorological station at the field site performing continuous measurements, obtained every minute and averaged at 30 minute intervals.
Manual measurements of the vegetation characteristics (LAI, above-ground biomass and necromass, height of the canopy) were generally carried out every two weeks. The LAI and above-ground biomass/necromass measurements were performed by harvesting random sample areas of 25 x 25 cm$^2$ (4 replicates), and using planimetric and gravimetric methods. For each sample, green biomass and dead plant material were measured separately (De Rosnay et al. 2006). Fig. 1 shows the in-situ observations of the LAI, the surface and root-zone soil moisture and the monthly accumulated precipitation for the four years (2001-2004). It is shown that 2003 was a particularly dry year, with an annual cumulative precipitation of less than 600 mm. Unlike the other years, 2003 shows an atypical double cycle of LAI, with a first peak in spring and a second one at the beginning of the winter season. Precipitation is quite irregularly distributed during 2004, with a wet spring and a very dry summer. This causes a rapid growth of the vegetation and a marked senescence during the dry period, with moisture observations reaching values below the wilting point ($w_{\text{wil}}$) throughout the summer and part of autumn.

In Table 1 a list of the most relevant characteristics of the soil at the SMOSREX site for ISBA-A-gs is provided. The soil is a loam characterized by its texture and density which were determined in the laboratory. The $w_{\text{wil}}$ and the field capacity parameters were derived from the clay content observations, by using the relationships given by Noilhan and Mahfouf (1996).

2.2. Land surface model: ISBA-A-gs

The land surface model used in this study is the ISBA-A-gs model (Calvet et al., 1998, Calvet et al., 2004, Gibelin et al., 2006). It is an improved version of the Interaction between the Soil, Biosphere and Atmosphere (ISBA) model, first developed by Noilhan and Planton
(1989) and further improved by Noilhan and Mahfouf (1996), to describe the land surface processes in weather and climate models.

The version of the ISBA model used in this study is based on the equations of the force-restore method (Deardorff, 1977, 1978), and the soil is represented by a single layer. Together with the surface fluxes ($LE, H, G$), five surface state variables are described: surface temperature ($T_s$), mean surface temperature ($T_2$), surface volumetric soil moisture ($w_g$), volumetric root-zone soil moisture ($w_2$) and canopy interception reservoir ($W_s$). The new version (ISBA-A-gs) accounts for the effect of the atmospheric CO$_2$ concentration on the stomatal aperture. The net assimilation of CO$_2$ is used to predict the vegetation biomass and the LAI. The model simulates two above-ground biomass reservoirs: the leaf biomass and the above-ground structural biomass. For herbaceous vegetation, the sum of these two reservoirs is the total above-ground biomass ($Bio$). The reservoirs are fed by the net assimilated carbon, and decreased by turnover and respiration terms. Phenology is modelled implicitly: LAI follows the variations of the leaf biomass, multiplied by a constant Specific Leaf Area (SLA). The SLA is related to the leaf nitrogen concentration ($N_l$) by using two plasticity parameters $e$ and $f$ (Gibelin et al. 2006):

$$SLA = eN_l + f.$$  \[1\]

The values of $e$ and $f$ used in this study are presented in Table 1.

Two strategies are represented for the response of the plant to water stress, drought-avoiding and drought-tolerant (Calvet 2000, Calvet et al. 2004) depending on the evolution of water use efficiency (WUE) under moderate stress: WUE increases in the early stages of soil water stress in the case of the drought-avoiding response, whereas WUE decreases or remains stable in the case of the drought-tolerant response.
The vegetation parameters of ISBA-A-gs are presented in Table 1. They are derived from the simulation of Calvet (2000) for the MUREX test site (Calvet et al., 1999). Following their work, the drought-tolerant strategy is used in this paper.

In this study, the model performance is evaluated by using the root mean square error (RMSE), the mean bias, and the efficiency score (or Nash criterion; Nash and Sutcliffe 1970) defined as:

$$E = 1 - \frac{\sum_i (x_{i}^{obs} - x_{i}^{simulated})^2}{\sum_i (x_{i}^{obs} - \bar{x}_{obs})^2} \quad [2]$$

where $x$ represents a state variable and $x^{obs}$ the corresponding observed variable. A value of $E$ equal to 1 corresponds to perfect simulations and values of $E$ close to 0 correspond to simulations equal to the constant average of the observations. Negative values of $E$ show that the model performance is less accurate than simply applying the arithmetic mean of the observations.

