

Ocean Waves

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Waves breaking on the sea front in Ardrossan, Western Scotland,
as Storm Gertrude hits the UK on January 29, 2016.

IMAGE: DANNY LAWSON/PA WIRE/ASSOCIATED PRESS



Ocean waves:

We are dealing with wind generated waves from gentle to rough ...



May 1, 2013

Porthleven Clock Tower, Cornwall, UK

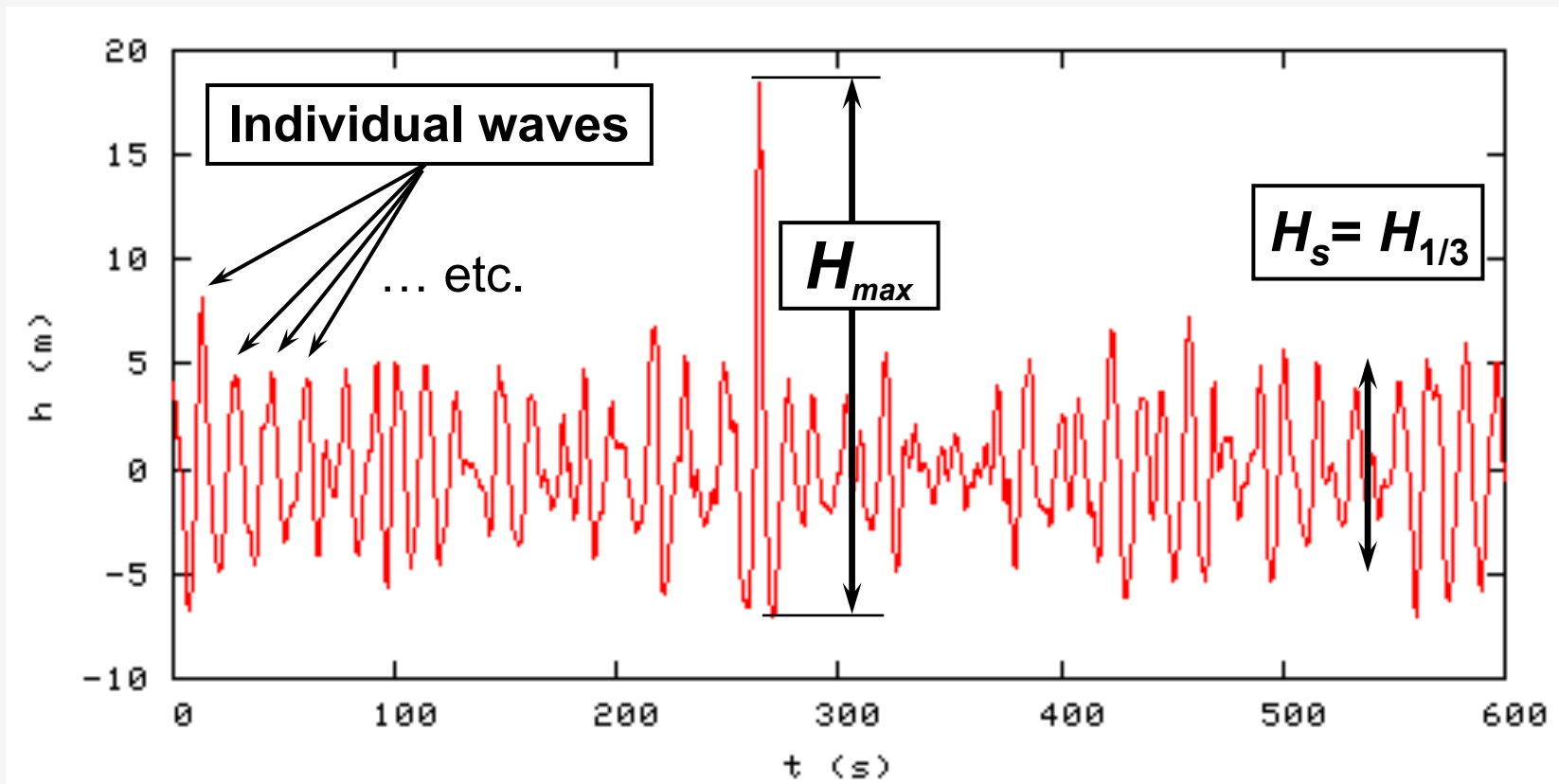


February 5, 2014

Observe Individual Waves,

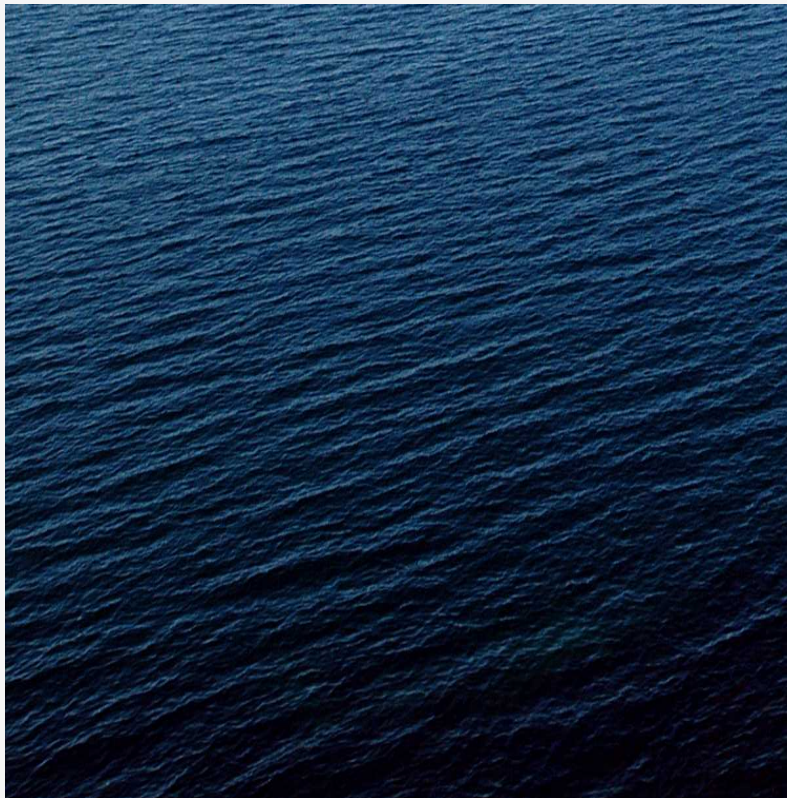
After a while, you can estimate a characteristic height the waves:
the Significant Wave Height, H_s ,

You might also notice that some waves are larger than the rest,
characterised by the Maximum Individual Wave Height, H_{max}

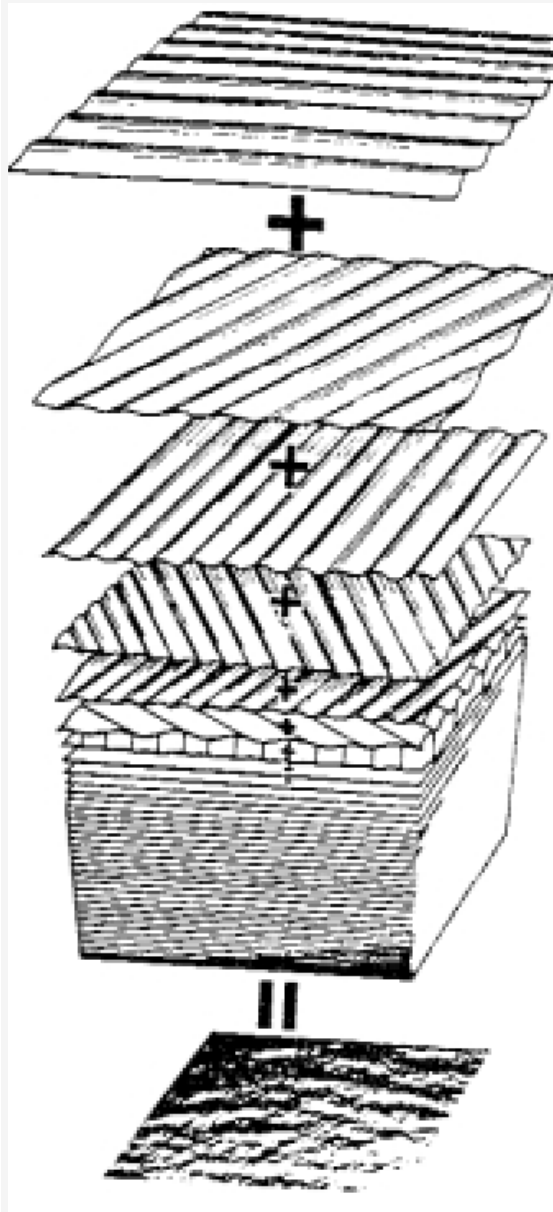


Surface elevation time series from platform Draupner in the North Sea

How do we go about making predictions on the sea state?

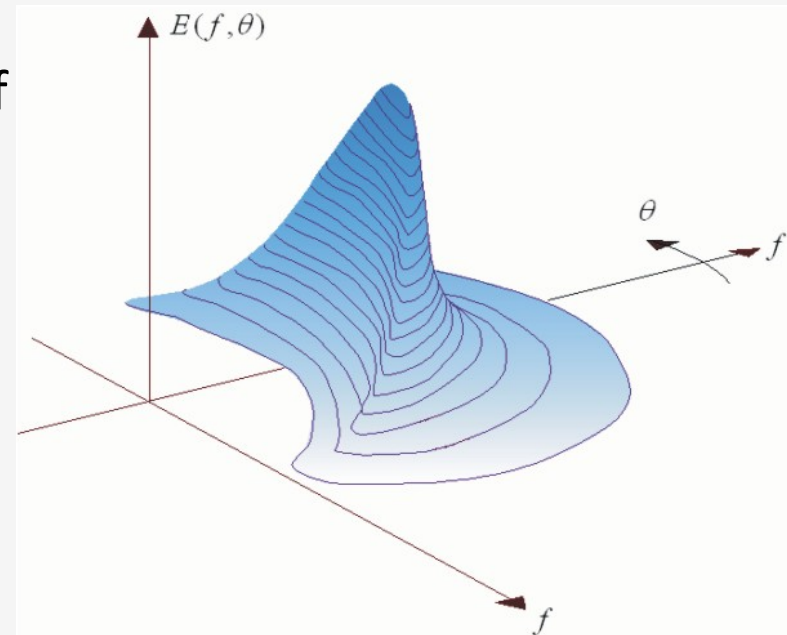


Wave Spectrum



- The irregular water surface can be decomposed into (*infinite*) number of simple sinusoidal components with different **frequencies** (f) and propagation **directions** (θ).

- The distribution of wave energy among those components is called: “**wave spectrum**”, $F(f, \theta)$.

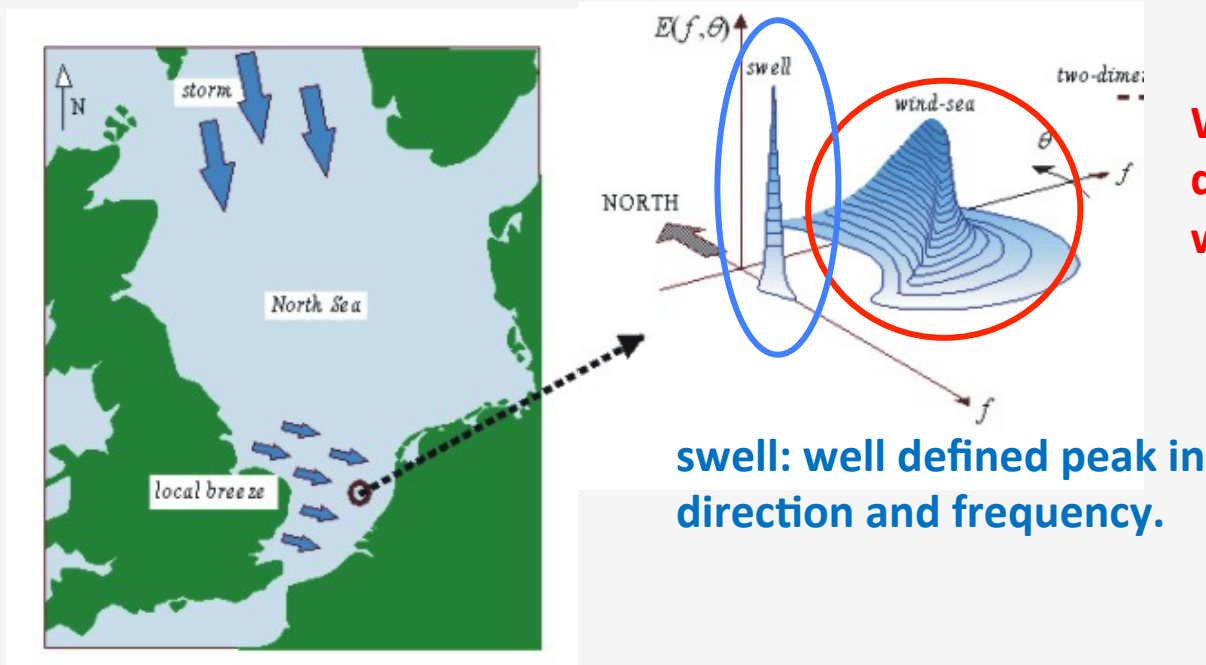


Modern ocean wave prediction systems are based on statistical description of oceans waves (i.e. ensemble average of individual waves).

The sea state is described by the two-dimensional wave spectrum $F(f, \theta)$.

For instance, the sea state off the coast of Holland might be the result of a local sea breeze. These waves are generally known as **windsea**

Waves might have also propagated from their generation area as **swell**



Windsea: broad distribution of the waves around a peak

swell: well defined peak in direction and frequency.

Ocean Wave Modelling

- The 2-D spectrum follows from the energy balance equation (in its simplest form: deep water case):

$$\frac{\partial F}{\partial t} - \vec{V}_g \cdot \nabla F = S_{in} - S_{nl} + S_{diss}$$

Where the group velocity V_g is derived from the dispersion relationship which relates frequency and wave number.

S_{in} : wind input source term (**generation**).

S_{nl} : non-linear 4-wave interaction (**redistribution**).

S_{diss} : dissipation term due to whitecapping (**dissipation**).

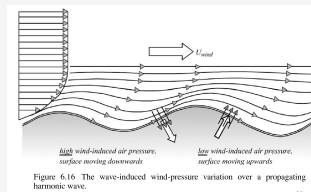


Figure 6.16 The wave-induced wind-pressure variation over a propagating harmonic wave.

the wave grows by this mechanism, the mechanism becomes more effective, etc.

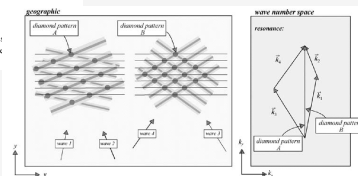
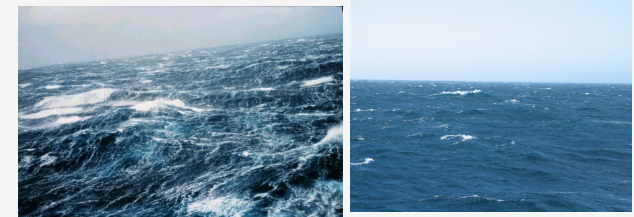


Figure 6.20 Quadruplet wave-wave interactions (realisable in deep water). Two pairs of wave components can create two diamond patterns with identical wave lengths and directions and therefore identical wave numbers. When the four waves are superimposed (not shown here), they can thus resonate. The wave-number vectors of the four wave components are shown in the right-hand panel in wave-number space with $k_1 + k_2 = k_3 + k_4$.



Wave Model Parameters

- Once you know the wave spectrum F , any other sea state parameters can be estimated. For example, the mean variance of the sea surface elevation η due to waves is given by:

$$\langle \eta^2 \rangle = \iint F(f, \theta) df d\theta$$

- The statistical measure for wave height, called the **significant wave height** (H_s):

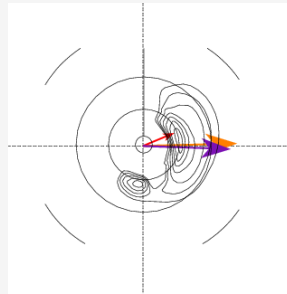
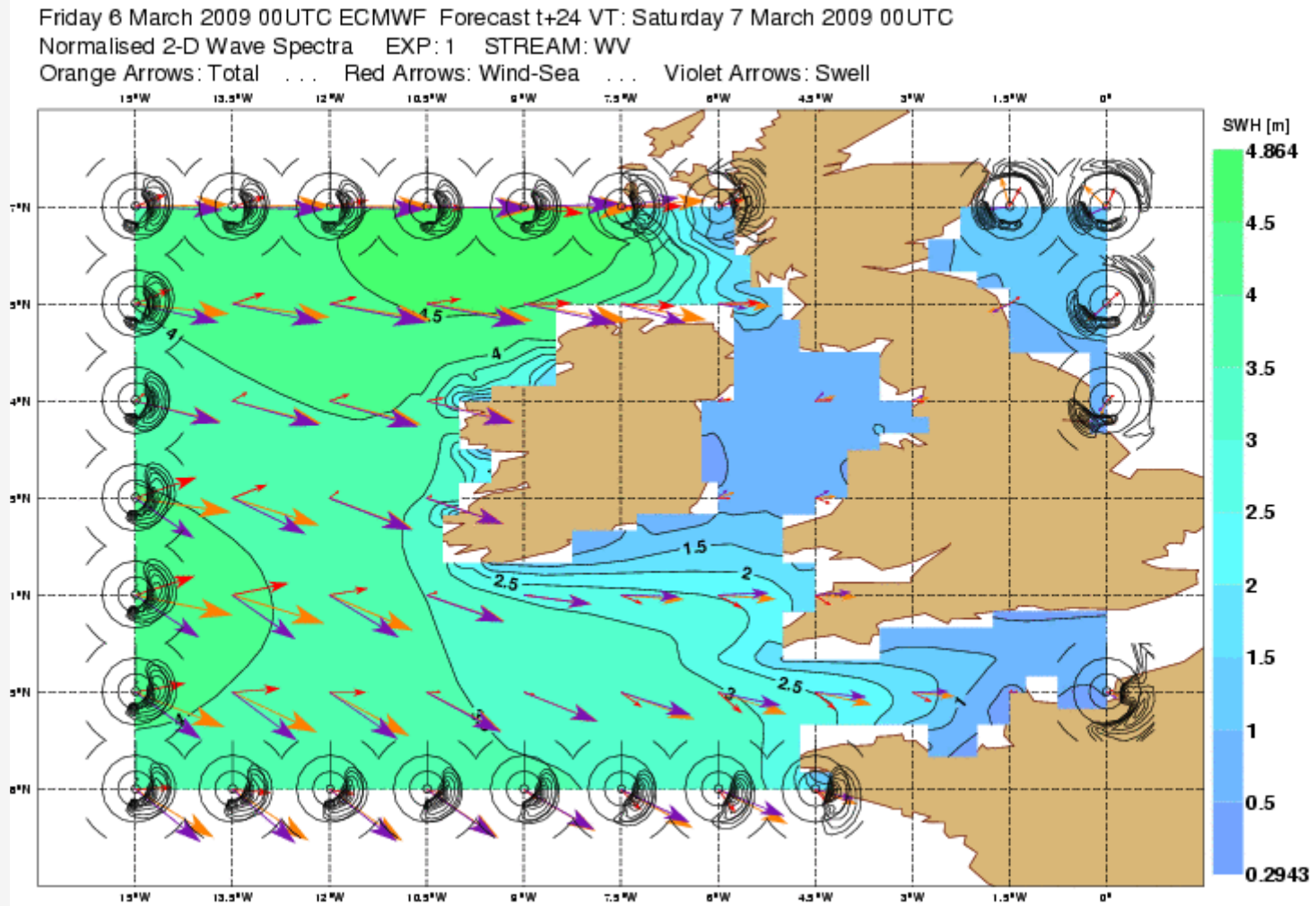
$$H_s = 4\sqrt{\langle \eta^2 \rangle}$$

The term **significant wave height** is historical as this value appeared to be well correlated with visual estimates of wave height from experienced observers.

