

# Introduction to the parameterization of sub-grid processes

Anton Beljaars

([anton.beljaars@ecmwf.int](mailto:anton.beljaars@ecmwf.int) room 016)

- What is parameterization?
- Processes, importance and impact.
- Testing, validation, diagnostics
- Parameterization development strategy

# Why parameterization

- Due to limited resolution, small scale processes are not resolved by large scale models and are **sub-grid**
- The **effect** of the sub-grid process on the large scale can only be represented statistically
- The procedure of expressing the effect of the sub-grid process on the resolved variables is called **parameterization**

# What is parametrization and why is it needed

- The standard Reynolds decomposition and averaging, leads to covariances that need “closure” or “parameterization”
  - Radiation absorbed, scattered and emitted by molecules, aerosols and cloud droplets play an important role in the atmosphere and need parameterization
  - Cloud microphysical processes need “parameterization”
- 
- Parameterization schemes express the effect of sub-grid processes in resolved variables
  - Model variables are  $U, V, T, q, (l, i, a, P_l, P_s)$

# Reynolds decomposition

e.g. equation for potential temperature:

$$\frac{\partial \Theta}{\partial t} + \underbrace{u \frac{\partial \Theta}{\partial x} + v \frac{\partial \Theta}{\partial y} + w \frac{\partial \Theta}{\partial z}}_{\text{advection}} = \underbrace{Q}_{\text{source}} + \underbrace{\lambda \left( \frac{\partial^2 \Theta}{\partial x^2} + \frac{\partial^2 \Theta}{\partial y^2} + \frac{\partial^2 \Theta}{\partial z^2} \right)}_{\text{molecular diffusion}}$$