2.3. Assimilation method: Simplified 1D-VAR

The choice of the assimilation scheme is based on the results obtained in MU07. Of the four assimilation methods compared in that study, the Ensemble Kalman Filter (EnKF) and a simplified 1D-VAR showed the best performance. However, the variational scheme presented an important advantage, as the computational cost was significantly lower, making it more suitable for operational purposes. Therefore, a simplified 1D-VAR was employed in this study.

2.3.1. Formalism

Variational methods use an assimilation window of predefined length, usually containing several observations. The initial value of the model state vector (the variables to be analysed) is perturbed and the optimal combination of model states is then found by
minimizing a cost function \( J \) (at observation times within the assimilation window). In our case, the state vector is composed of two state variables \( (w_2) \) and vegetation above-ground biomass \((Bio)\). The cost functions for the two state variables are:

\[
J(Bio) = \frac{1}{2} \left( Bio - Bio^b \right)^T B^{-1}_{Bio} \left( Bio - Bio^b \right) + \frac{1}{2} \left( LAI^{OBS} - H(Bio) \right)^T R^{-1}_{LAI} \left( LAI^{OBS} - H(Bio) \right) = J^b_{Bio} + J^{OBS}_{LAI}
\]

[3]

\[
J(w_g) = \frac{1}{2} \left( w_g - w_g^b \right)^T B^{-1}_{w2} \left( w_g - w_g^b \right) + \frac{1}{2} \left( w_g^{OBS} - H(w_g) \right)^T R^{-1}_{wg} \left( w_g^{OBS} - H(w_g) \right) = J^b_{w2} + J^{OBS}_{wg}
\]

[4]

where the superscripts \( ^b \) and \( ^{OBS} \) denote the initially estimated values of the state variables within the assimilation window (background) and the observed variables, respectively; and \( H \) is the non-linear observation operator which transfers the state variables into observation space. The “best” analyses are the result of minimizing the distance between the state variables and the first-guess weighted by the background error covariance matrix \( B \) \((J^b_{Bio} \text{ and } J^b_{w2} \text{ terms})\) and the distance between the observations and the model predictions \((J^{OBS}_{LAI} \text{ and } J^{OBS}_{wg} \text{ terms})\) within the assimilation window, weighted by the observation error covariance matrix \( R \). In the case of a linear observation operator and a normal distribution of the errors, the analysed state variables of the cost functions [3] and [4] are expressed by:

\[
Bio = Bio^b + K_{Bio} \left( LAI^{OBS} - H_{Bio} \left( Bio^b \right) \right); \quad K_{Bio} = B_{Bio} H_{Bio}^T [H_{Bio} B_{Bio} H_{Bio}^T + R_{LAI}]^{-1}, \quad [5]
\]

and

\[
w_2 = w_2^b + K_{w2} \left( w_g^{OBS} - H_{w2} \left( w_2^b \right) \right); \quad K_{w2} = B_{w2} H_{w2}^T [H_{w2} B_{w2} H_{w2}^T + R_{wg}]^{-1}, \quad [6]
\]

respectively. In the non-linear case, the minimum of the cost functions [3] and [4] is evaluated by deriving adjoint or tangent linear models. However, this is an often difficult and time consuming task (Reichle et al., 2002). The simplified 1D-VAR (Balsamo et al., 2004) circumvents this problem by using a numerical linear approximation of the observation
operator. This approximation consists of a perturbation of the initial value of the state variables \( w_1 = w_1^b + \delta w_1 \) for the root zone soil moisture and \( Bio = Bio^b + \delta Bio \) for the vegetation biomass) and studying the impact of this perturbation on the predicted variables at each observation time step \( i \) within the assimilation window (with \( n \) observations). In this way, linearised observation operators of the type: 

\[
H = \begin{bmatrix} \frac{\delta y^i}{\delta x_0}, \ldots, \frac{\delta y^n}{\delta x_0} \end{bmatrix}
\]

are obtained, where \( \delta x_0 \) represents the perturbation of the initial state variable and \( \delta y^i \) the change in the simulated variable at time step \( i \) (for \( i=\{1, n\} \), due to \( \delta x_0 \). This operator \( H \) is then substituted in [5] and [6], and also replaces the non-linear observation operator \( H \).