It can be shown to correspond to the average 1/3rd highest waves ($H_{1/3}$).

Wave Model Parameters

2-D spectrum can be used to specify boundary conditions for limited area wave model.

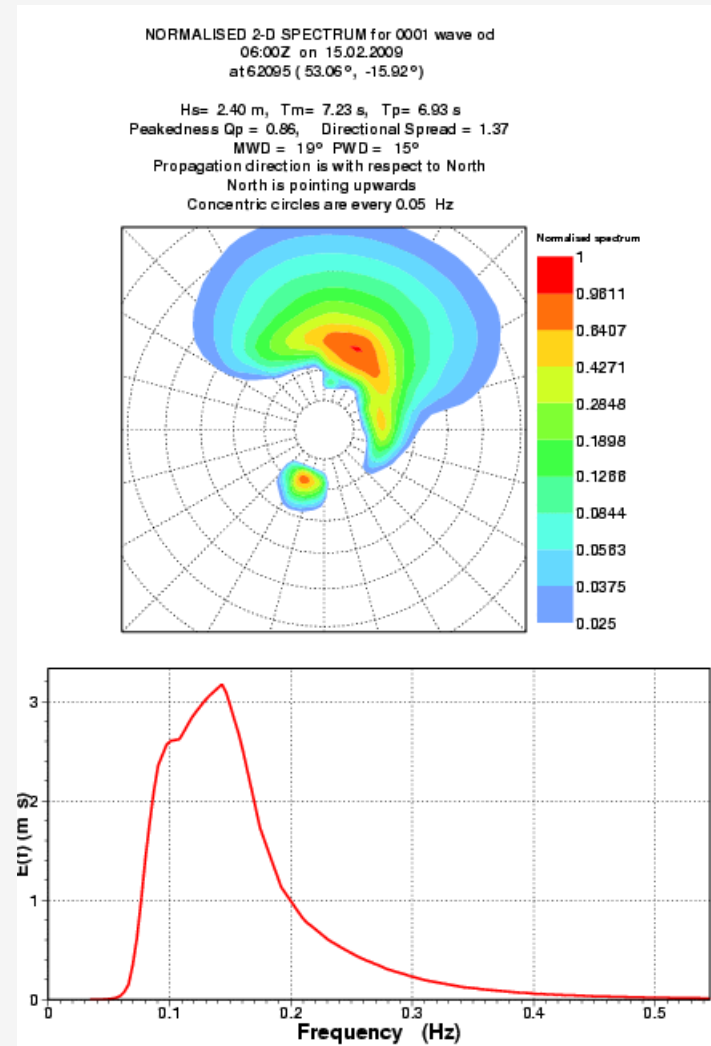


Spectra used as boundary conditions

- windsea
- swell
- total sea

Wave Model Parameters

Or if you only look at one location ...

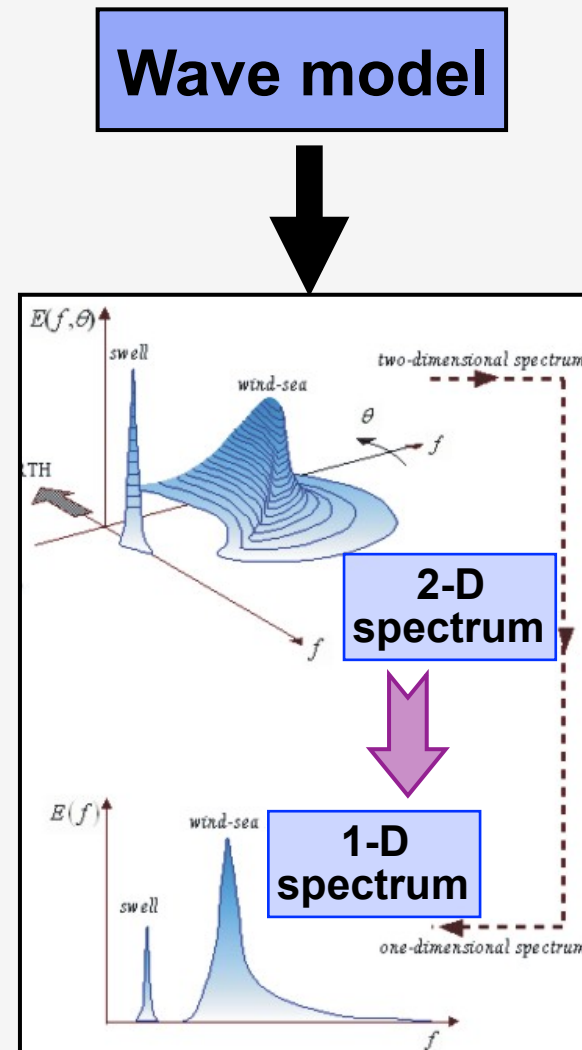


Wave Model Products

The complete description of the sea state is given by the 2-D spectrum, however, it is a fairly large amount of data.

It is therefore reduced to integrated quantities:

1-D spectrum obtained by integrating the 2-D spectrum over all directions and/or over a frequency range.



Wave Model Parameters

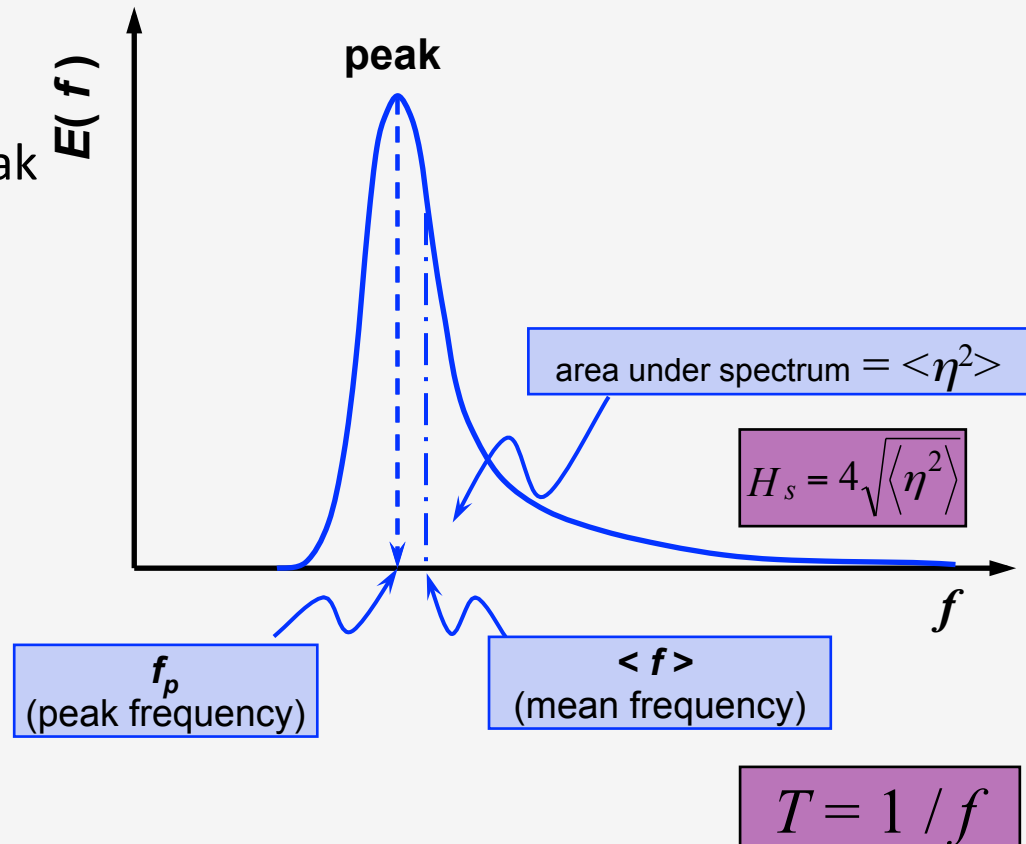
When simple numbers are required, the following parameters are available:

The significant wave height (H_s).

The peak period (period of the peak of the 1-D spectrum).

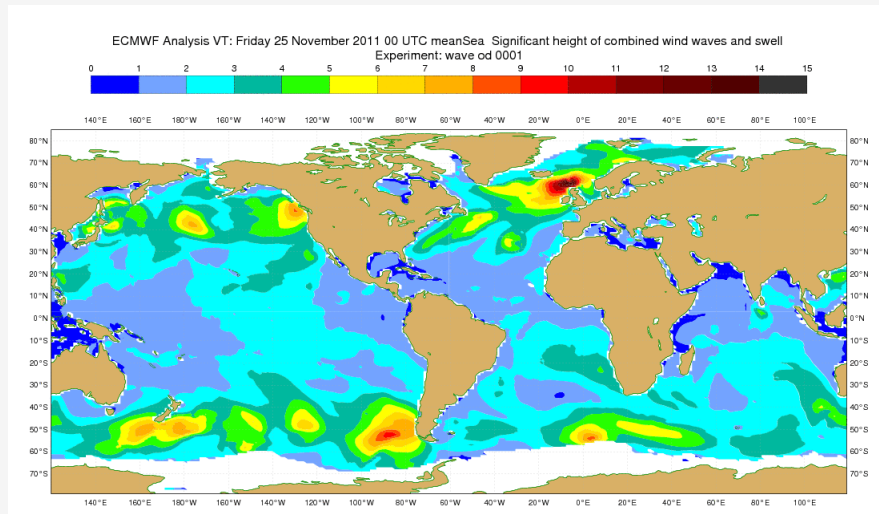
Mean period(s) obtained from weighted integration of the 2-D spectrum.

Integrated mean direction.
and many others.



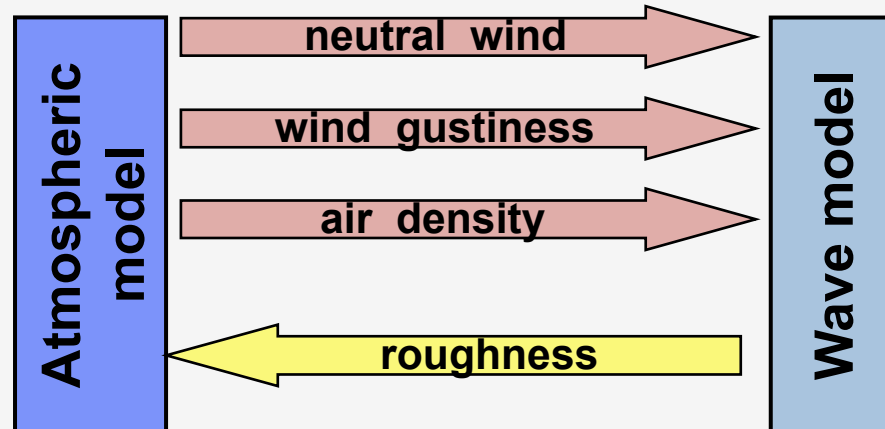
Complete list at: <http://www.ecmwf.int/services/archive/d/parameters/order=/table=140/>

ECMWF Wave Model Configurations



Global from 81°S to 90°N

Coupled to the atmospheric model with feedback of the sea **surface roughness** change due to waves.



ECMWF Wave Model Configurations

High resolution (HRES-WAM)

- 28 km grid spacing.
- Dissemination grid: $0.25^{\circ} \times 0.25^{\circ}$
- 36 frequencies.
- 36 directions.
- Coupled to the TL1279 model.

- Analysis every 6 hrs and 10 day forecasts from 0 and 12 UTC.

Ensemble forecasts (EPS-WAM)

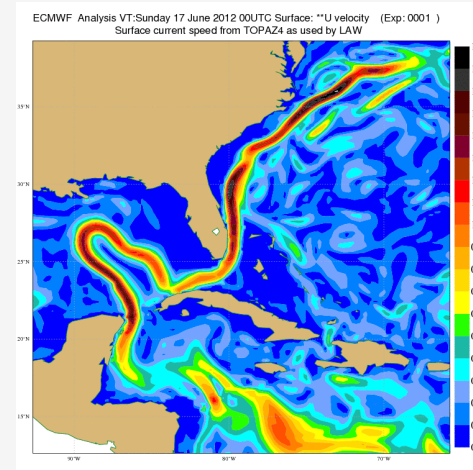
- 55 km grid spacing.
- Dissemination grid: $0.5^{\circ} \times 0.5^{\circ}$
- 30 frequencies.
- 24 directions .
- Coupled to TL639 .
- (50+1) (10+5) day forecasts from 0 and 12UTC (monthly twice a week).
- **Coupled to ocean model.**

ECMWF Wave Model Configurations

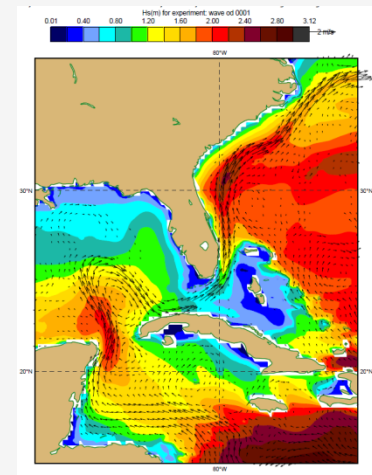
We also have the uncoupled global configuration (stand alone)

High resolution stand alone(HRES-SAW)

- **11 km** grid spacing.
- Dissemination grid: $0.125^\circ \times 0.125^\circ$
- 36 frequencies.
- 36 directions.
- Forced by HRES fields.
- Analysis every 6 hrs and 10 day forecasts from 0 and 12 UTC.
- Imposed surface currents from TOPAZ4 system.



TOPAZ4
surface currents



ECMWF Wave Model Configurations after the upgrade in March (in bold)

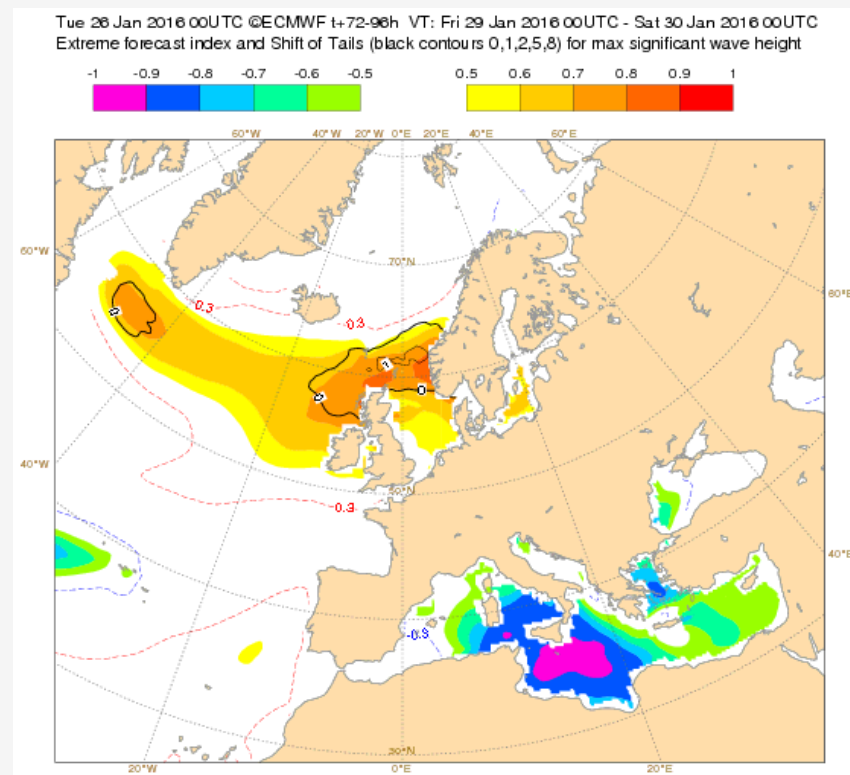
	HRES-WAM	ENS-WAM	HRES-SAW
resolution	14km	28km	11km
dissemination	0.125°x0.125°	0.25°x0.25°	0.1°x0.1° or 0.125°x0.125°
frequencies	36	36	36
directions	36	36	36
forcing	Tco1279	Tco639	HRES

NB: HRES-SAW unchanged except for dissemination,
Ongoing work to move HRES-SAW to unstructured grid.

Wave Model Products: EFI plots

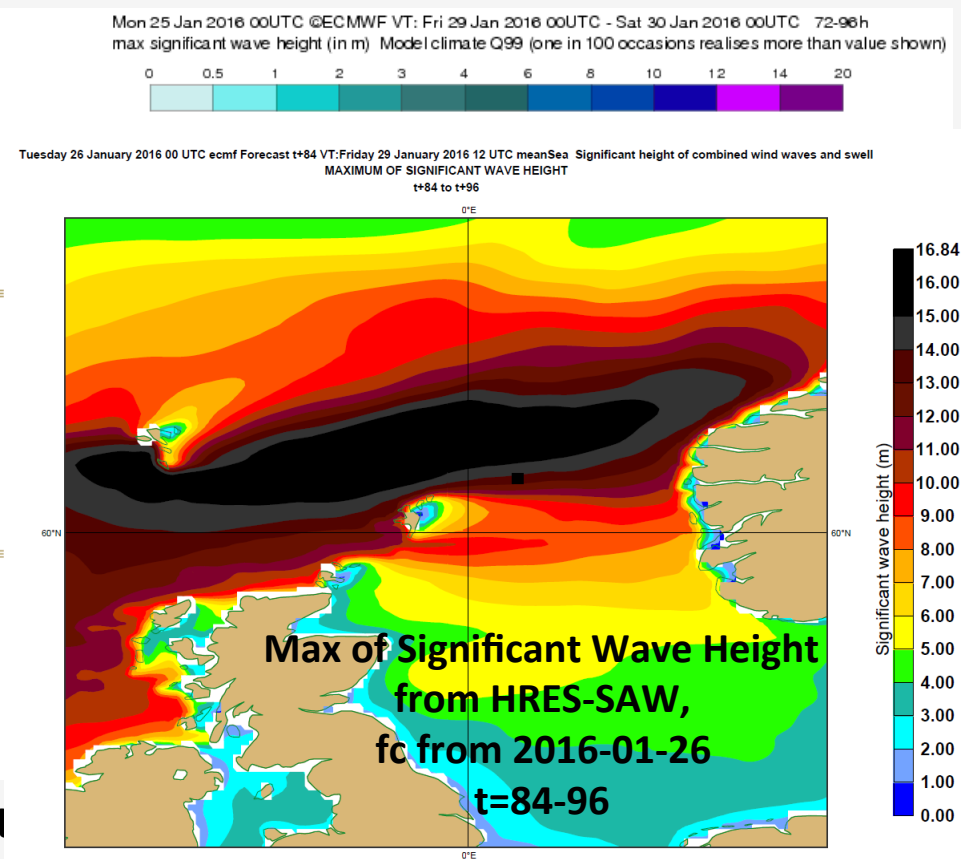
From the model climate, it is possible to derive indices that indicate deviations in probabilistic terms from what is 'expected'.

Extreme Forecast Index (EFI): 1 means that all EPS are above climate.