**Reynolds decomposition:**  $U = u + u', \quad V = v + v',$   
 $W = w + w', \quad \Theta = \theta + \theta'.$

**Averaged (e.g. over grid box):**

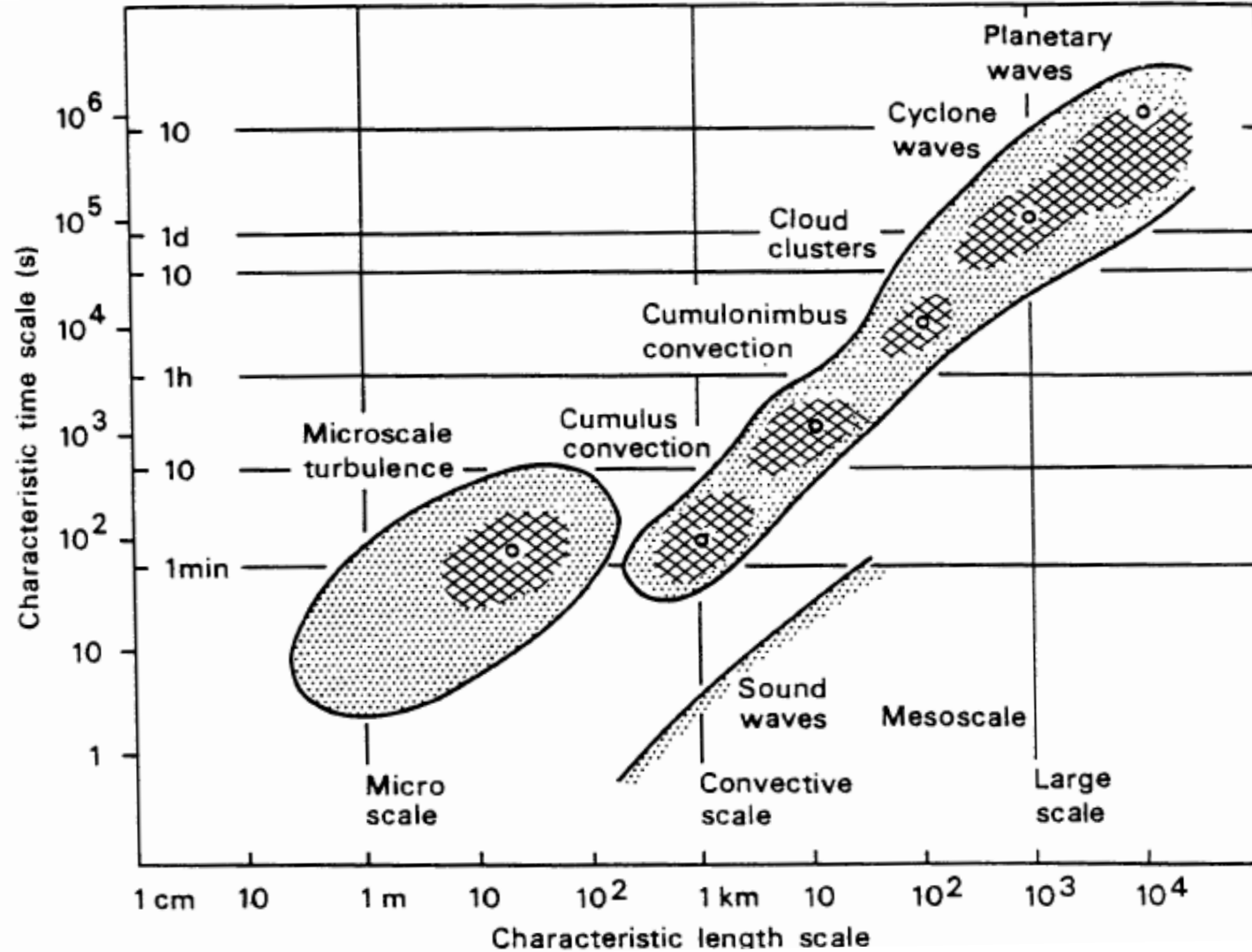
$$\frac{\partial \theta}{\partial t} + u \frac{\partial \theta}{\partial x} + v \frac{\partial \theta}{\partial y} + w \frac{\partial \theta}{\partial z} =$$

$$Q + \frac{\partial}{\partial x} \left( -\overline{u'\theta'} + \lambda \frac{\partial \theta}{\partial x} \right) + \frac{\partial}{\partial y} \left( -\overline{v'\theta'} + \lambda \frac{\partial \theta}{\partial y} \right) + \frac{\partial}{\partial z} \left( -\overline{w'\theta'} + \lambda \frac{\partial \theta}{\partial z} \right)$$