### 2.3.2. Setting of the main 1D-VAR parameters

The most difficult task in the implementation of an assimilation scheme is the description of the error matrices. It is a key aspect, because the correction of the system state depends on the background and observation error prescription (see Eqs. [3] to [6]). The size of the initial perturbation and the length of the assimilation window is also discussed in this section.

(i) **Assimilation window length**

The choice of the assimilation window length for a variational assimilation scheme is particularly important when the scheme is applied to large regions. In this study, a 10-day assimilation window, which is close to the sampling time of many LAI products (e.g. a 8-day MODIS product is available), was chosen because shorter assimilation windows would regularly exclude LAI observations altogether.

(ii) **Observational errors**

In this study, observed time series of surface soil moisture \( w_g \) and LAI were used for the assimilation into the model. For \( w_g \), the same method as in MU07 was applied, i.e. the error derived from the dispersion of in-situ observations was doubled and therefore set to \( R_{w_g} \).
= 0.06 m$^3$m$^{-3}$. For LAI, an observational error is difficult to obtain from the experimental procedure followed in SMOSREX. Moreover, the LAI observations exhibited quite different cycles (in terms of shape and maxima) in 2001 and 2002. It was decided to use an empirical value of $R_{LAI} = 1$ m$^2$m$^{-2}$, which is expected to account for all sources of uncertainties (observational system and representativeness error). Both values were assumed to be constant throughout the whole period 2001-2004. A sensitivity study was performed in order to assess the value of a variable LAI observation error. However, no or little impact on the assimilation results were found. For the sake of simplicity, a constant value was used.

(iii) Background errors

For the description of the error in the estimation of $w_2$, an ensemble of simulations was created between two consecutive observations by using different initial states of $w_2$ and by perturbing the atmospheric forcing. For each assimilation window the dispersion of the residuals (difference between an observation and the model estimation) was assessed. During the calibration year (2001) this quantity was shown to have a constant value of 0.02 m$^3$m$^{-3}$. The same approach was used to estimate a model covariance error for the vegetation biomass over the 10-days of the individual assimilation windows. It was observed that the evolution of the standard deviation of the residuals does not vary much over the year 2001. However, a slight seasonal effect is observed (not shown). Departure from the mean value is about 0.01 kg m$^{-2}$ on average. Therefore, the background error for the vegetation biomass was assumed to be constant and was set equal to the average of the standard deviation of the residuals in 2001 (0.05 kg m$^{-2}$).

(iv) Linear hypothesis

A further important parameter in the implementation of this simplified variational assimilation scheme is the choice of the perturbation size of the state variables, because it determines the quality of the linear approximation through the observation operator $H$. To
evaluate the “optimal” size of this perturbation, the following test was conducted: an ensemble of linear operators $H$ was obtained by finite differences (by a random Gaussian perturbation of the initial value of $w_2$ and/or the vegetation biomass) for a 10-day period (four components for $H_{w_2}$ and one for $H_{BIO}$) and their standard deviation ($\sigma$) was calculated. Several values of the initial perturbation of the state variables were tested. The smallest perturbations of $w_2$ (between 0.005 and 0.015 m$^3$m$^{-3}$) produced a strong value of $\sigma$ to the four linearized components of $H_{w_2}$ during the calibration year (not shown). This is due to the numerical noise produced by infinitesimal perturbations in the vicinity of the initial value. The most suitable perturbation should result in a low sensitivity of $H_{w_2}$. $H_{w_2}$ was found to be less sensitive for perturbations close to 0.05 m$^3$m$^{-3}$ and this value was used in the assimilation algorithm.