EFI and shift of tail for significant wave height

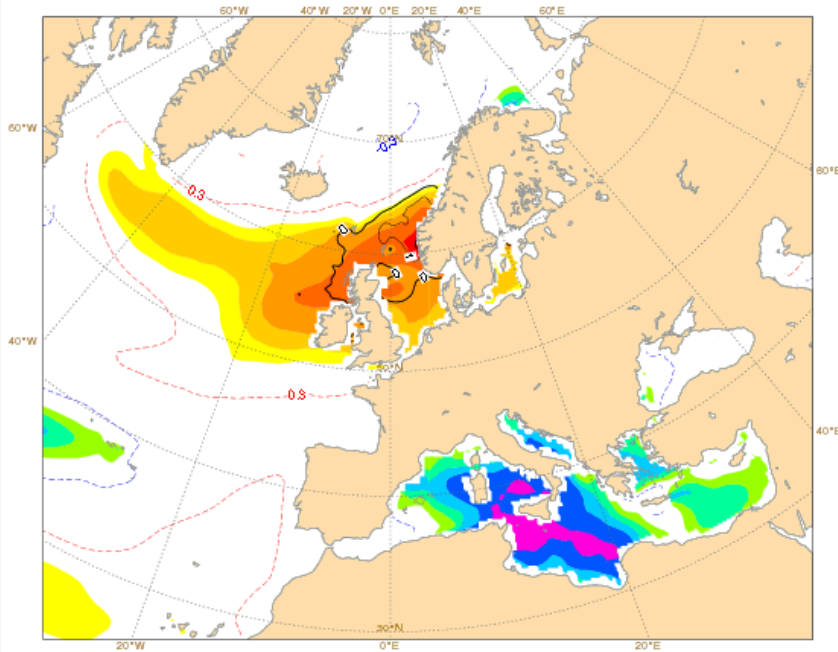
Tue 26 Jan 2016, 00 UTC, t=72-96
Gertrude (UK), Tor (Norway)



significant wave height

Wave Model Products

Wed 27 Jan 2016 00UTC @ECMWF t+48-72h VT: Fri 29 Jan 2016 00UTC - Sat 30 Jan 2016 00UTC
 Extreme forecast index and Shift of Tails (black contours 0,1,2,5,8) for max significant wave height

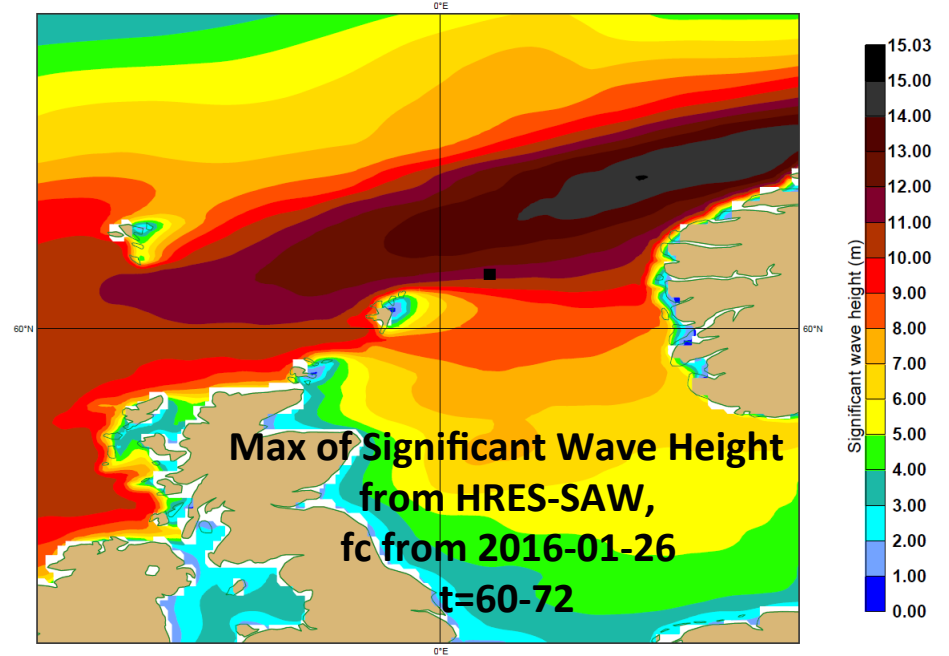


Wed 27 Jan 2016, 00 UTC, t=48-72

Mon 25 Jan 2016 00UTC @ECMWF VT: Fri 29 Jan 2016 00UTC - Sat 30 Jan 2016 00UTC 48-72h
 max significant wave height (in m) Model climate Q99 (one in 100 occasions realises more than value shown)

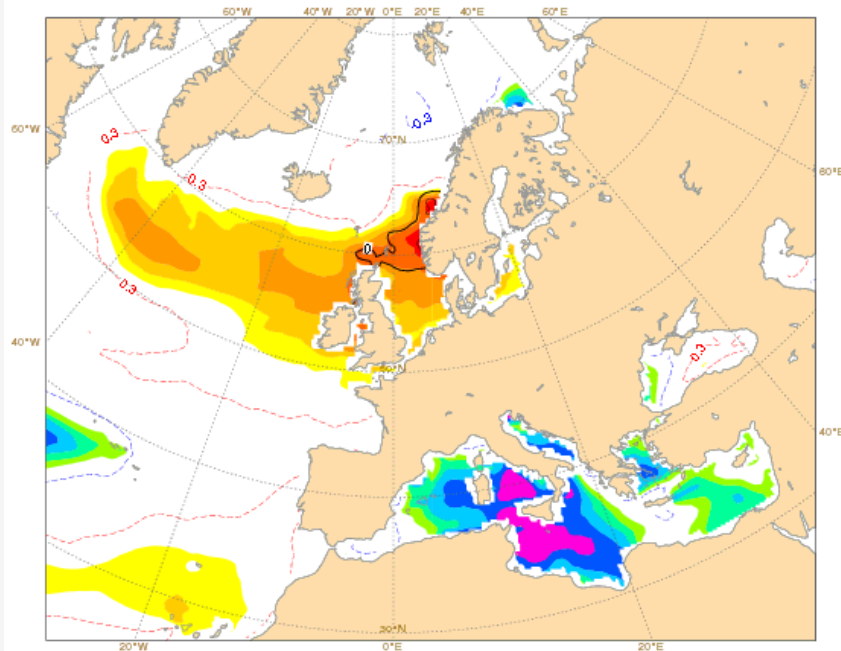


Wednesday 27 January 2016 00 UTC ecmf Forecast t+60 VT: Friday 29 January 2016 12 UTC meanSea Significant height of combined wind waves and swell
 MAXIMUM OF SIGNIFICANT WAVE HEIGHT
 t+60 to t+72



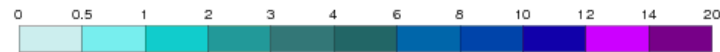
Wave Model Products

Fri 29 Jan 2016 00UTC @ECMWF t+0-24h VT: Fri 29 Jan 2016 00UTC - Sat 30 Jan 2016 00UTC
 Extreme forecast index and Shift of Tails (black contours 0,1,2,5,8) for max significant wave height

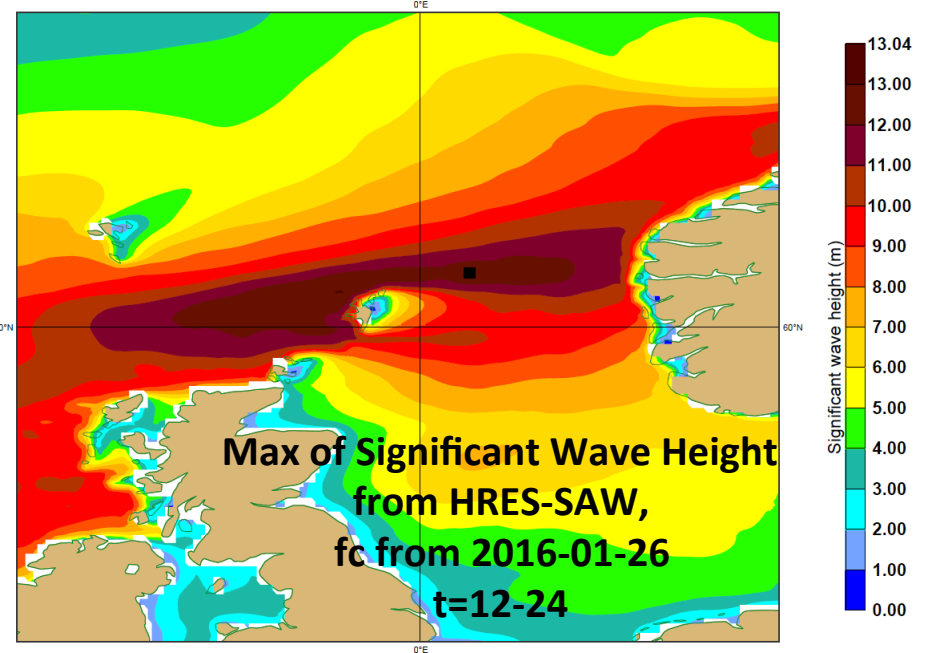


Fri 29 Jan 2016, 00 UTC, t=12-24

Thu 28 Jan 2016 00UTC @ECMWF VT: Fri 29 Jan 2016 00UTC - Sat 30 Jan 2016 00UTC 0-24h
 max significant wave height (in m) Model climate Q99 (one in 100 occasions realises more than value shown)

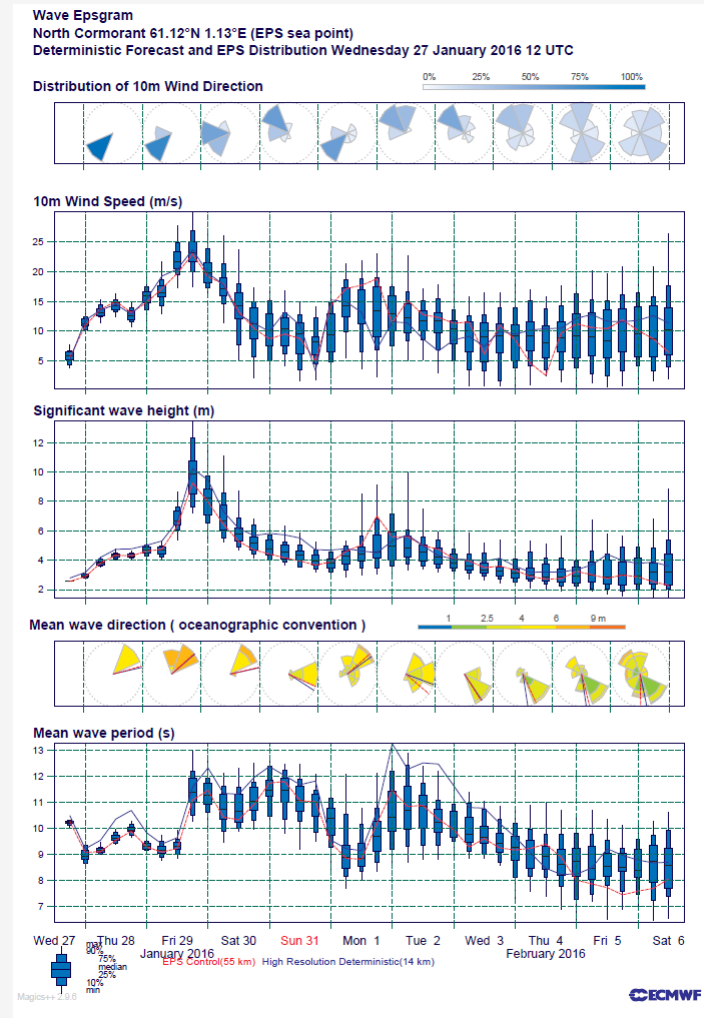
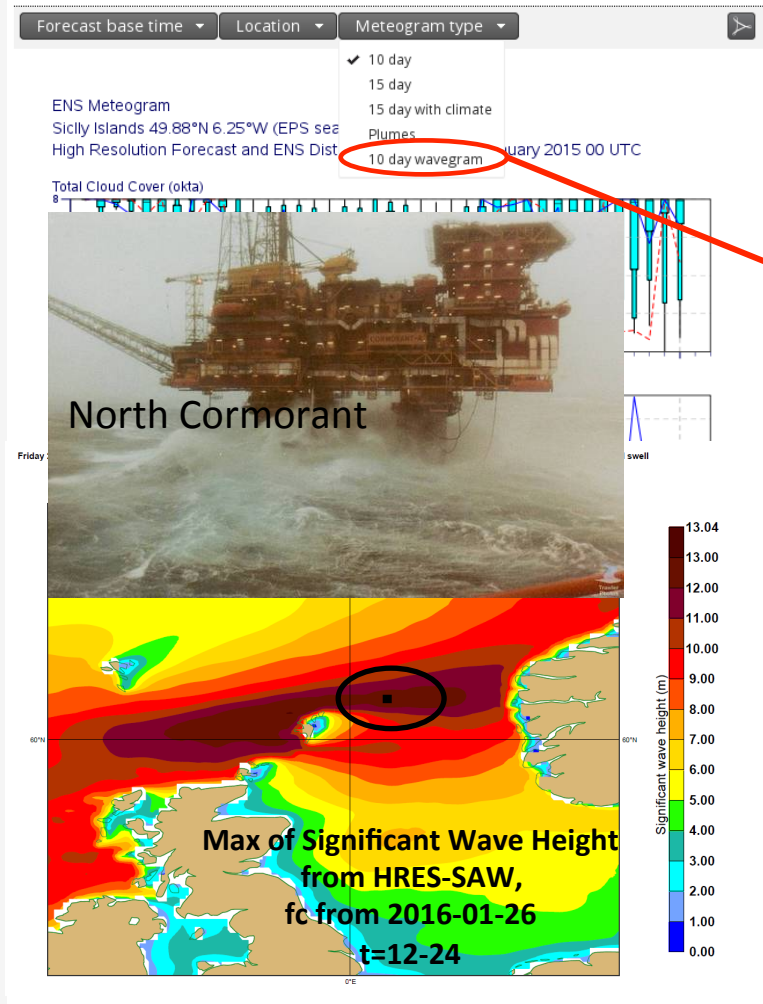


Friday 29 January 2016 00 UTC ecmf Forecast t+12 VT: Friday 29 January 2016 12 UTC meanSea Significant height of combined wind waves and swell
 MAXIMUM OF SIGNIFICANT WAVE HEIGHT
 t+12 to t+24



A bit more compact: Wave EPSgram:

Like normal EPSgram but for
wind direction, wind speed,
significant wave height,
mean wave direction and mean period.

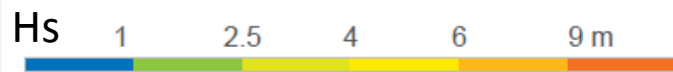


A bit more compact: Wave EPSgram:



max
90%
75%
median
25%
10%
min

ENS Control(55 km) High Resolution (28 km)



Hs

1

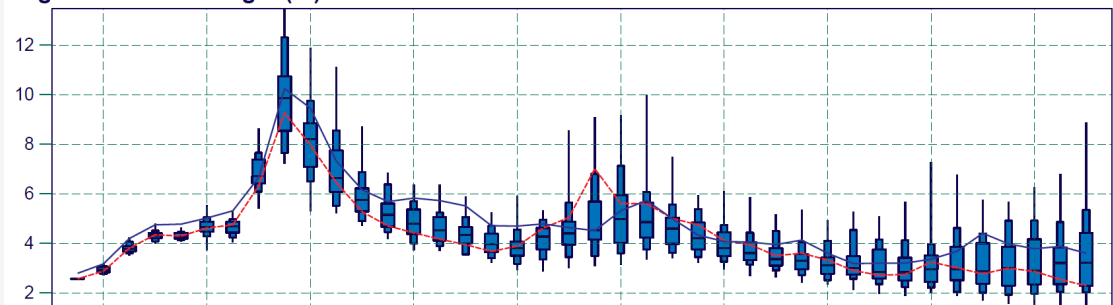
2.5

4

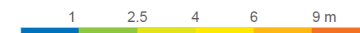
6

9 m

Significant wave height (m)



Mean wave direction (oceanographic convention)



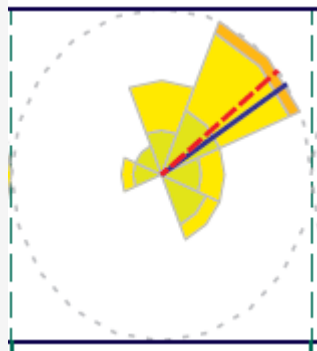
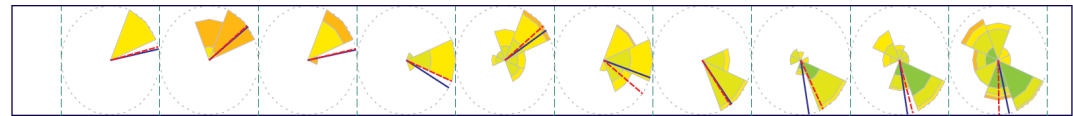
1

2.5

4

6

9 m

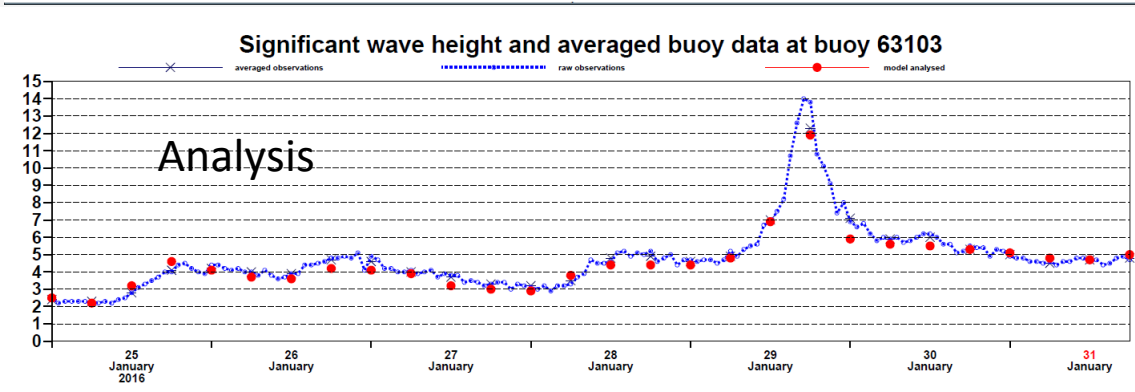
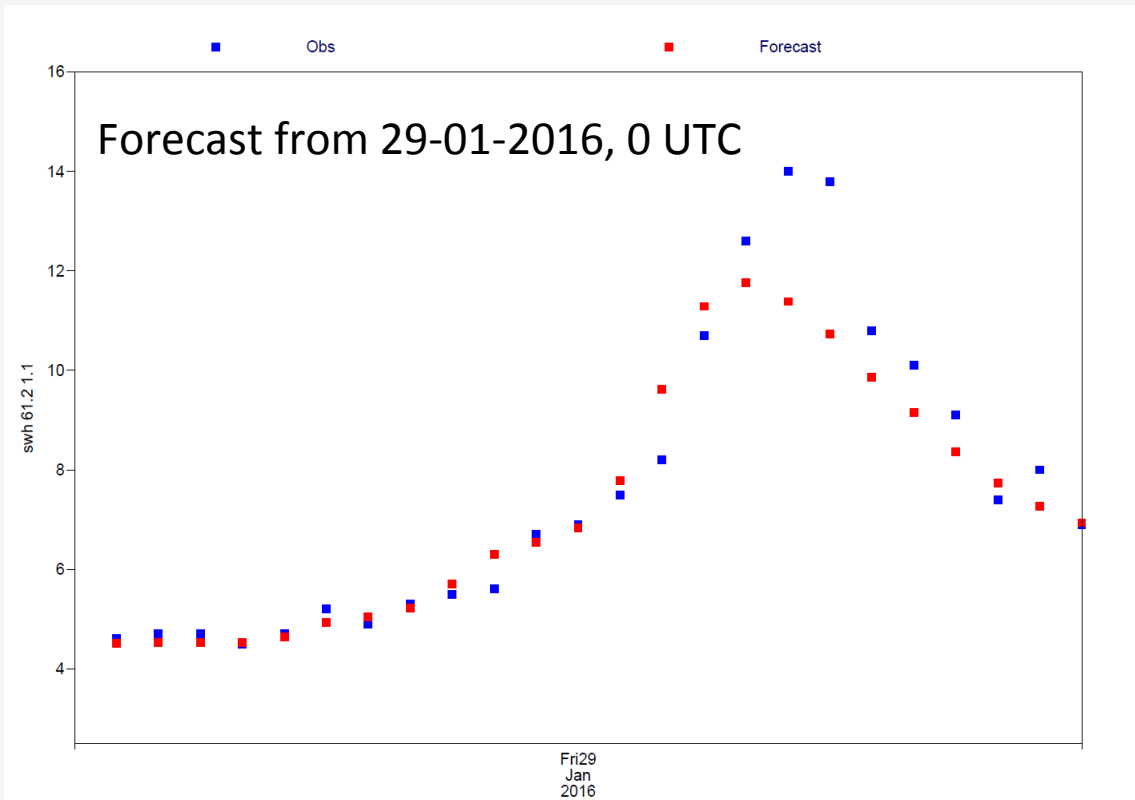
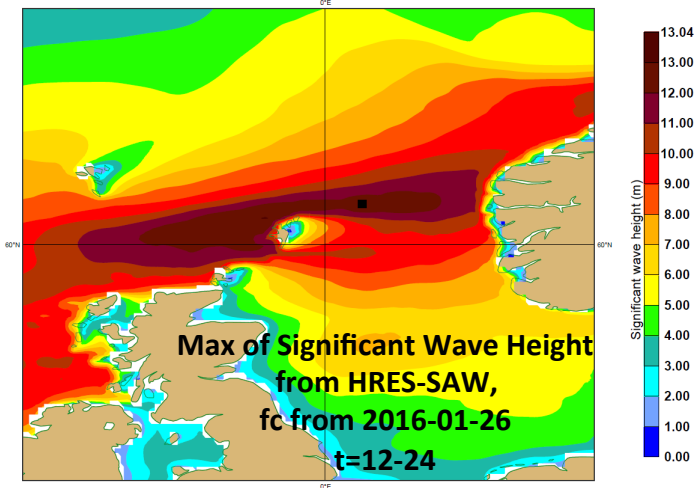


Each octant is coloured based on the distribution of the significant wave height associated with each mean direction. The coloured areas correspond to the fractional number of ensemble members with wave height in the range specified by the coloured ruler.