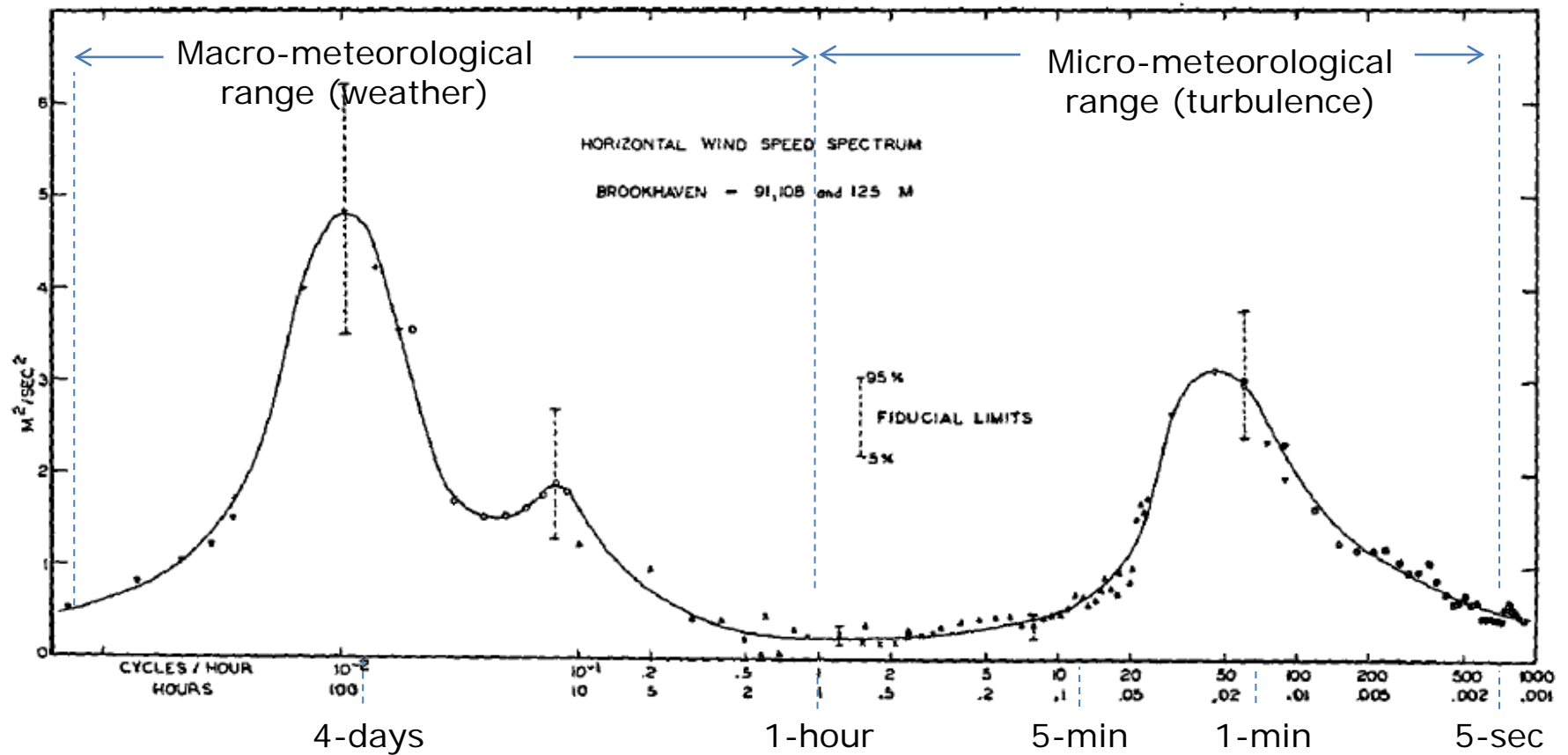
$Q$  : source term (e.g. radiation absorption/emission or condensation)

$\overline{w'\theta'}$  : sub-grid (Reynolds) transport term (e.g. due to turbulence, convection)