Fig. 2 illustrates how the optimal perturbation of $Bio$ was determined. The $\sigma$ of the sole component of $H_{BIO}$ in a 10-day assimilation window is presented for contrasting values of perturbations of $Bio$. In Fig. 2, the optimal perturbation, producing the lowest $\sigma$ values, is located between 0.07 and 0.10 kg m$^{-2}$. It was finally set to 0.07 kg m$^{-2}$. Fig. 2 shows that perturbation values lower than 0.07 kg m$^{-2}$ and between 0.10 and 0.13 kg m$^{-2}$ produced larger $\sigma$ values. Perturbations higher than 0.13 kg m$^{-2}$ were found also to produce larger uncertainties in $H_{BIO}$ (not shown).

(v) Implementation

The implementation of the simplified assimilation scheme can be undertaken in different ways. In this study, $w_2$ and vegetation biomass were perturbed at the beginning of each assimilation window, in order to determine the linearized observation operator. This configuration necessitated 3 runs for each assimilation window (one for each perturbed variable and one for the control run).

2.3.3. Dynamical correction of the wilting point
As mentioned before, $w_{\text{wilt}}$ is estimated by the LSM and then treated as a constant parameter (found to be 0.17 m$^3$m$^{-3}$ for the SMOSREX site). However, the assimilation scheme is allowed to initialise the model with $w_2$ states below $w_{\text{wilt}}$, following the assimilation of $w_g$. This occurred during the drought periods of the years 2003 and 2004 (MU07). In this case, ISBA-A-gs did not allow any further evapotranspiration and soil water extraction through the roots, even after significant rainfall events. This led to a strong vegetation mortality rate. However, the SMOSREX field observations performed during the summer 2003 show that the vegetation growth in response to rainfall may be rapid (Fig. 1). The performance of the vegetation analyses was also affected by this constraint. The following solution is proposed: for each assimilation step with an analysed value of $w_2$ below the fixed $w_{\text{wilt}}$, the model $w_{\text{wilt}}$ is re-set by substituting its value with the analysed value of $w_2$. This simple modification to the model allows plant growth in response to rainfall to occur after a drought.
3. Results

3.1. \( w_2 \) and biomass analyses (2001-2004)

In Fig. 3, the 1D-VAR analysis of \( w_2 \) and the vegetation biomass are presented for the years 2001 to 2004 (Fig. 3a and 3b, respectively) with a non-stationary \( w_{\text{wilt}} \) (see section 2.3.3). The simulation performed with ISBA-A-gs and without the assimilation of \( w_g \) or LAI observations (i.e. the control simulation) is also presented in Fig. 3. The predicted LAI (control and analysis) is also shown on Fig. 3c. The assimilated observations are the surface soil moisture (one observation every three days) and the LAI (one observation every 10 days). Analyses, observations and the control model reference are superposed for comparison purposes. It is shown that \( w_2 \) is generally well reproduced during the whole period from 2001 to 2004, with a score \( E \) equal to 0.86 after the assimilation in contrast to 0.79 for the control simulation (Table 2). The added value of the assimilation is particularly noticeable during the six months following June 2003, for which the model without assimilation is not able to descend below the prescribed \( w_{\text{wilt}} \) and consequently overestimates the moisture during the rest of that year.

On Fig. 3c, the impact of the joint \( w_2 \) and vegetation biomass analysis is shown for the LAI predictions. The predicted values of LAI are quite close to the observations, improving the performance from \( E = 0.17 \) for the control run to \( E = 0.72 \), and RMSE from 0.80 m\(^2\) m\(^{-2}\) to 0.47 m\(^2\) m\(^{-2}\) after the assimilation (Table 2). The main disagreements are found during the senescence periods of the vegetation when the model clearly overestimates the LAI (except for 2003, where an anomalous double cycle of LAI was observed). Since the vegetation biomass observations are sparse and very scattered for 2001 and 2002, it is not clear whether the assimilation improves the control model simulation for these years. It is observed that during the second cycle of vegetation in 2003, the biomass is slightly overestimated after the
analysis, which is in agreement with the higher LAI observations assimilated. The RMSE and the score for the years 2003 and 2004 were not improved, which may be explained by the limited number of available observations of vegetation biomass. However, for the whole study period, the analysis of the vegetation biomass improved the score from 0.17 to 0.23.