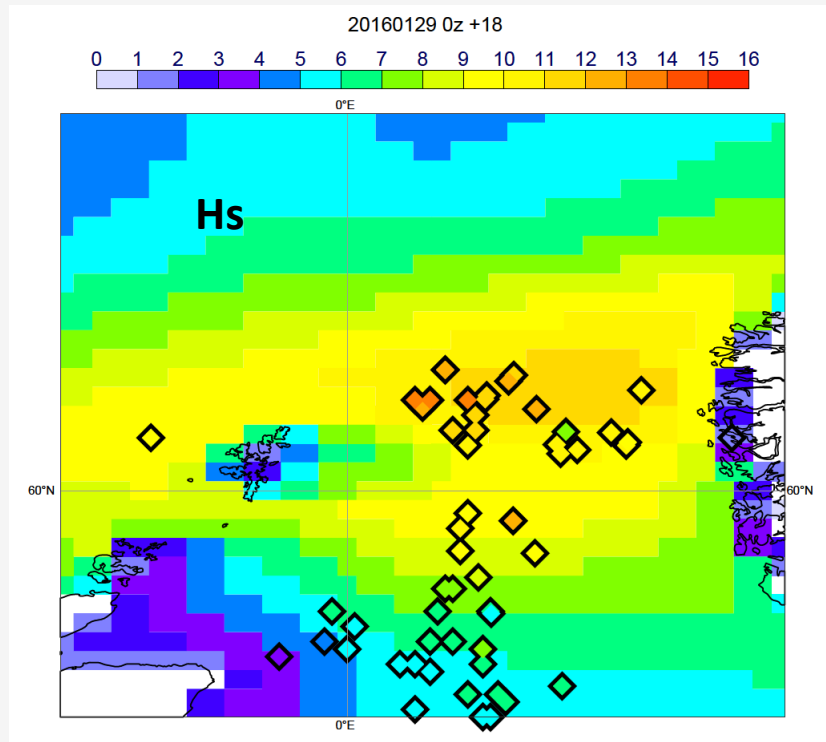
Wave Model Products: how did we do?



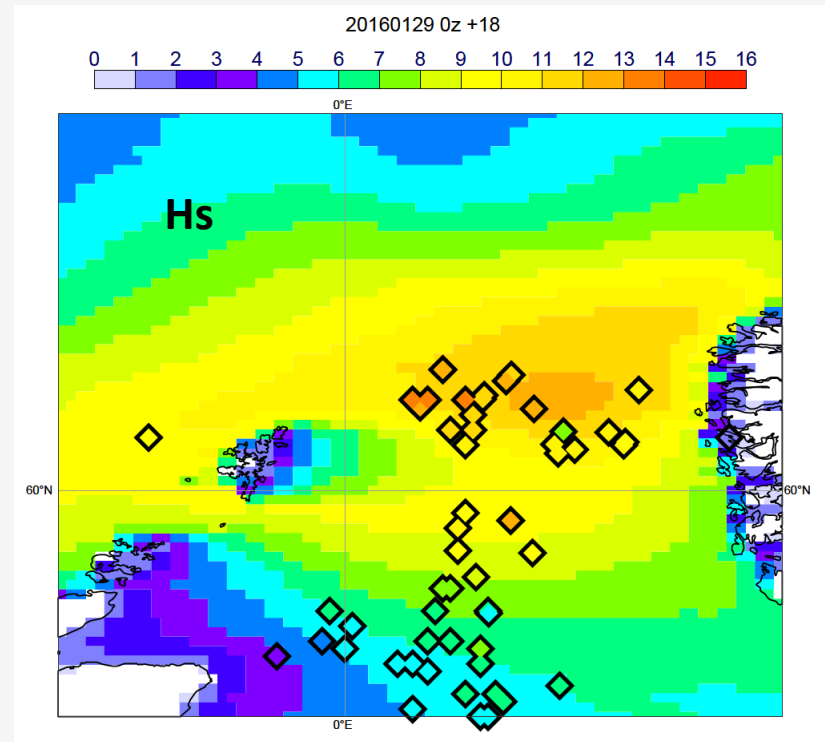
Friday 29 January 2016 00 UTC ecmf Forecast t+12 VT:Friday 29 January 2016 12 UTC meanSea Significant height of combined wind waves and swell
MAXIMUM OF SIGNIFICANT WAVE HEIGHT
t+12 to t+24



Wave Model Products: how did we do?



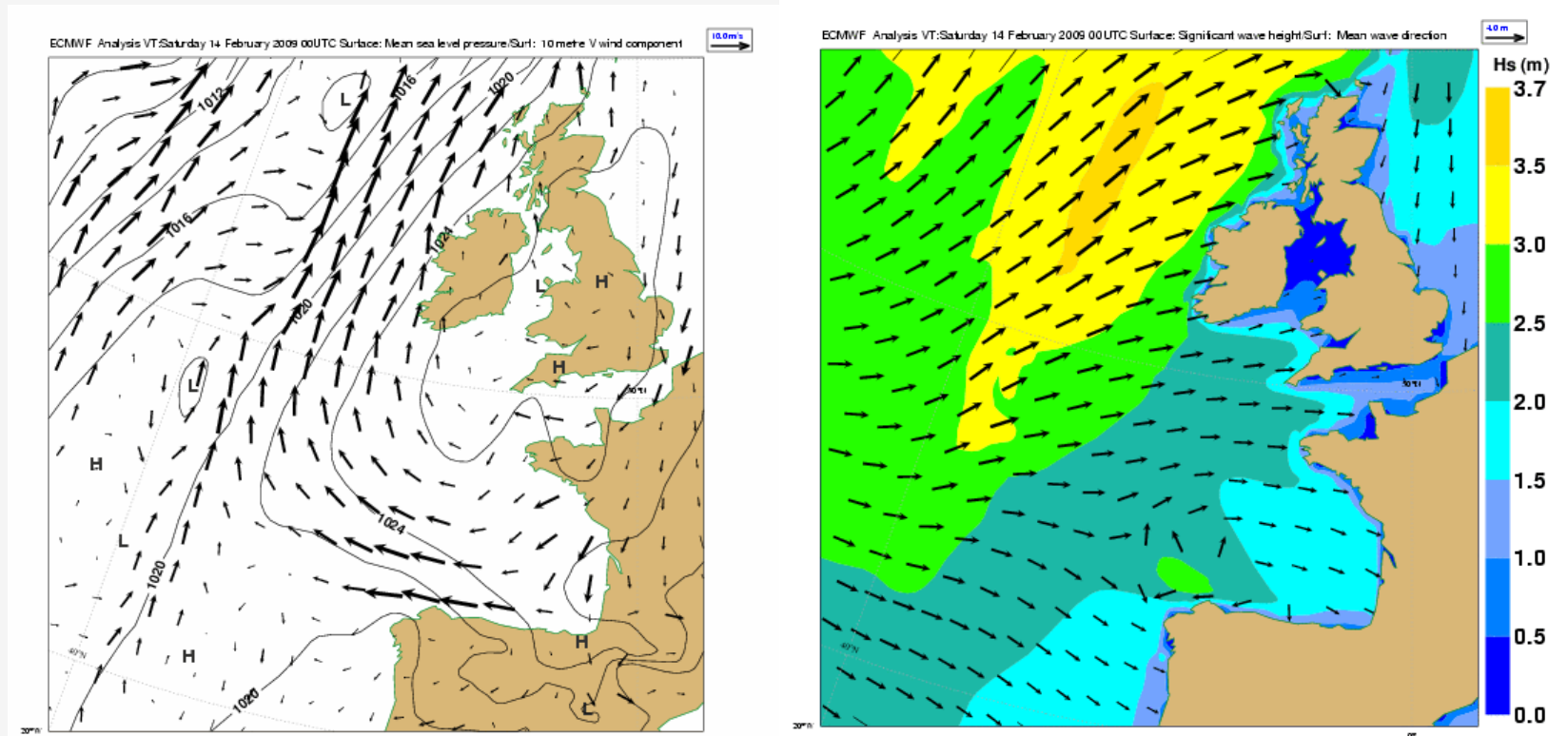
O-suite



E-suite

A bit more on Wave Model Products

**Use simple parameters:
total wave height and mean propagation direction**



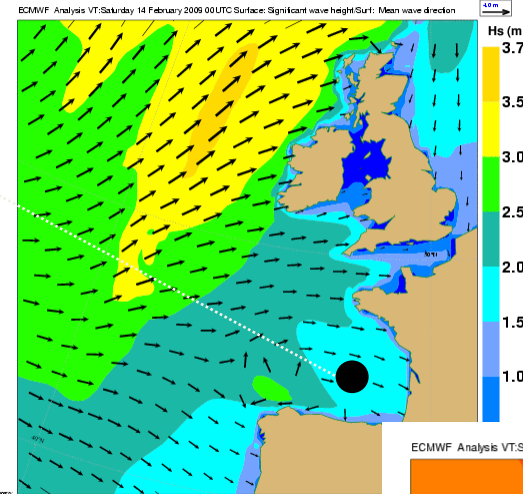
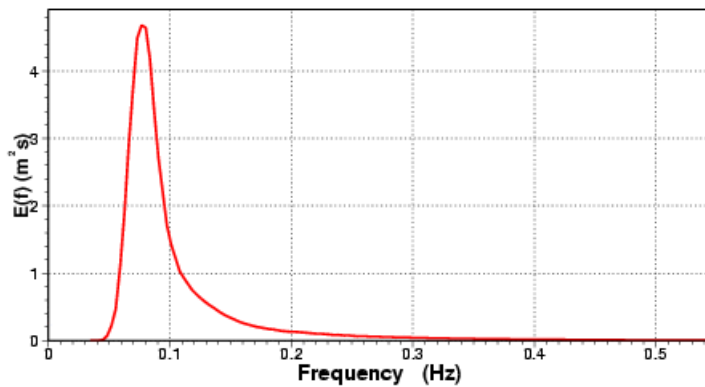
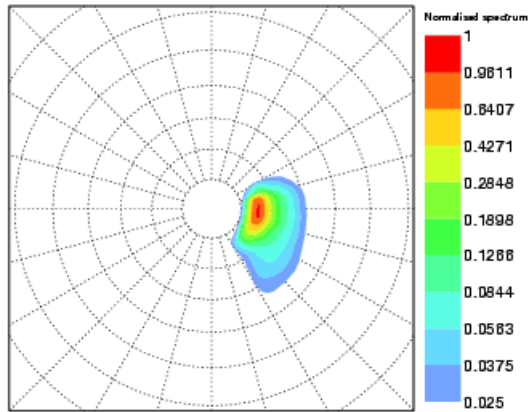
**10m winds and mean sea level pressure:
Analysis : 14 February 2009, 00 UTC**

**Wave height and mean direction:
Analysis : 14 February 2009, 00 UTC**

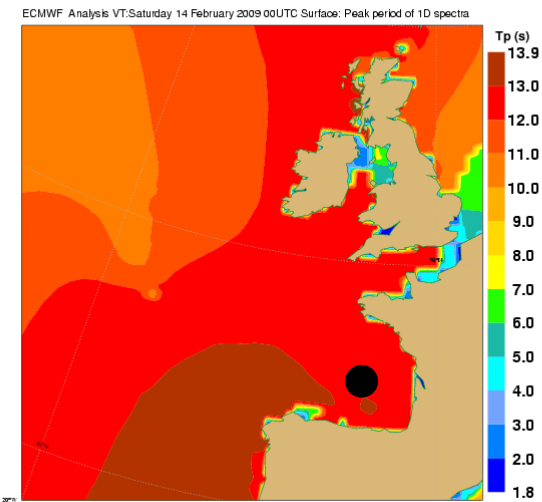
Wave Model Products

NORMALISED 2-D SPECTRUM for 0001 wave od
00:00Z on 14.02.2009
at 62001 (45.20°, -5.00°)

Hs= 1.76 m, Tm=11.25 s, Tp=13.51 s
Peakedness Qp = 2.18, Directional Spread = 1.38
MWD = 93° PWD = 90°
Propagation direction is with respect to North
North is pointing upwards
Concentric circles are every 0.05 Hz



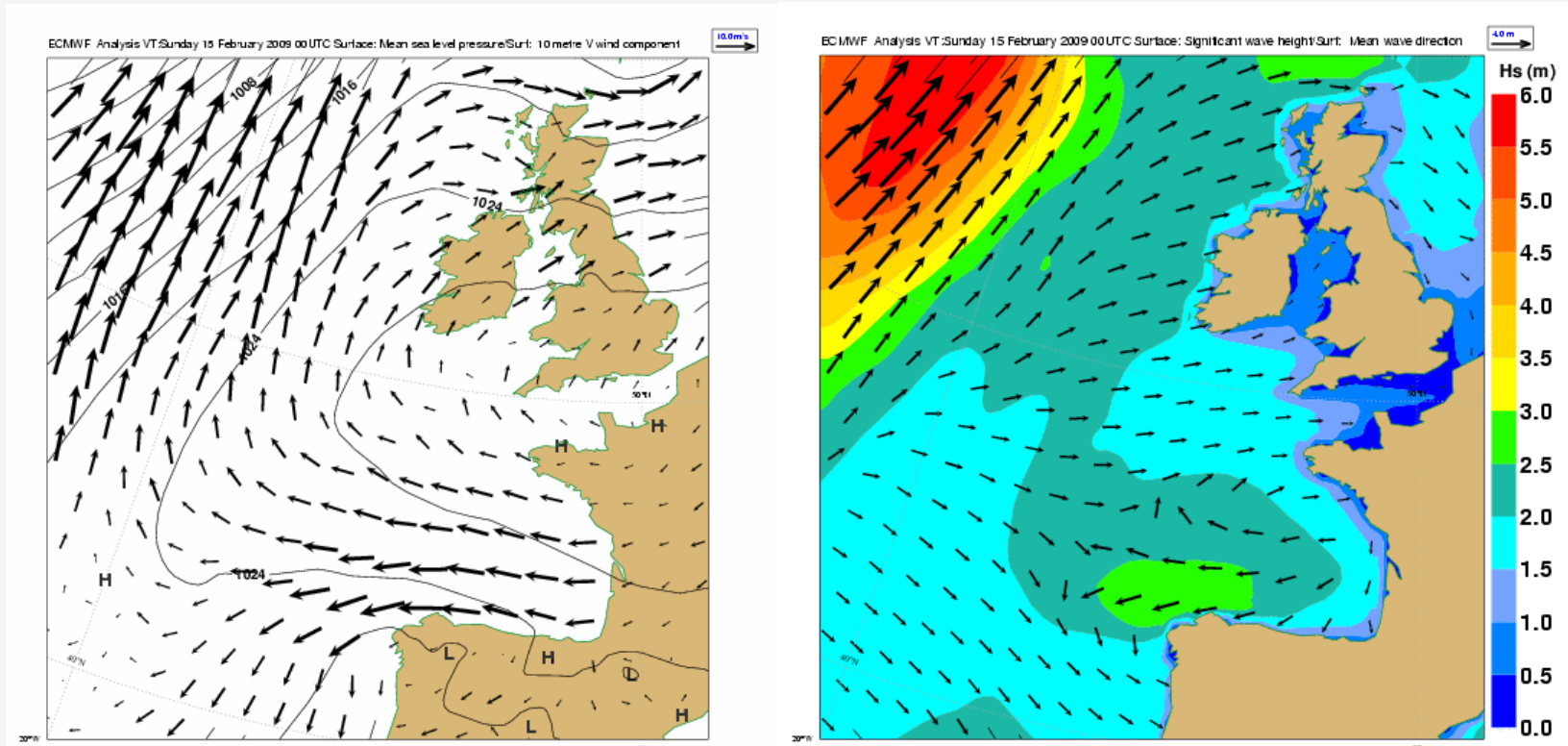
Wave height and me
Analysis : 14 February



PEAK PERIOD:
Analysis : 14 February 2009, 00 UTC

Wave Model Products

Situation might be more complicated !