In Fig. 4, the impact of setting a non-stationary $w_{wilt}$ is only shown for 2003 and 2004, because $w_{wilt}$ was only modified during these two years. During the periods with analysed $w_2$ below $w_{wilt}$ an increased vegetation mortality rate is observed. The need for re-setting $w_{wilt}$ is particularly apparent between July and October 2004, when the vegetation biomass analyses were close to zero. During this period, each time $w_2$ analyses were below $w_{wilt}$ ISBA-A-gs stopped plant transpiration and photosynthesis, which resulted in a high vegetation mortality rate. Consequently, the performance of the vegetation biomass analyses for 2003 and 2004 was low (Table 2) compared to the case of a modified $w_{wilt}$. This effect is less evident in 2003, since the drying period is shorter than in 2004. For the complete four years, the score of the vegetation biomass decreases (compared with a non-stationary $w_{wilt}$) from 0.23 to 0.12. The lower vegetation biomass during the dry periods also had an impact on the soil water reservoir, which produced higher moisture levels. The score for $w_2$ decreased from 0.86 to 0.82 (Table 2).
3.2. Zero precipitation

The simulations at SMOSREX are forced with good quality measurements of meteorological variables, representative for the study area. However, at larger scales the information about meteorological variables is less accurate. In order to test the robustness of the 1D-VAR, even when forcing data are subjected to large errors, the precipitation was set to 0. Precipitation is a key variable within atmospheric forcing data sets and is particularly important for the water reservoir evolution. For this experiment, the assimilation scheme was run again for the whole 4-year period under investigation. Fig. 5 shows the same plots as Fig. 3, but with the new, degraded forcing data. Although the new analyses produced a drier soil, the general shape of the curve of the analyzed $w_2$ was maintained. It is now much smoother, since the information about the precipitation events is lacking. It is important to remark that the assimilation scheme permits the increase of the root-zone soil moisture before the start of the growing period. Otherwise, given the absence of precipitation, a growing season would not be simulated. The LSM, with precipitation set to 0, tends to decrease the root-zone soil moisture between two observations. However, the 1D-VAR generates positive increments which correct the water deficiency in order to match the $w_g$ observations. The advantage over the control simulation is considerable. Under the precipitation constriction, the control simulation would rapidly fall to 0.17 $m^3m^{-3}$ (constant $w_{wilt}$), and since the model would not receive precipitation, the moisture reservoir would remain at this lower boundary. The benefits of the data assimilation are also clear for the vegetation: although the biomass analyses are obtained with less accuracy (in particular, lower peak values are obtained), especially during the wet years 2001 and 2002, the start of the growing season is still well predicted. The need for a non-stationary $w_{wilt}$ is highlighted again when Fig. 5 is compared to
Fig. 6. In the latter, the vegetation biomass reaches a value of 0 in those periods where $w_2$ is below $w_{\text{wilt}}$, and which now have a longer duration, due to the lack of precipitation. The score for the vegetation biomass becomes negative and for the LAI is reduced from 0.48 (non-stationary $w_{\text{wilt}}$) to 0.14 (stationary $w_{\text{wilt}}$). In Fig. 6, the $w_2$ analyses for the summer period are overestimated in the years 2003 and 2004, because of a very low level of vegetation, while better retrievals are obtained by re-setting $w_{\text{wilt}}$. The evapotranspiration is strongly reduced without precipitation, since the simulation of the vegetation biomass underestimates the real conditions (Table 3).

4. Summary and Discussion

The present study is a continuation of the work initiated in MU07. There, a simplified 1D-VAR assimilation scheme was compared with other assimilation schemes, and it was shown that it offered the best performance in view of a future implementation in a regional experiment. However, the LAI was forced and the vegetation biomass was not corrected for, as only $w_g$ observations were assimilated. Nevertheless, vegetation biomass is also an important surface variable, vital to estimate the carbon and water vapour fluxes, and its analysis is also essential. In this study, field observations of $w_g$ and LAI were assimilated at the same time into the ISBA-A-gs LSM. When comparing Fig. 3a of this study with Fig. 4 of MU07, two main differences are observed with regard to the analyses of $w_2$: i) a degradation at the end of 2001 is observed, ii) the correction over the dry period of 2004 is less accurate. This is a consequence of analysing the vegetation biomass in addition to soil moisture. From October 2001 to February 2002 no LAI observations were available, which resulted in interpolated values of less than 0.5 $m^2m^{-2}$ during this period. In this study, these estimates were assimilated and the LAI retrievals after assimilation were close to these observations. This produced lower transpiration and water extraction rates, hence a slower drying of the
water reservoir and as a consequence an overestimation of the $w_2$ analyses. Before the
implementation of the joint assimilation of $w_g$ and LAI observations into the fully coupled
model, a number of tests were performed. In particular, the assimilation of $w_g$ alone and of
LAI alone was attempted (MU07).

The assimilation of $w_g$ alone (LAI was not controlled by any observation) did not
improve the simulated LAI. It tended to speed up the growing period and to increase the
maximum value of LAI reached each year. This factor had detrimental effects on the analysed
$w_2$ during the spring of 2002 (values lower than the control simulation, and much lower than
the observations were obtained).

The assimilation of LAI alone ($w_g$ was not constrained by any observation) generally
improved $w_2$ only marginally. However, it tended to increase the error on the simulated $w_2$
during the drought periods (e.g. October 2001, July-August 2003, July 2004, October 2004),
while it permitted to obtain analysed vegetation biomass values very similar to those shown in
Figs. 3 and 4.

No flux validation data was available and the positive or negative impact of the
assimilation on the fluxes could not be quantified. On a daily basis, the simulated
evapotranspiration was not fundamentally changed by the assimilation. However, the new
annual cycles of the flux was more consistent with the available observations of vegetation
biomass and LAI, which showed that the LAI produced by the control simulation was
underestimated during the start of the growing season and overestimated during the
senescence phase.

The $w_{wilt}$ limitation imposed by the single soil layer of the model used in this study
tends to trigger a high vegetation mortality rate during marked droughts, and to underestimate
the impact (on vegetation growth and on the water and carbon fluxes) of significant rainfall
events after the droughts. A simple solution consists in re-setting $w_{wilt}$ dynamically during
anomalously dry periods. The introduction of a non-stationary $w_{wilt}$ was shown to improve the moisture and vegetation predictions as compared to the control simulation with a stationary $w_{wilt}$. This led to an improvement of the score of $w_2$ from 0.79 to 0.86. Furthermore, the score was slightly improved from 0.17 to 0.23 for the vegetation biomass analysis. The final value of 0.23 is rather low, partly because the high level of scatter in the observations found for 2001 and 2002 prevents the score of reaching higher values.

Solutions potentially suitable to overcome the $w_{wilt}$ problem, include the attribution of more weight to the LAI observations by reducing the observational error when the initial $w_2$ is found below the prescribed $w_{wilt}$. However, this poses a problem when LAI observations are not reliable. The simple solution of prescribing a non-stationary $w_{wilt}$ value, low enough for drought periods, was assessed (not shown). Indeed, a lower $w_{wilt}$ (e.g. 0.10 m$^3$m$^{-3}$ instead of 0.17 m$^3$m$^{-3}$) permitted to improve the control simulation of $w_2$ during the summer/autumn of dry years (2003-2004). However, this change triggered a significant underestimation of $w_2$ during the summer/autumn of the normal/wet years (2001-2002). These results were to be expected, as prescribing a lower value of the wilting point is tantamount to increasing the total extractable soil moisture of the soil. The vegetation simulated by ISBA-A-gs over this site tends to exploit the whole soil moisture reservoir prescribed in the model, even during a wet year like 2002. It was eventually decided that it was preferable to use the 0.17 m$^3$m$^{-3}$ value, which is a typical wilting point value for a loam and which allows a good model performance during normal years. The difference between the model and the observations in 2003 and 2004 can be explained by the rather extreme droughts encountered during these two years. A number of biological and physical explanations are proposed:

In the model, the wilting point depends on the soil texture. In reality, this parameter may also depend on the plant ability to extract water from a particular soil. The SMOSREX fallow is a multi-specific canopy. During drought events, the plant species most capable of extracting
water in dry conditions have an advantage in their competition with the other species. This effect could change the behaviour of the soil-plant system from one year to another. To some extent, this effect could also happen at large spatial scales for natural ecosystems and agricultural areas (e.g. farmer may choose to use cultivars adapted to dry conditions during dry years).