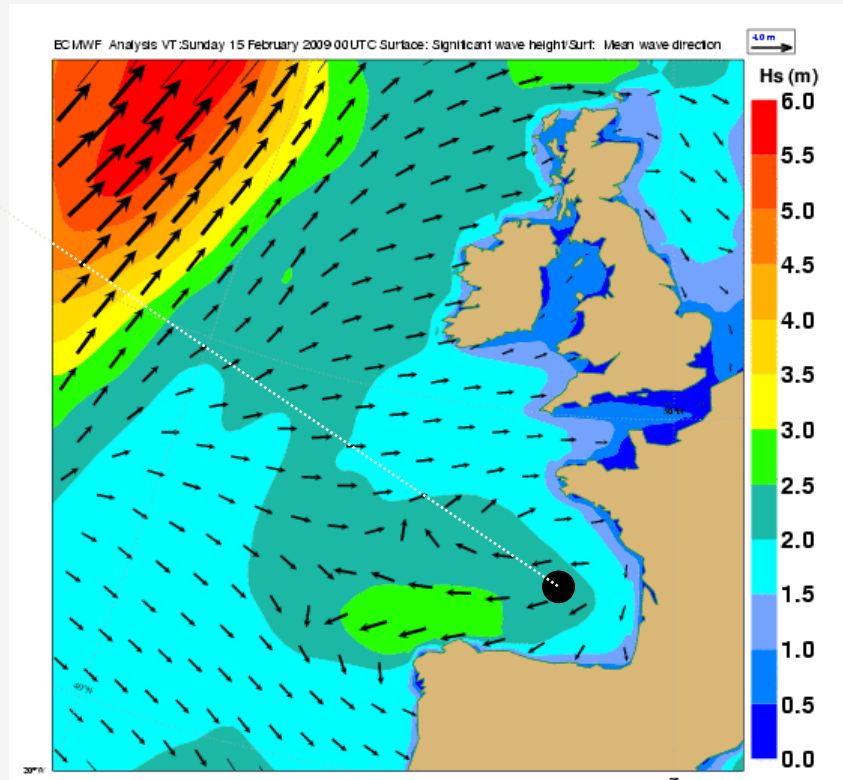
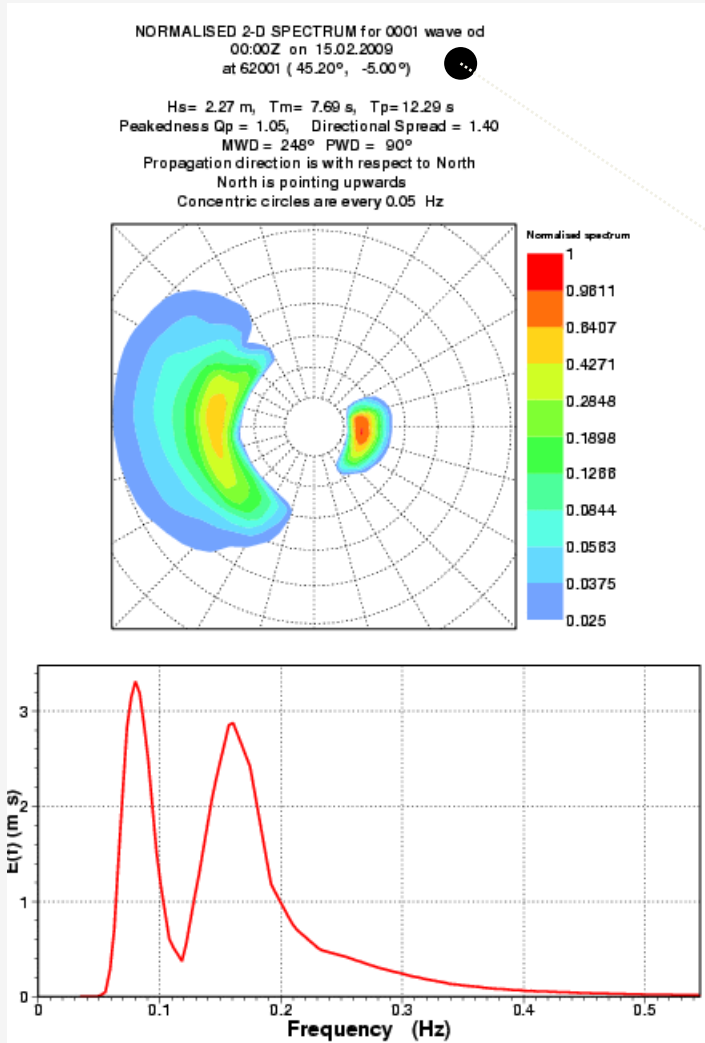


**10m winds and mean sea level pressure:
Analysis : 15 February 2009, 00 UTC**

**Wave height and mean direction:
Analysis : 15 February 2009, 00 UTC**

Wave Model Products

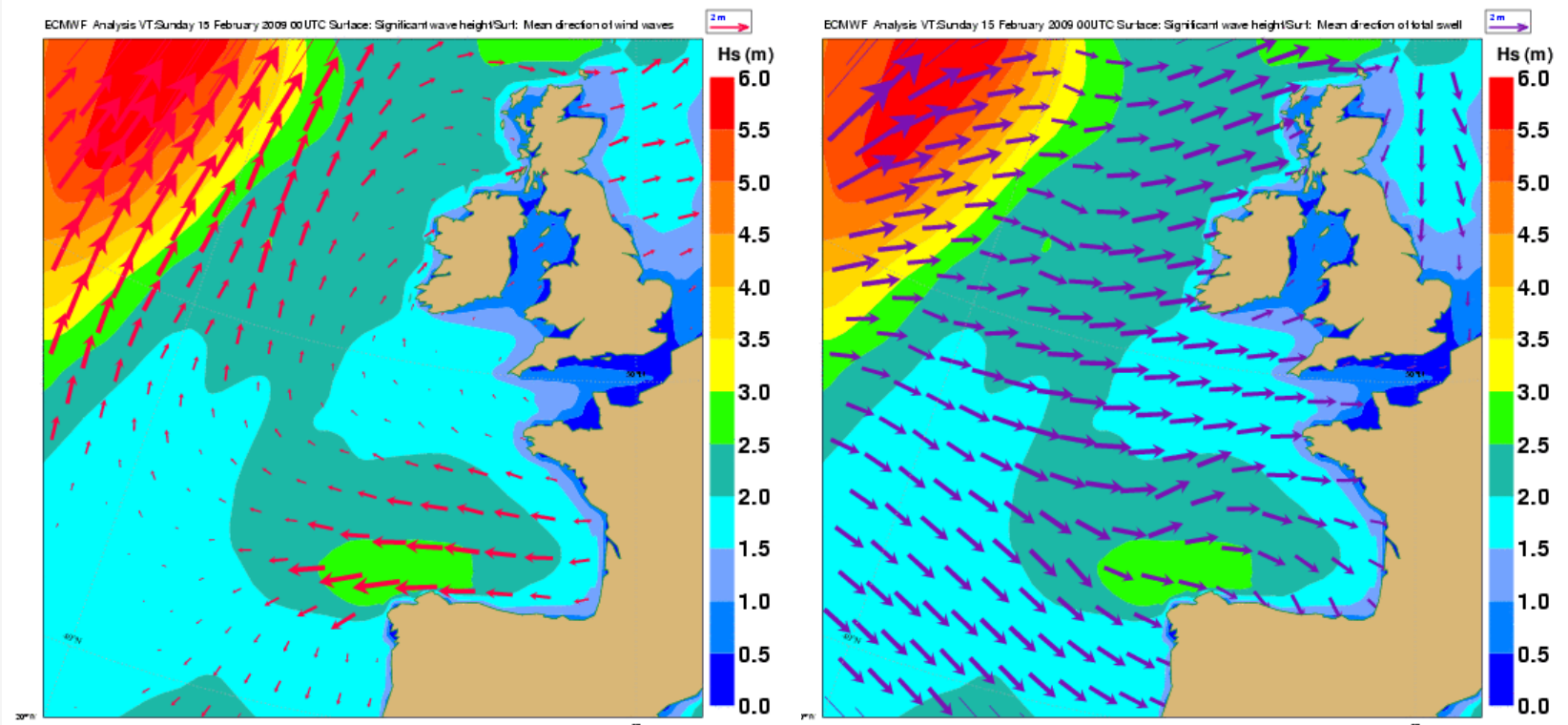
Situation might be more complicated:



Wave height and mean direction:
Analysis : 15 February 2009, 00 UTC

Wave Model Products

A scheme is used to split the global wave fields into waves which are under the direct influence of the forcing wind, the so-called **windsea** or wind waves, and those waves that are no longer bound to the forcing wind, generally referred to as **swell**. Period and mean direction are also determined for these split fields.

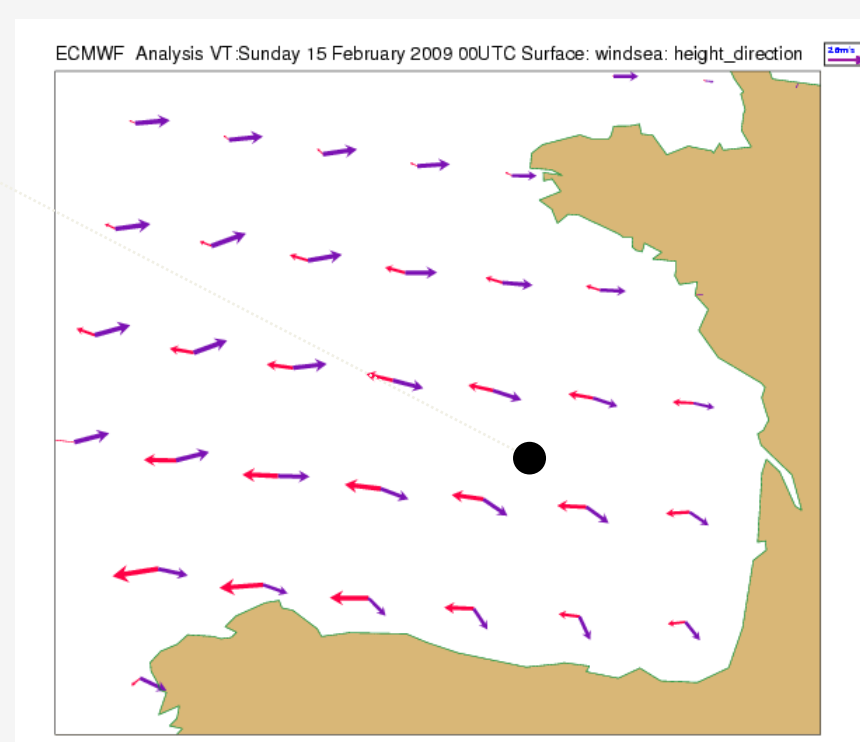
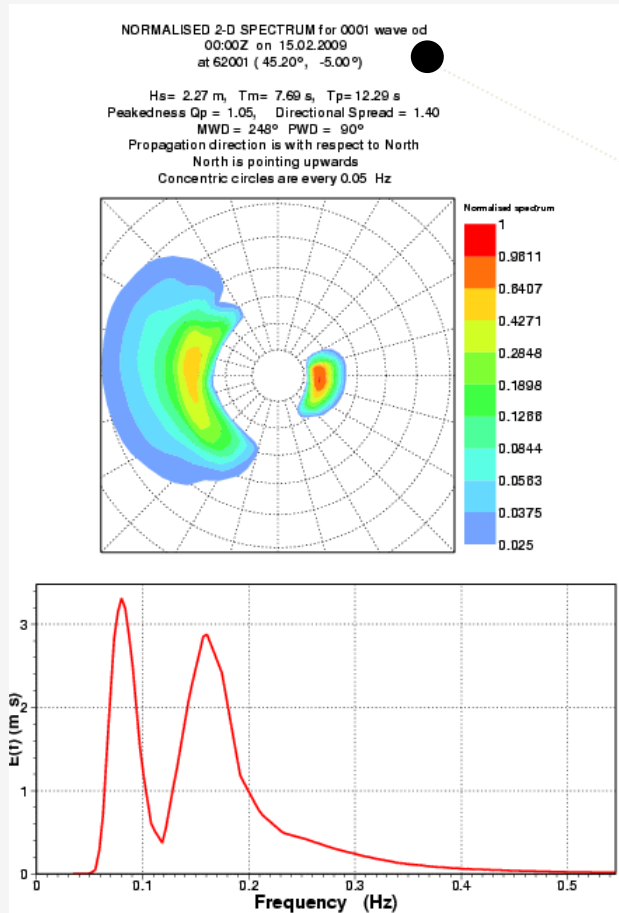


Wave height and **windsea** mean direction:
Analysis : 15 February 2009, 00 UTC

Wave height and **swell** mean direction:
Analysis : 15 February 2009, 00 UTC

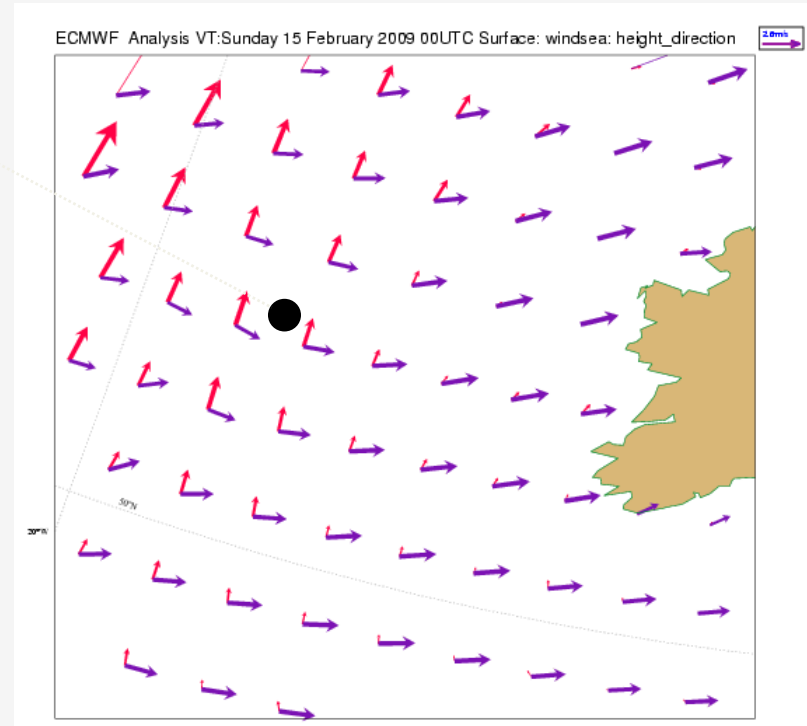
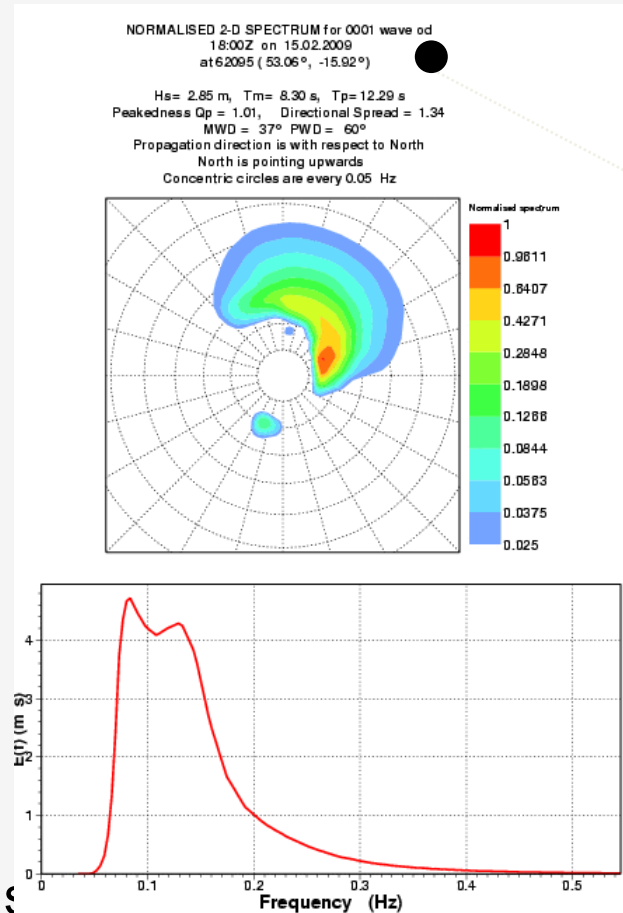
Wave Model Products

Windsea and swell: opposing sea

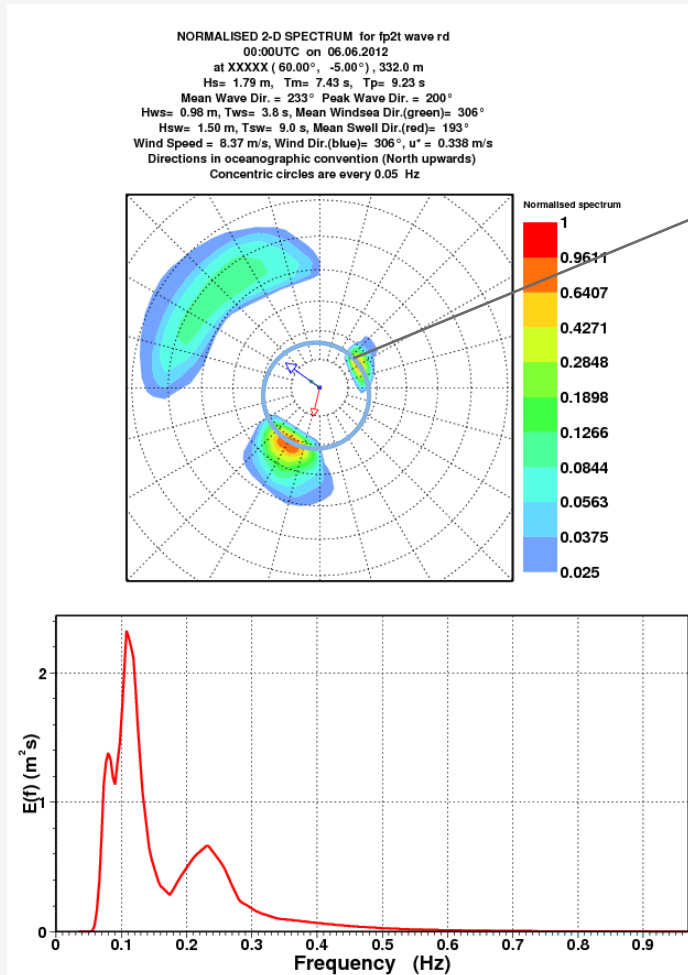


Wave Model Products

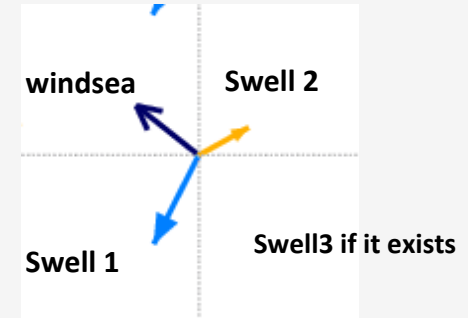
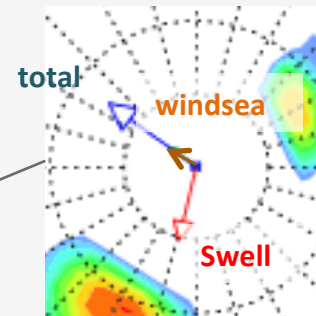
Windsea and swell: cross sea



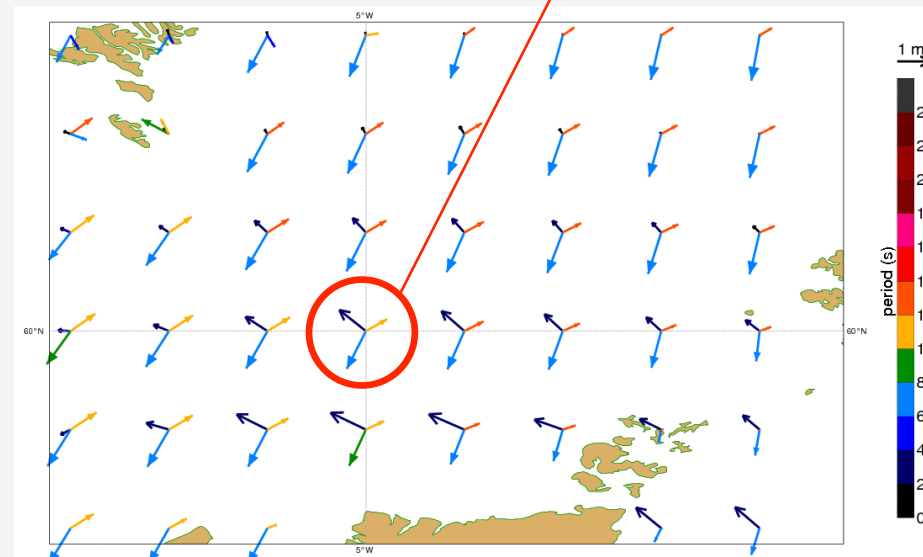
Since May 2015: spectral partitioning



Operational:



New decomposition:



Ocean wave forecasts

At the end of December 2013 and beginning of January 2014, the UK and western Europe were battered by large waves:



Ocean wave forecasts

Then again in February and early March:



May 1, 2013

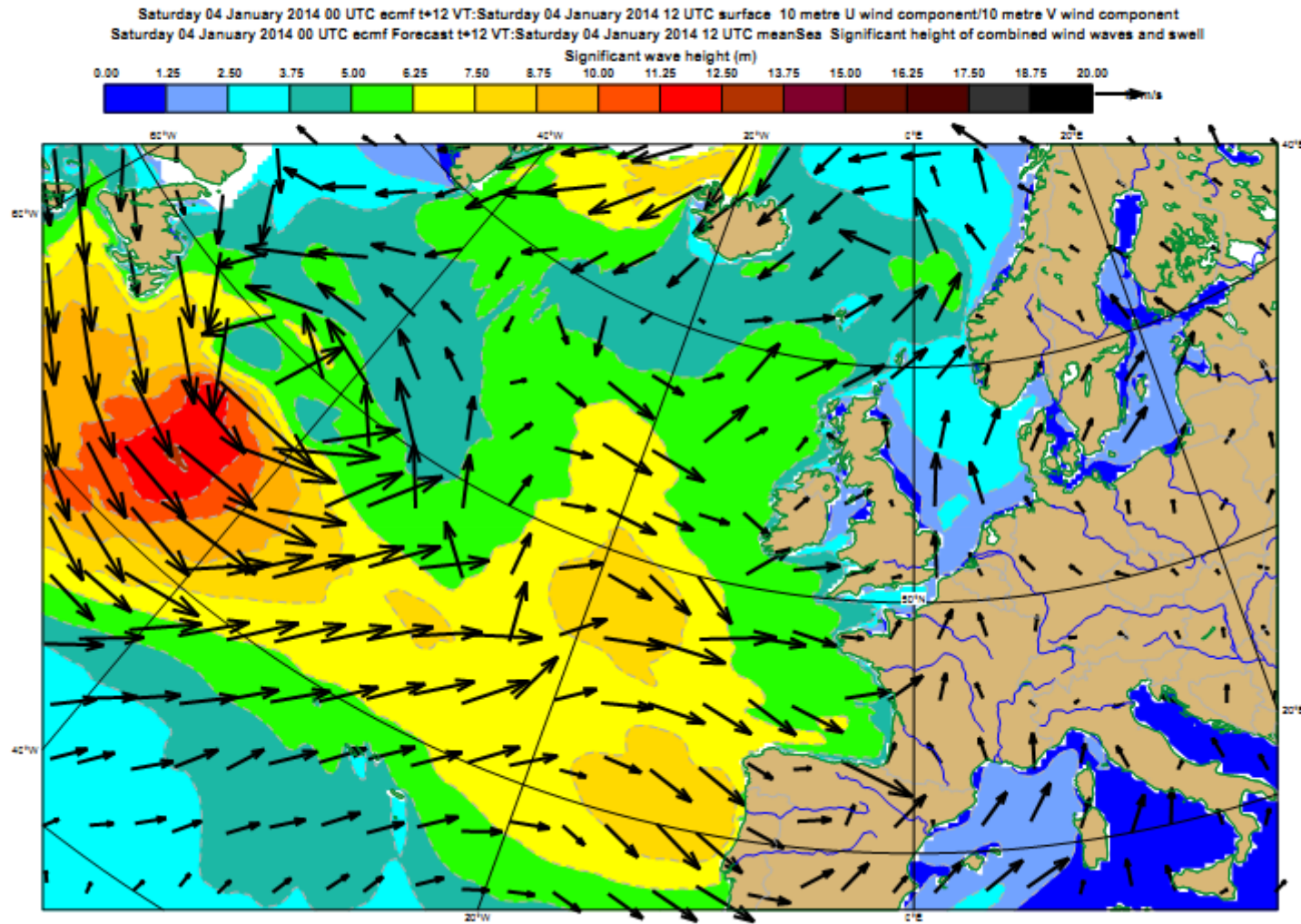
Porthleven Clock Tower, Cornwall



February 5, 2014

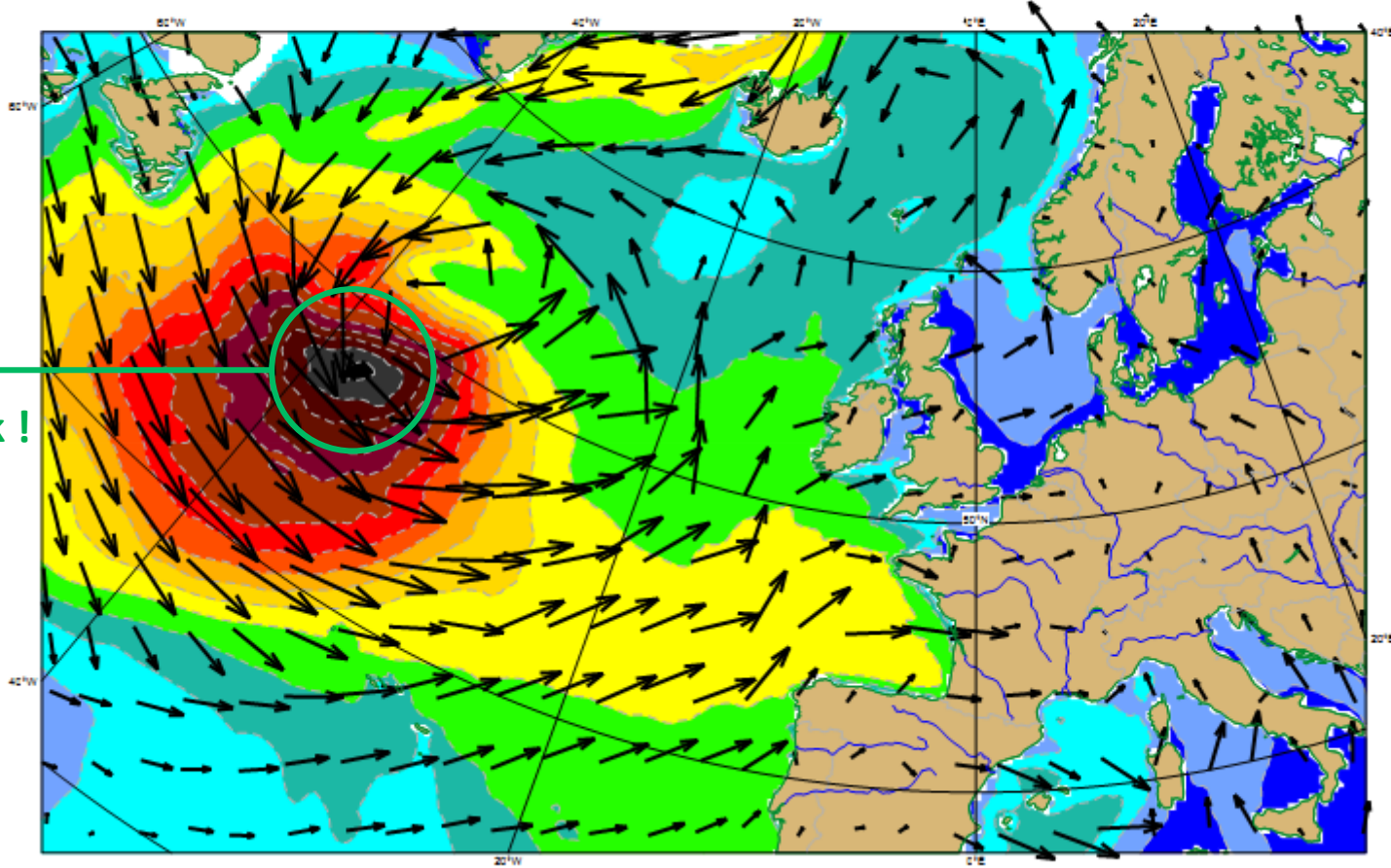
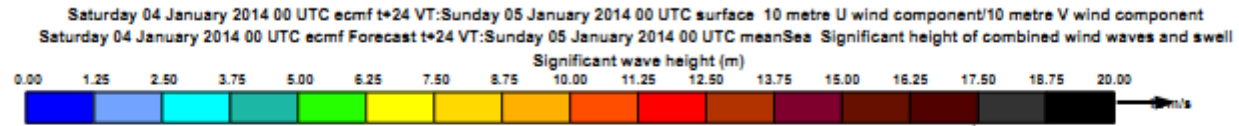
Ocean wave forecasts

Wave height forecast and wind from 4 January 2014, step 12 hours



Ocean wave forecasts

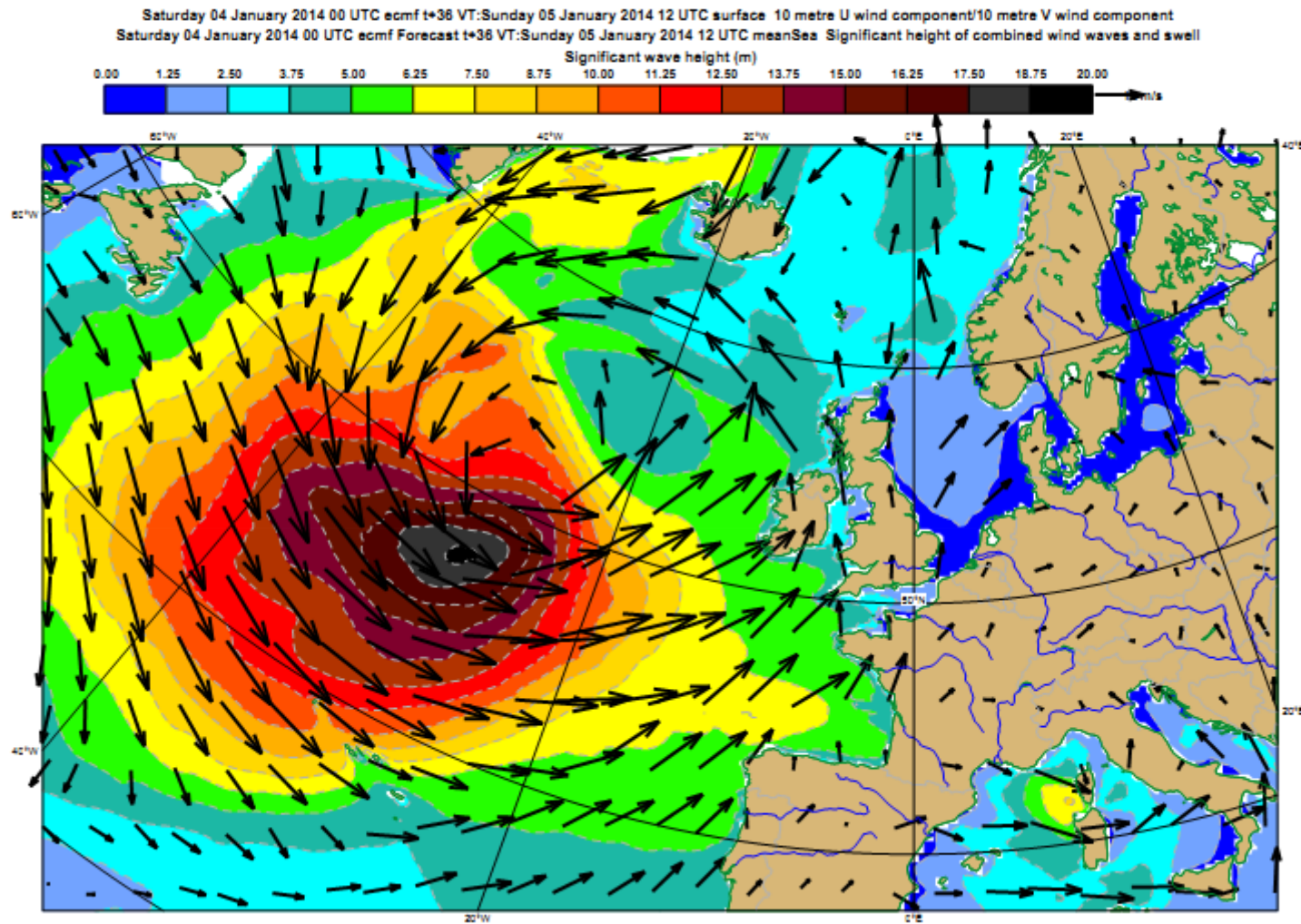
Wave height forecast and wind from 4 January 2014, step 24 hours



Nearing
20m
at its peak !

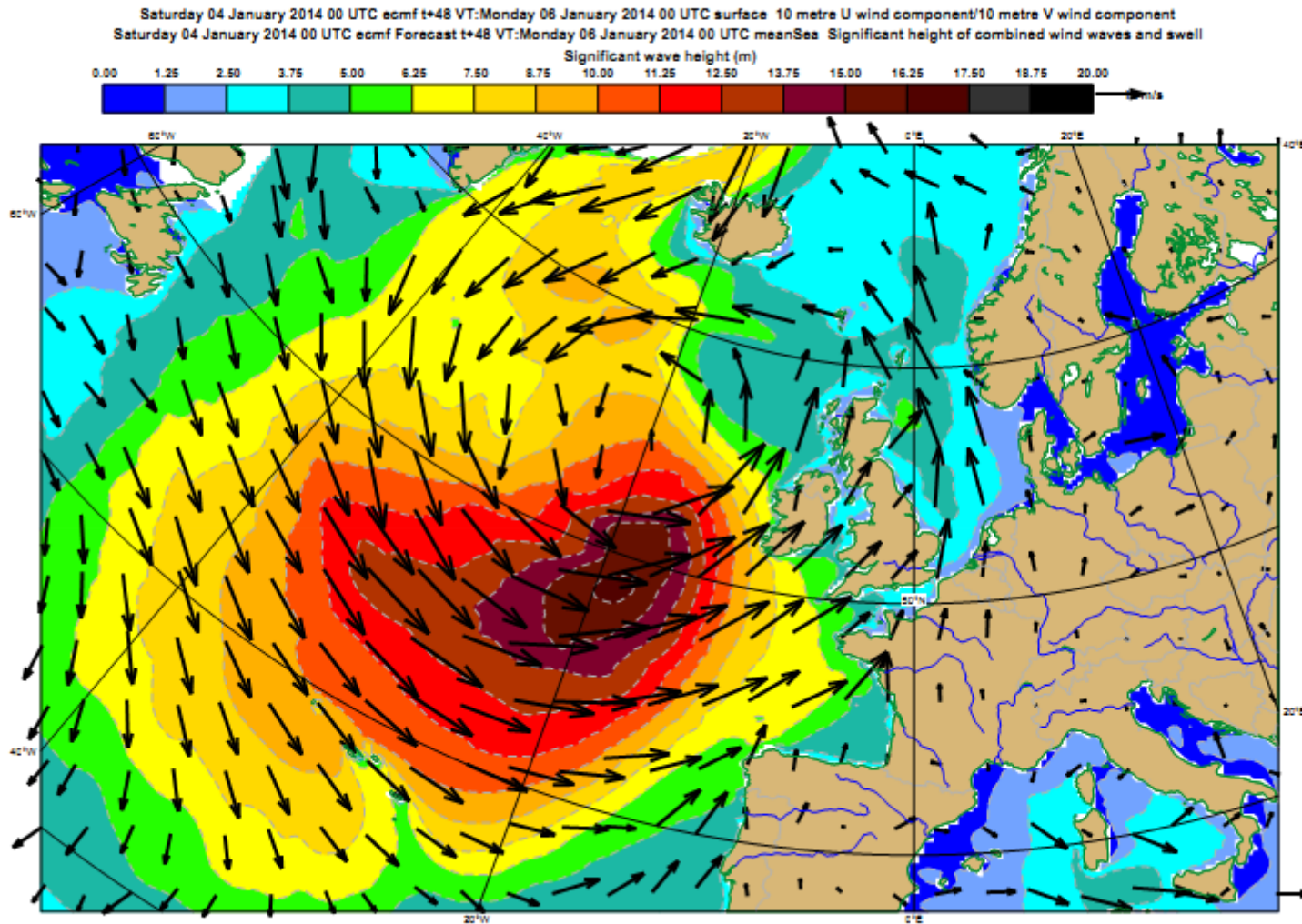
Ocean wave forecasts

Wave height forecast and wind from 4 January 2014, step 36 hours



Ocean wave forecasts

Wave height forecast and wind from 4 January 2014, step 48 hours



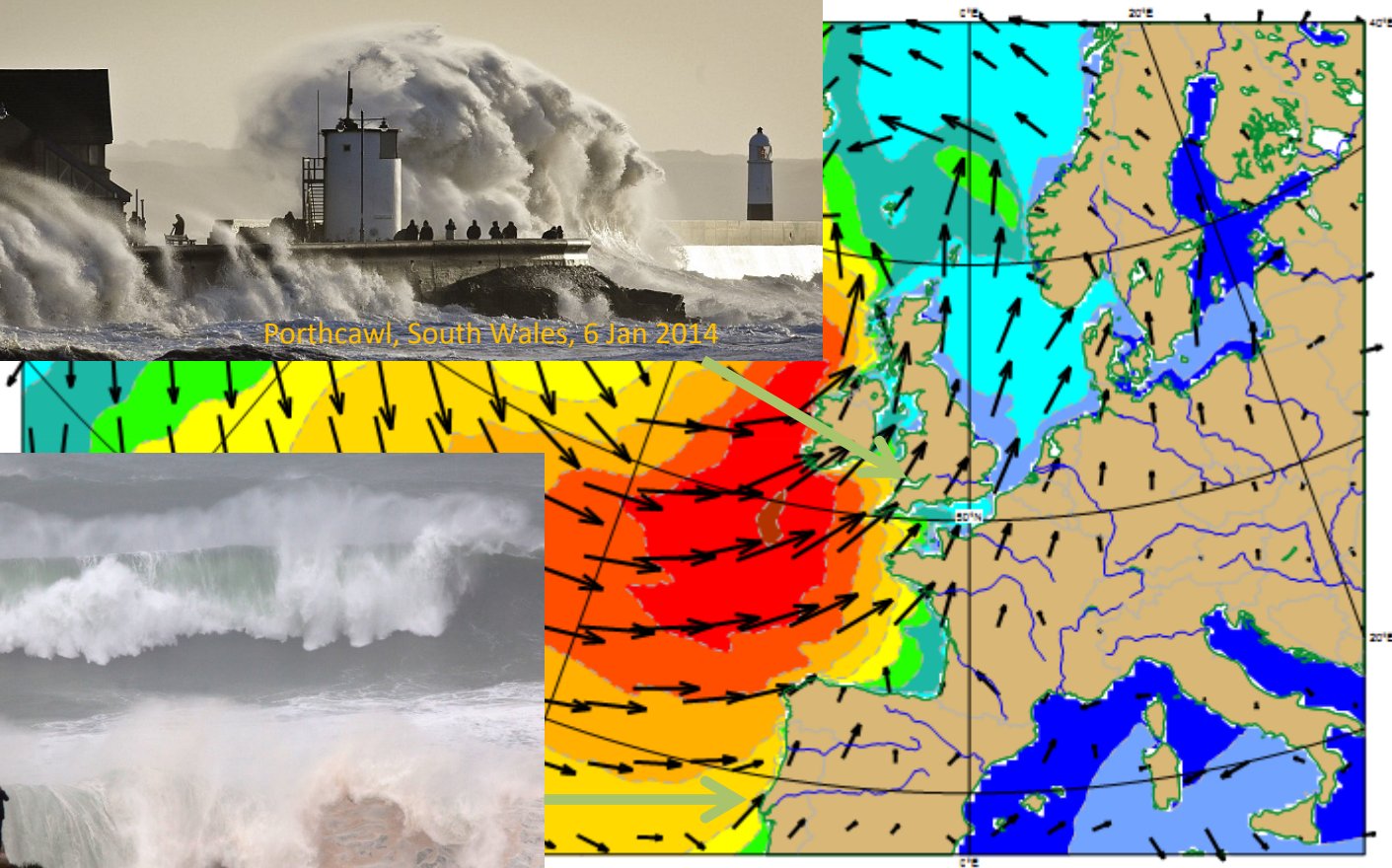
Ocean wave forecasts

Wave height forecast and wind from 4 January 2014, step 60 hours

Saturday 04 January 2014 00 UTC ecmf t+60 VT: Monday 06 January 2014 12 UTC surface 10 metre U wind component/10 metre V wind component
Saturday 04 January 2014 00 UTC ecmf Forecast t+60 VT: Monday 06 January 2014 12 UTC meanSea Significant height of combined wind waves and swell
Significant wave height (m)

0.00	1.25	2.50	3.75	5.00	6.25	7.50	8.75	10.00	11.25	12.50	13.75	15.00	16.25	17.50	18.75	20.00
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→ m/s



Long swell forecasts

Swell are long waves propagating away from storms.