Over the SMOSREX site, the fallow biomass is very dense and the dead vegetation residues tend to form a dense vegetal mulch at the soil surface (De Rosnay et al. 2006). In the model, the strong decrease in direct soil evaporation due to the mulch (Gonzalez-Sosa et al. 2001) is not represented explicitly. In order to represent the mulch effect, a fixed vegetation cover fraction of 100 % was assumed in the ISBA-A-gs simulations. Test simulations were performed with lower vegetation cover fraction values (allowing bare soil evaporation) and showed that this effect is not sufficient to simulate a total soil moisture content below the wilting point. In the field, phenomena like the formation of deep cracks into the soil may foster the soil evaporation and this process is not accounted for by the model.

The use of a soil multi-layer scheme, which describes more accurately the evolution of the prognostic variables during dry periods than a single layer model with an averaged soil moisture content, may lead to a better prediction of soil moisture and LAI. In particular, the impact on the vegetation of rewetting the top soil layer is better accounted for by a multilayer model. However, the inclusion of several soil layers would augment the computational burden of the assimilation. The assimilation of observations into a multi-layer soil model is not a simple task. If all layers are to be analysed individually, an understanding of the error-correlation between near-surface soil moisture observations and the different layers are required (Reichle et al. 2001, Walker et al. 2002).

It was shown that when precipitation observations contain large errors, the joint assimilation of \( w_k \) and LAI is capable of restoring the annual trend of \( w_2 \) and vegetation
biomass, but large errors may occur in the absolute value of these quantities. An attempt was made to deactivate the plant growth module of the model and to analyse $w_2$ only. In this case, the observed LAI was prescribed to the model instead of being assimilated. The soil moisture evolution was better predicted, because the root-plant water extraction and evapotranspiration rates were more realistic. In case of large precipitation errors, imposing LAI from external observations may be an advantage for the retrieval of soil moisture. However, as stated above, a large error in the LAI observations may prevent the assimilation scheme to lead to a significant improvement.

In this study, an assimilation window of 10 days was used. Longer windows have the advantage of reducing the computing time but they result in a degradation of the model prediction. For example, a test with a 30-day assimilation window showed that the score $E$ of the analysed $w_2$ and vegetation biomass decreased from 0.86 and 0.23, respectively, to 0.79 and a negative value.

5. Conclusion

In the SMOSREX case study, the joint assimilation of $w_g$ and LAI observations by using a simplified 1D-VAR assimilation scheme over a fallow, has demonstrated that:

- The temporal evolution of both $w_2$ and the vegetation biomass are significantly improved by the assimilation. The assimilation scheme generally reduces the model underestimation of vegetation biomass during the growing phase and, especially, the overestimation of vegetation biomass during the senescence phase of the vegetation.
- The use of a non-stationary $w_{wilt}$ is required for dry years during which soil moisture observations are found below the a priori value of $w_{wilt}$. This change limits
the vegetation mortality during (and after) very dry conditions and the underestimation of the evapotranspiration following an inaccurate simulation of the biomass.

- In the presence of significant errors in the atmospheric forcing, the leaf onset and the seasonal dynamics of the soil moisture are still retrieved well even, for example, if precipitation is set to 0. However, the error on the analysed variables ($w_2$ and the vegetation biomass) is large. In this case, the analysis of $w_2$ is more efficient if the vegetation biomass is not analysed, i.e. if good quality LAI observations are prescribed to the model, instead of simulating the vegetation growth.

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1. a) LAI, b) $w_g$, c) $w_2$ and d) monthly precipitation for 2001 to 2004 as measured over the SMOSREX site. On top the interpolated LAI (solid line) is superimposed to the observations (circles). Note that the spline function used for LAI interpolation changed from one year to another, depending on data quality and frequency. The $w_g$ and $w_2$ simulations of ISBA-A-gs (solid line) using the offensive strategy as response to water stress (drought tolerant) are superimposed to the observations (dots for $w_g$ and stars for $w_2$).