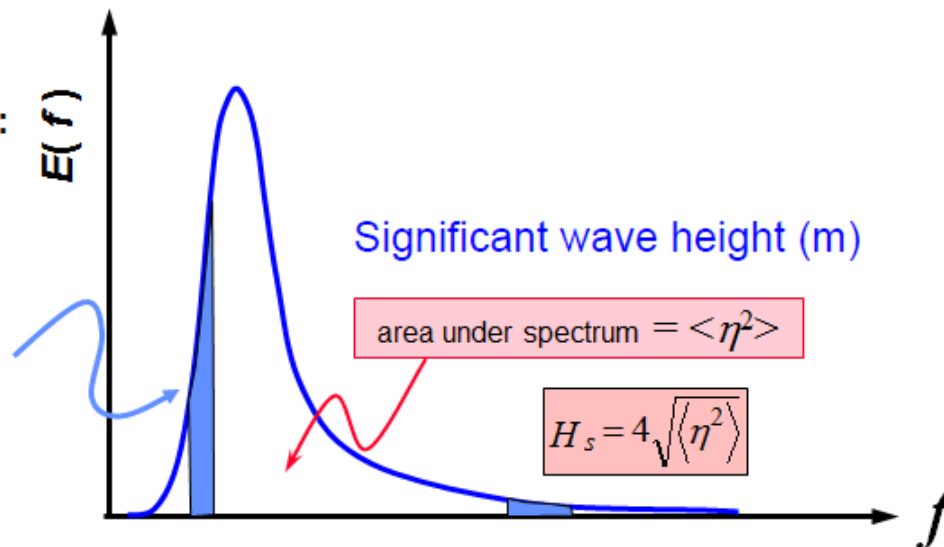
It is possible to follow the evolution of the swell.

Define the Equivalent Wave Height:

EWH,
Equivalent Wave Height
for a given frequency bin:

$$EHW = 4\sqrt{A}$$

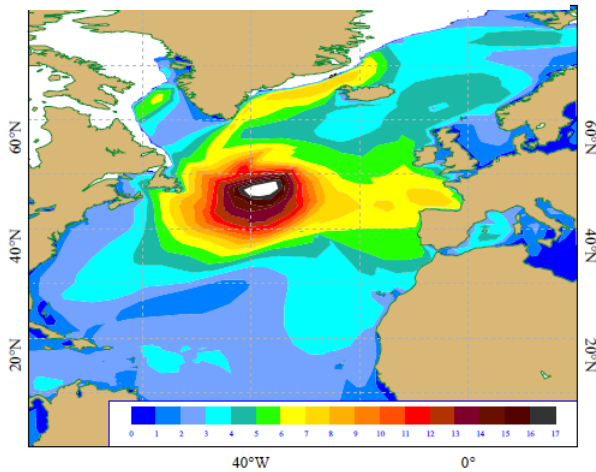
where A is the
area under curve for
a given frequency bin



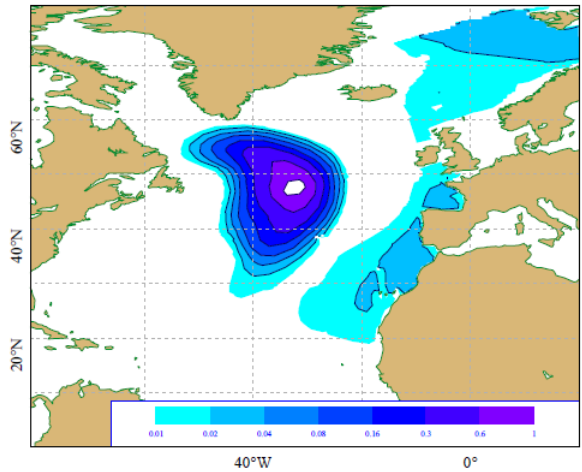
Long swell forecasts

Wave height and long swell forecast from 4 January 2014, step 24

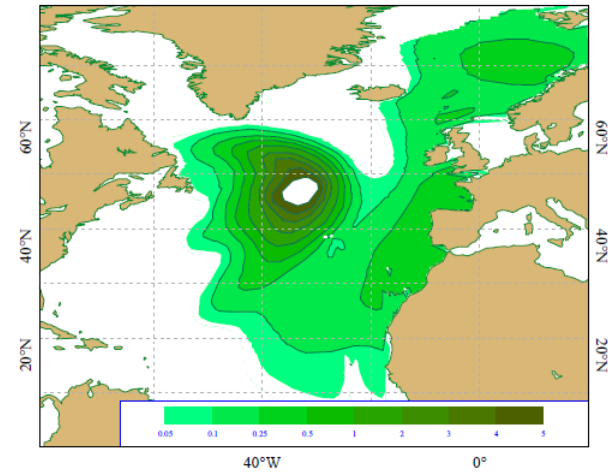
Significant wave height (m)



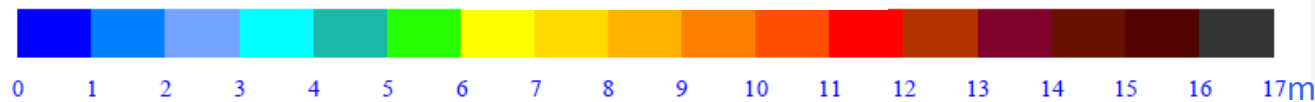
Wave energy in terms of wave height for waves with periods between 25 and 29 sec. (1000 to 1300 m wavelength)



Wave energy in terms of wave height for waves with periods between 21 and 25 sec. (700 to 1000 m wavelength)



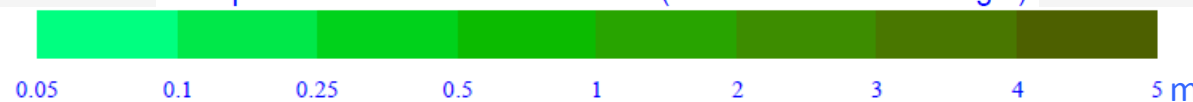
Significant wave height (m)



Wave energy in terms of wave height for waves with periods between 25 and 29 sec. (1000 to 1300 m wavelength)



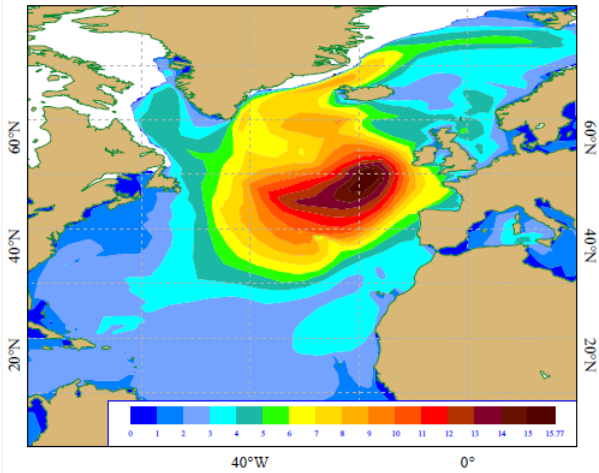
Wave energy in terms of wave height for waves with periods between 21 and 25 sec. (700 to 1000 m wavelength)



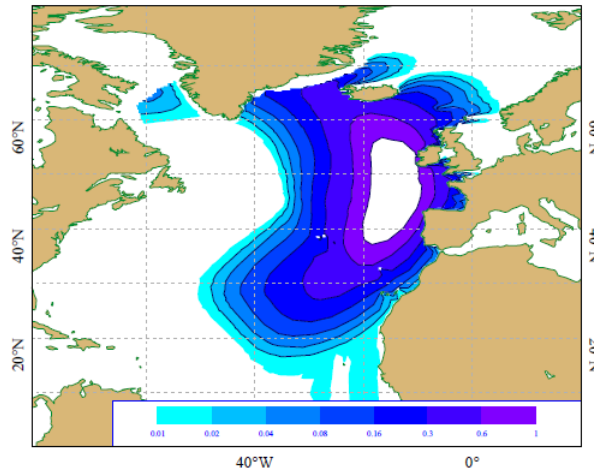
Long swell forecasts

Wave height and long swell forecast from 4 January 2014, step 48

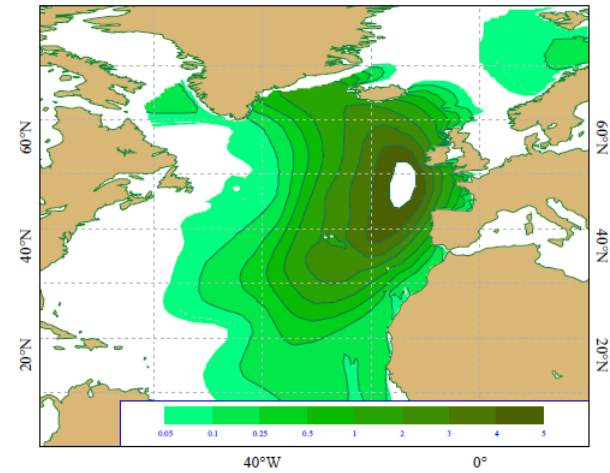
Significant wave height (m)



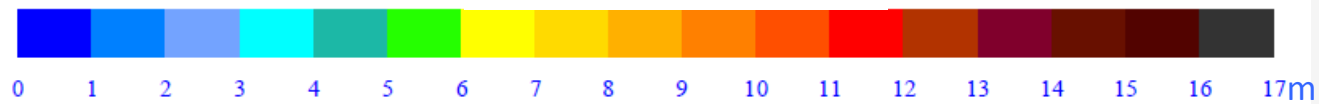
Wave energy in terms of wave height for waves with periods between 25 and 29 sec. (1000 to 1300 m wavelength)



Wave energy in terms of wave height for waves with periods between 21 and 25 sec. (700 to 1000 m wavelength)



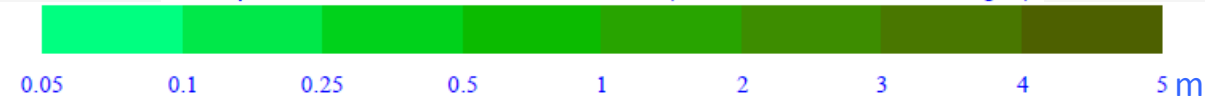
Significant wave height (m)



Wave energy in terms of wave height for waves with periods between 25 and 29 sec. (1000 to 1300 m wavelength)



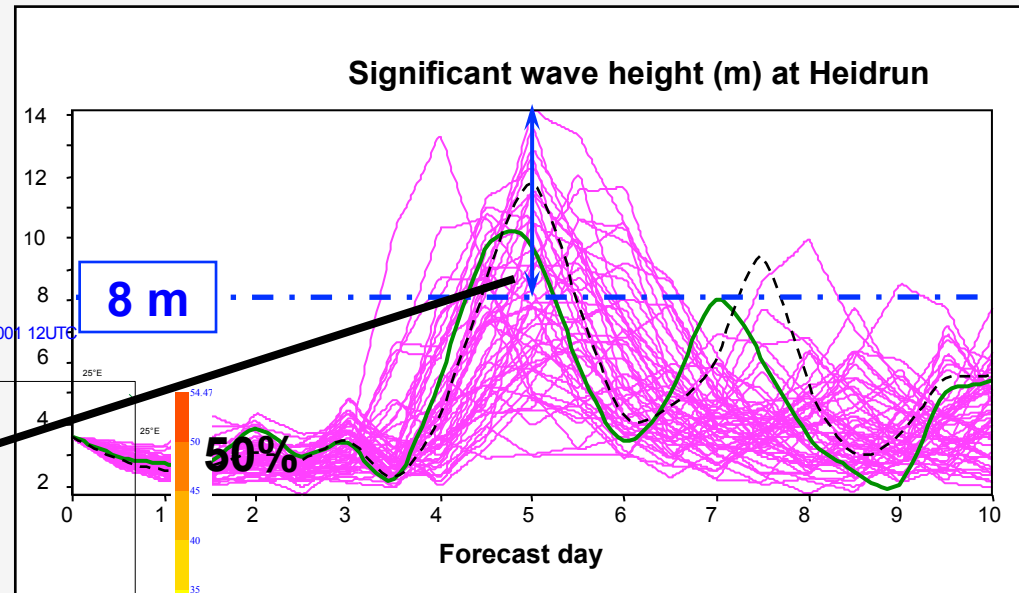
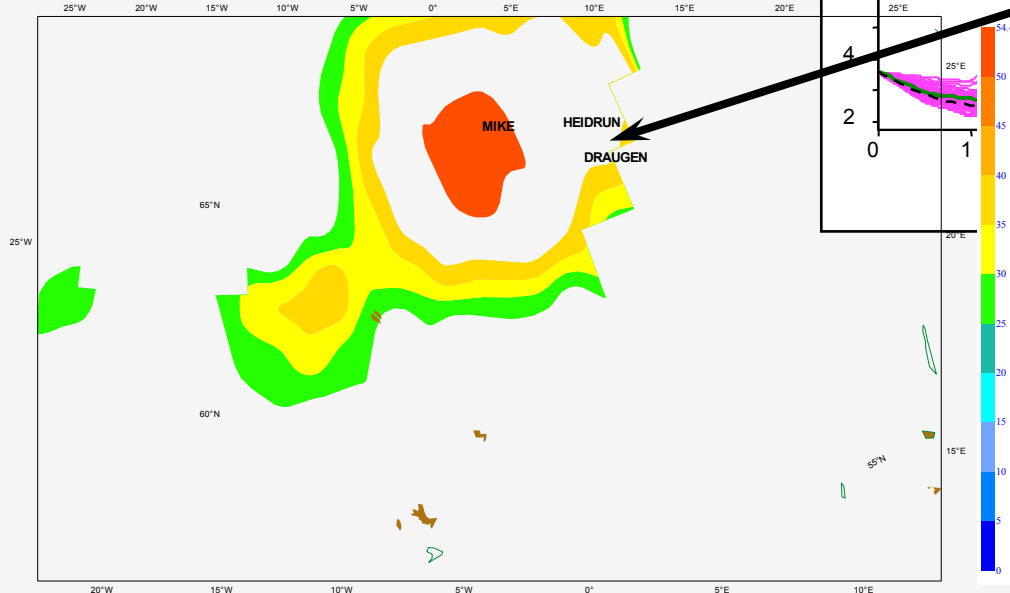
Wave energy in terms of wave height for waves with periods between 21 and 25 sec. (700 to 1000 m wavelength)



A more 'classic' use of the EPS:

From an ensemble of wave forecasts it is possible to derive probabilities for certain wave conditions.

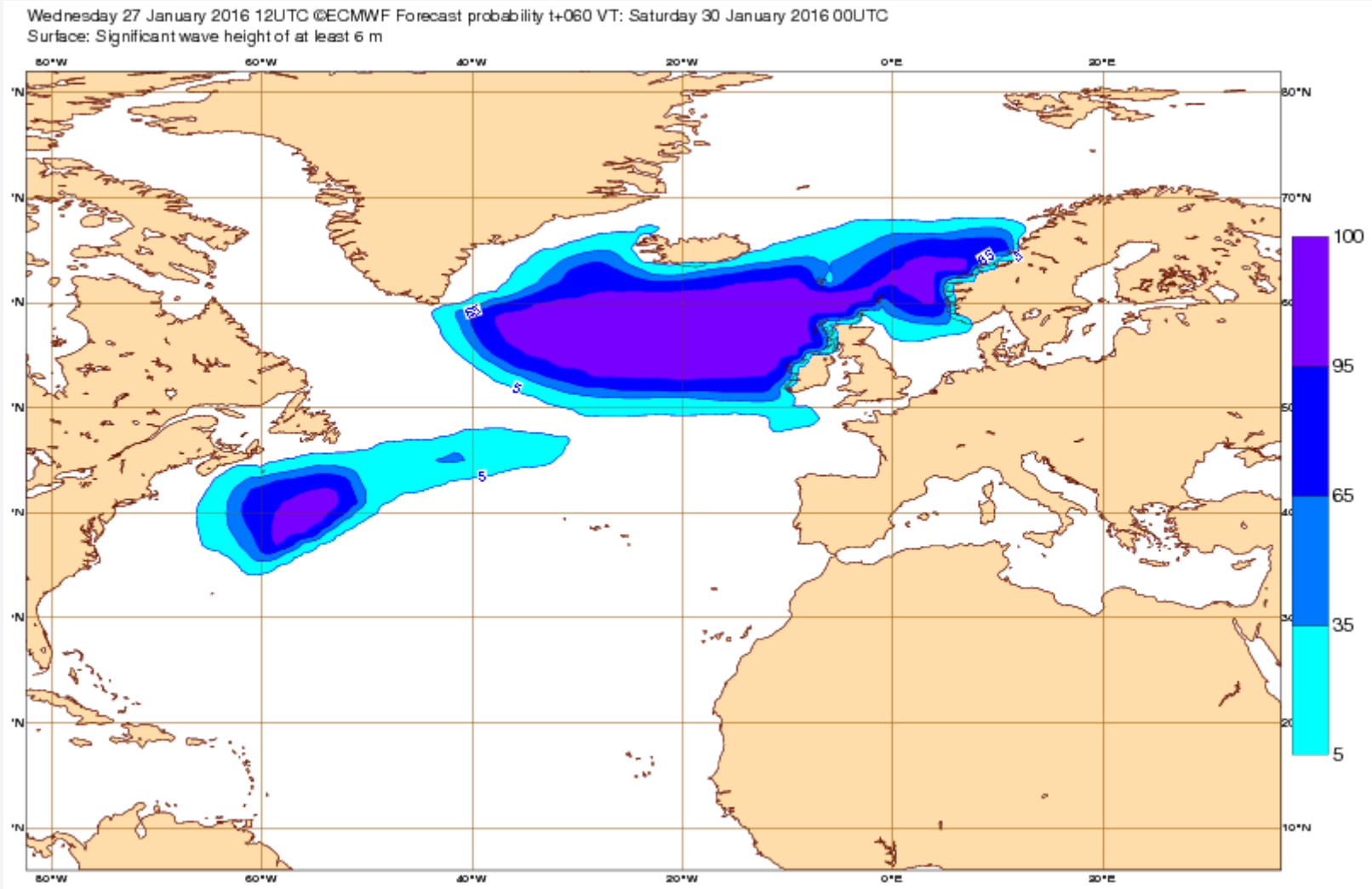
Tuesday 6 November 2001 12UTC ECMWF EPS Probability Forecast t+120 VT: Sunday 11 November 2001 12UTC
Surface: significant wave height probability >8