2. Temporal evolution of the linearized $H_{BIO}$ standard deviation. $H_{BIO}$ is computed by an initial perturbation of the vegetation biomass. The standard deviation of $H_{BIO}$ is presented for four different intervals for the initial perturbation of the vegetation biomass: $[0.005, 0.030]$, $[0.03, 0.07]$, $[0.07, 0.10]$, $[0.10, 0.13]$, in units of kg m$^{-2}$. $H_{BIO}$ values are in units of m$^2$ kg$^{-1}$.

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6. Same as Fig. 5, but using a fixed wilting point. The results for the years 2001 and 2002 are omitted as being similar as in Fig. 5.
Figure 1.- a) LAI, b) $w_2$, c) $w_2$ and d) monthly precipitation for 2001 to 2004 as measured over the SMOSREX site. On top the interpolated LAI (solid line) is superimposed to the observations (circles). Note that the spline function used for LAI interpolation changed from one year to another, depending on data quality and frequency. The $w_2$ and $w_2$ simulations of ISBA-A-gs (solid line) using the offensive strategy as response to water stress (drought tolerant) are superimposed to the observations (dots for $w_2$ and stars for $w_2$).
Figure 2.- Temporal evolution of the linearized $H_{BIO}$ standard deviation. $H_{BIO}$ is computed by an initial perturbation of the vegetation biomass. The standard deviation of $H_{BIO}$ is presented for four different intervals for the initial perturbation of the vegetation biomass: [0.005, 0.030], [0.03, 0.07], [0.07, 0.10], [0.10, 0.13], in units of kg m$^{-2}$. $H_{BIO}$ values are in units of m$^2$ kg$^{-1}$.
Figure 3.- Analysis of a) the root zone soil moisture (circles) and b) vegetation biomass, using the simplified 1D-VAR method and a dynamical correction of the wilting point for 2001 to 2004 over the SMOSREX experimental site. c) LAI before and after the assimilation. For comparison purposes, analysed values are superimposed over the in-situ observations (points) and the model basic estimations (solid line).
Figure 4.- Analysis of a) the root zone soil moisture (circles) and b) vegetation biomass, using the simplified 1D-VAR method and a fixed wilting point for 2003 to 2004 over the SMOSREX experimental site. c) LAI before and after the assimilation. For comparison purposes, analysed values are superimposed over the in-situ observations (points) and the model basic estimations (solid line).
Figure 5: Analysis of a) the root zone soil moisture and, b) vegetation biomass, using the simplified 1D-VAR method for 2001 to 2004, with precipitation set to zero. c) LAI before and after the assimilation. Analyzed values (circles) are superimposed over the in-situ observations (points) and the model basic estimations (solid line) for comparison purposes.
Figure 6.- Same as Fig. 5, but using a fixed wilting point. The results for the years 2001 and 2002 are omitted as being similar as in Fig. 5.
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3. Evapotranspiration yearly cumulated flux (LE, in mm year$^{-1}$) after the assimilation of LAI and $w_g$ observations for four different model configurations, and for the control simulation.
TABLE 1.
Main soil and vegetation parameters used in the ISBA-A-gs simulations over the SMOSREX site.

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<th>Soil parameters</th>
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<th>Value</th>
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<table>
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<td>Leaf nitrogen concentration</td>
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TABLE 2.
Yearly and global RMSE and mean bias for the root zone-soil moisture (in m³ m⁻³), the above-ground vegetation biomass (in kg m⁻²), and the LAI (in m² m⁻²) of the analyses (4 model configurations) and the control simulation. The score E (dimensionless) is indicated.

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<td>0.06</td>
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TABLE 3.

Evapotranspiration yearly cumulated flux (LE, in mm year\(^{-1}\)) after the assimilation of LAI and \(w_g\) observations for four different model configurations, and for the control simulation.

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<td>dynamic (w_{wilt}) and no rain</td>
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<td>144.7</td>
<td>171.1</td>
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