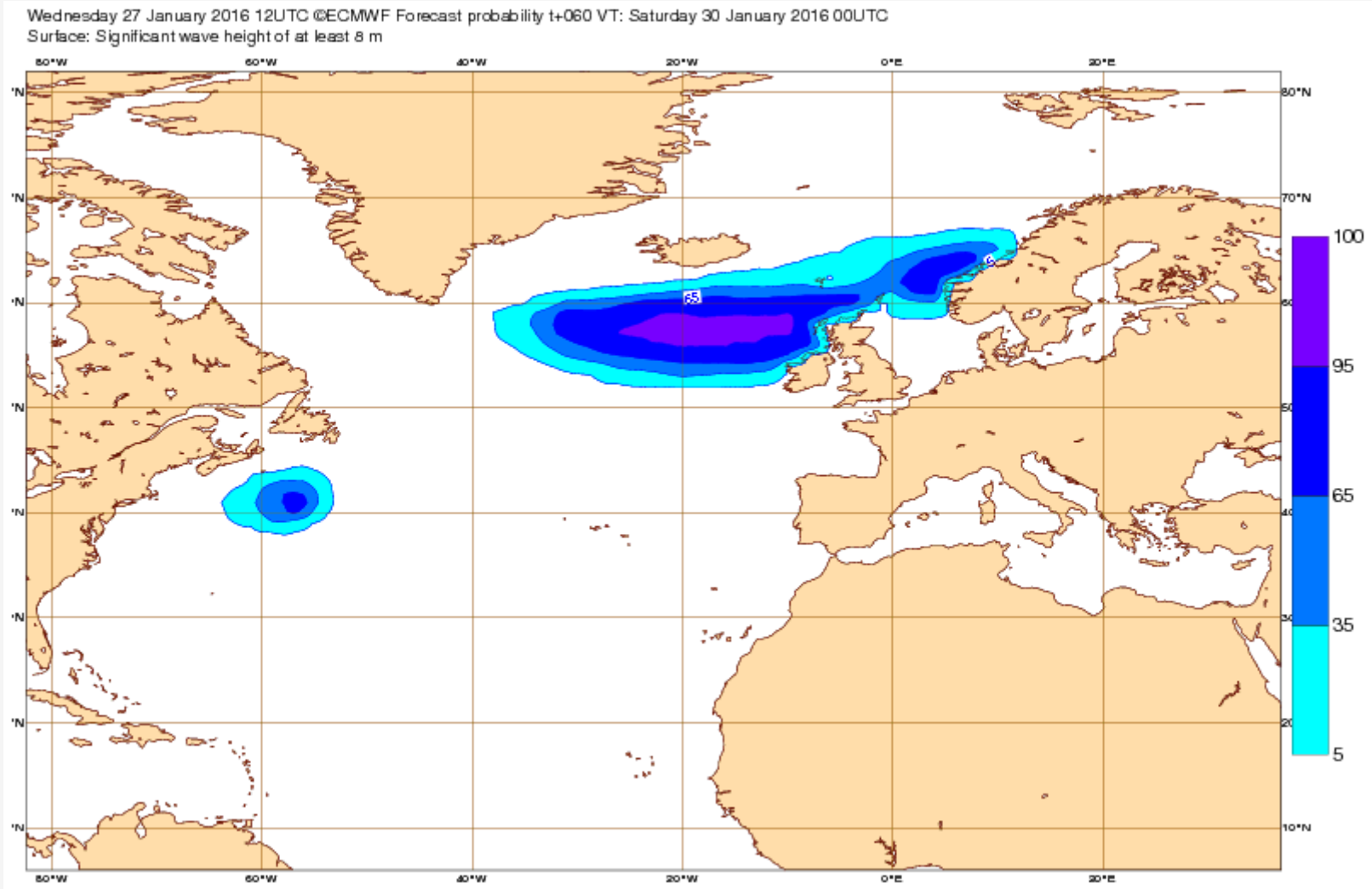
06 Nov. 2001 12 UTC ECMWF EPS probability forecast t+120

Significant wave height above 8 m

Basic EPS Wave Model Products



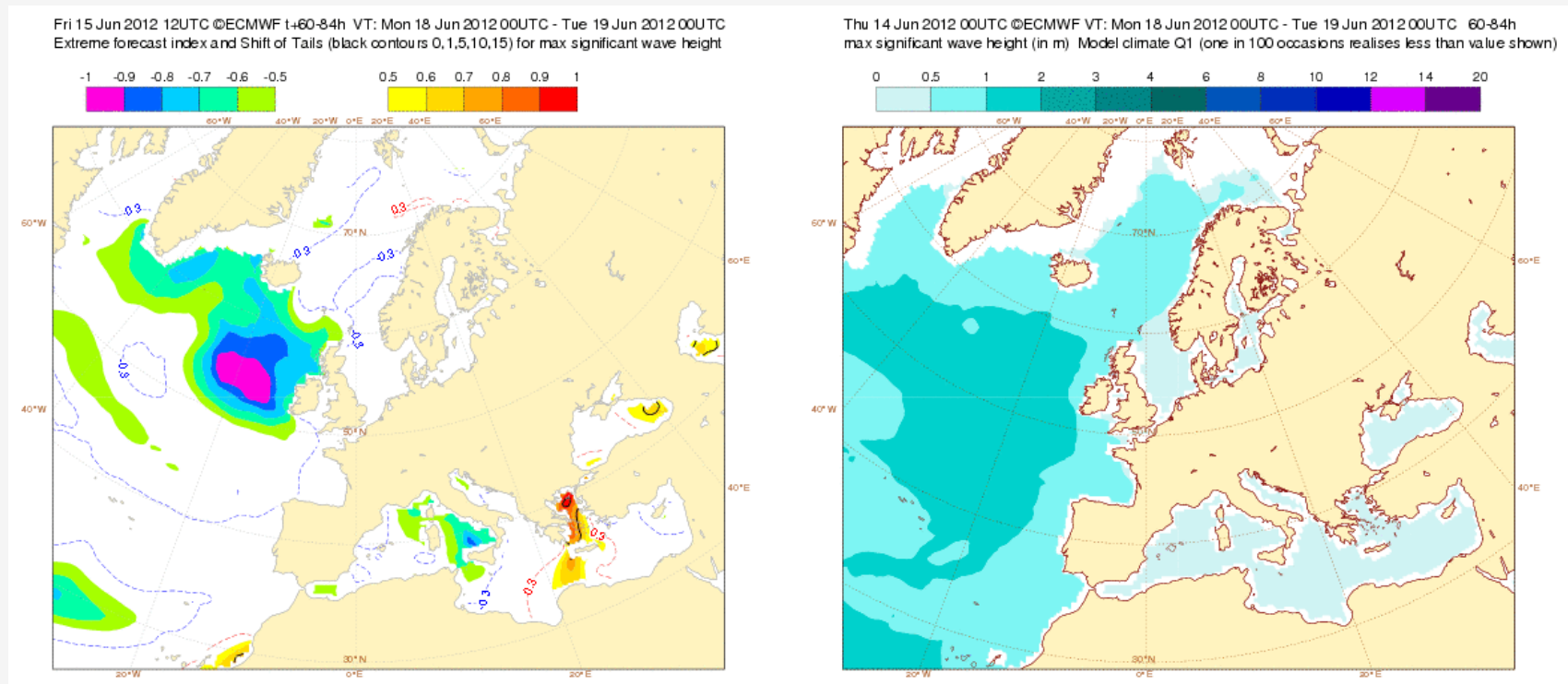
Basic EPS Wave Model Products



EFI plots

From the new model climate, it is possible to derive indices that indicate deviations in probabilistic terms from what is 'expected'.

Extreme Forecast Index (EFI): -1 means that all EPS are below climate.



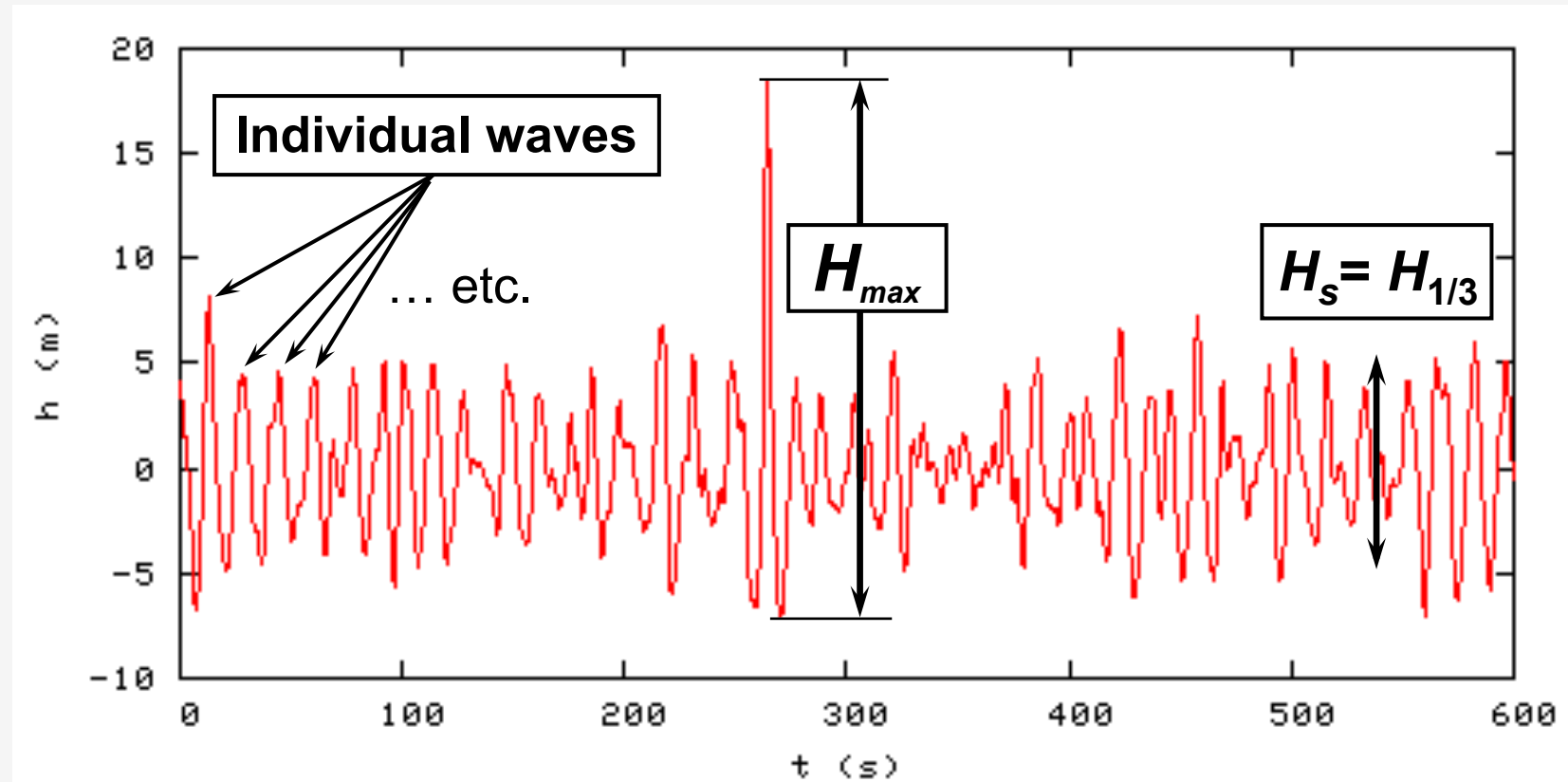
EFI for significant wave height

01 percentile of the distribution for significant wave height

We are not always dealing with nice 'predictable' waves:



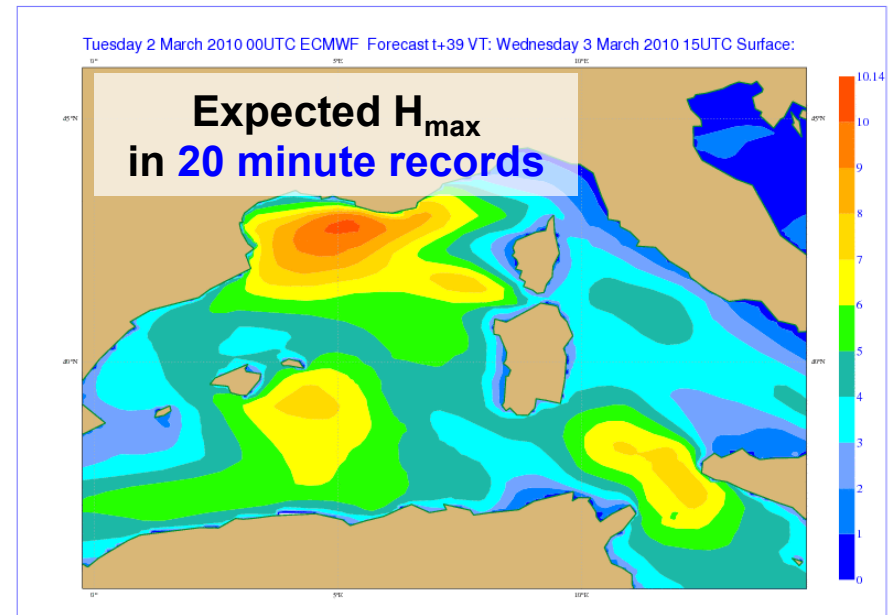
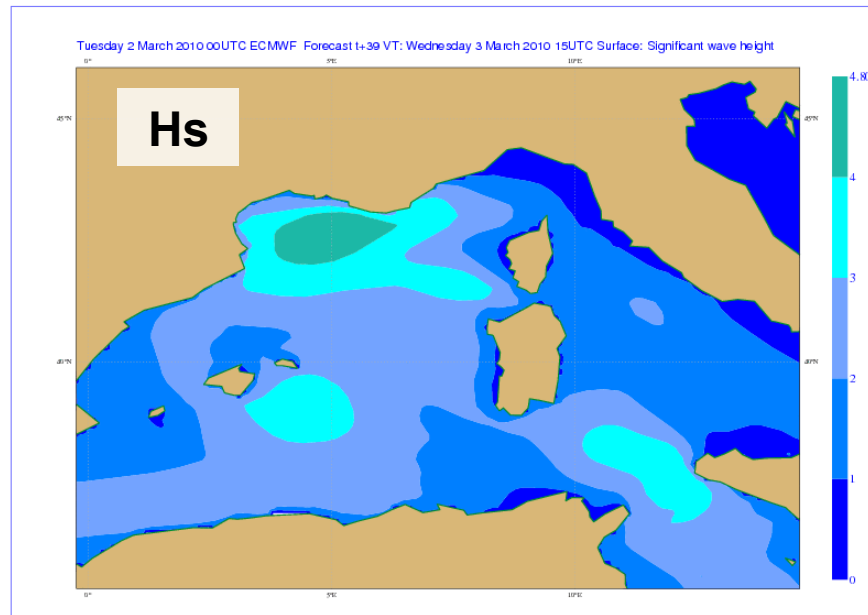
Individual Waves,
Significant Wave Height, H_s ,
Maximum Individual Wave Height, H_{max} , and
Freak Wave



If $H_{max} > 2.2 H_s \rightarrow$ freak wave event

Wave Model Products: Extreme Waves

We have a parameter to estimate the height of the **highest individual wave** (H_{\max}) one can expect. Its value can be derived from the 2d wave spectrum:



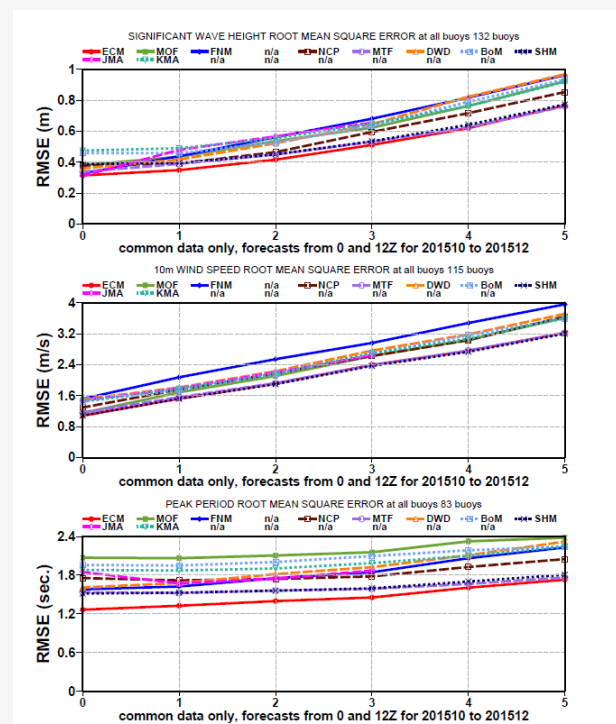
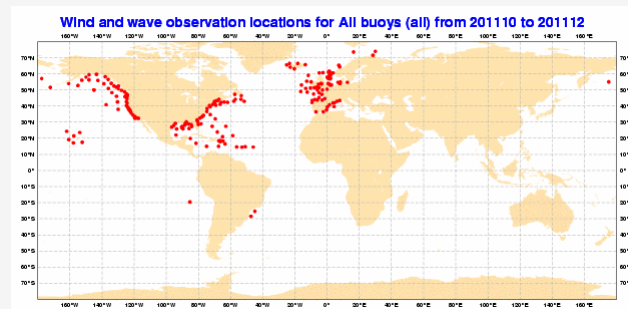
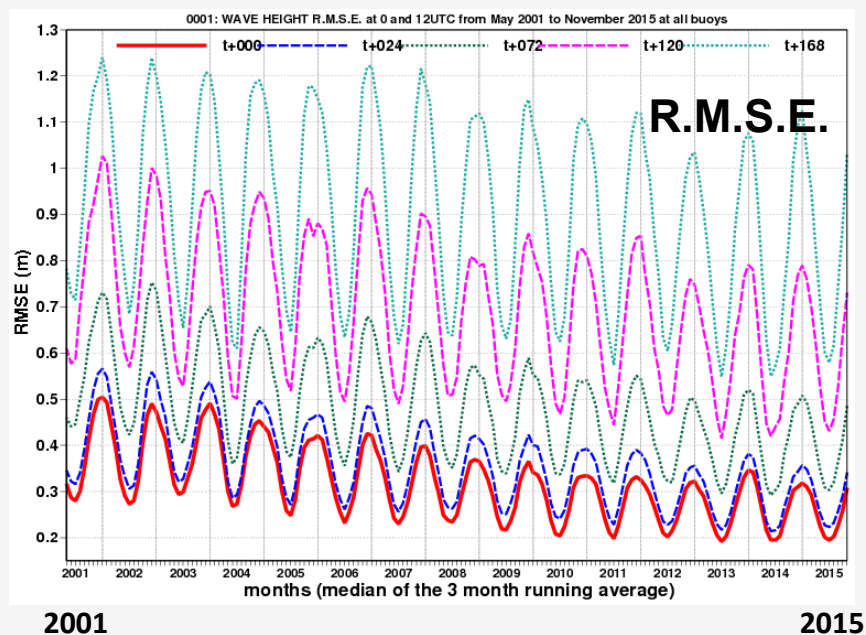
March 3, 2010, 15UTC

Forecasts fields from Friday 2 March, 2010, 0 UTC

Continued general improvement of model forecasts

For example: ECMWF forecast wave height against buoy measurements:

Home -> Forecasts -> Charts -> Verifications -> Wave Products Comparison



See also the Wave Forecast Verification Project maintained on behalf of the Expert Team on Waves and Storm Surges of the WMO-IOC Joint Technical Commission for Oceanography and Marine Meteorology (JCOMM)

http://www.jcomm.info/index.php?option=com_content&task=view&id=131&Itemid=37

Questions ?