# Space and time scales



# Space and time scales



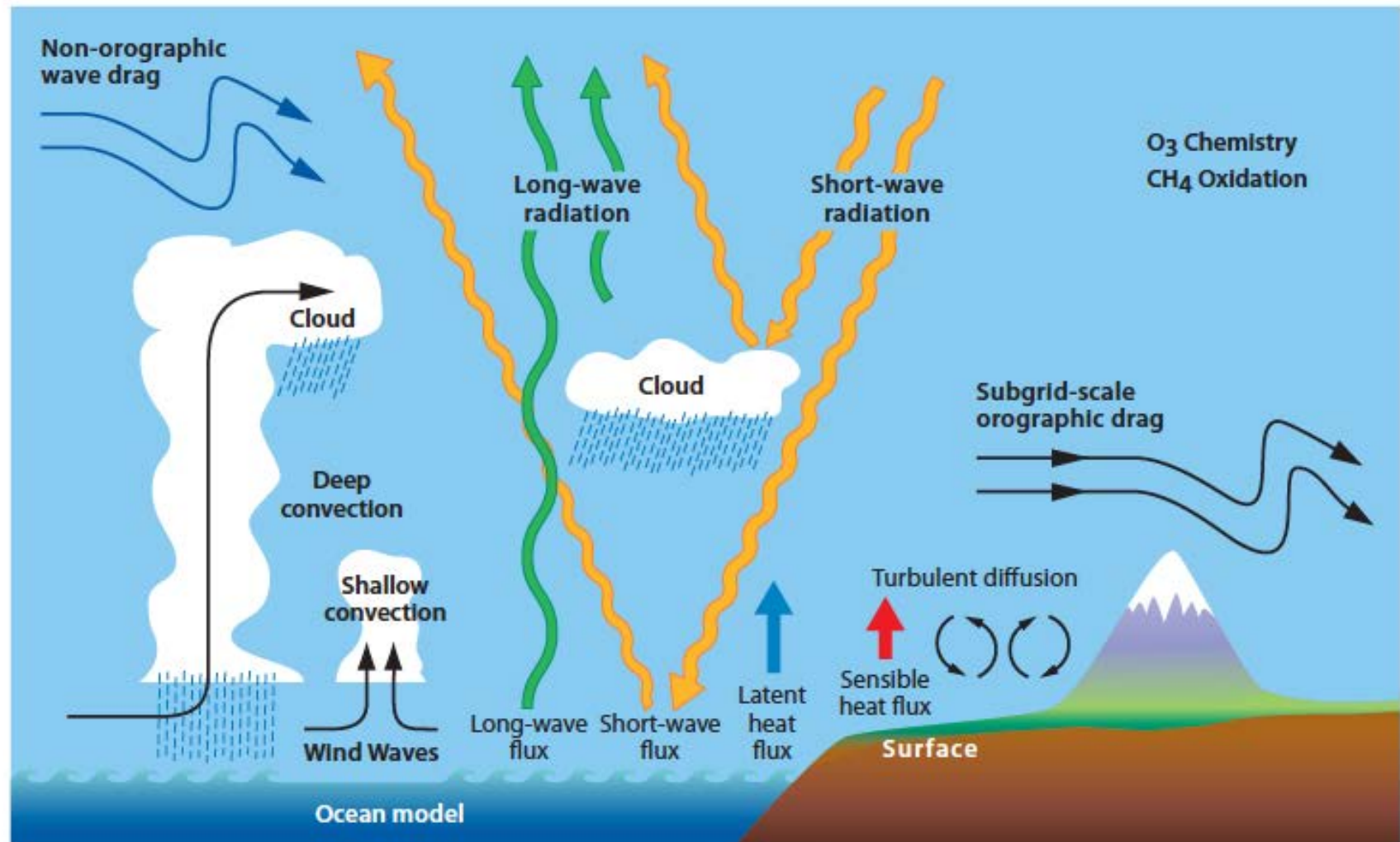
Horizontal wind speed spectrum at Brookhaven at  $z=100m$  (van der Hoven, 1957)

# Numerical models of the atmosphere

	Vert. Scales	time range	Hor. scales
• Climate models	100 km	400 m	100 years
• Global weather prediction	15 km	200 m	10 days
• Limited area weather pred.	5 km	200 m	2 days
• Cloud resolving models	500 m	100 m	1 day
• Large eddy models	50 m	50 m	5 hours

**Different models need different level of parameterization**

# Parameterized processes in the ECMWF model





# Applications and requirements

- **Applications of the ECMWF model**

- Data assimilation T1279L137-outer and T95/T159/T255-inner loops: 12-hour 4DVAR.
- Medium range forecasts at T1279/L137 (16 km): 10 days from 00 and 12 UTC.
- Ensemble prediction system at T639L91 (32 km) for 10 days, and T319 (65 km) up to day 15; 2x(50+1) members.
- Short range at T1279L137 (15 km): 3 days, 4 times per day for LAMs.
- Seasonal forecasting at T255L91(80 km): 200 days ensembles coupled to ocean model.
- Monthly forecasts (ocean coupled) at T319L91: Twice a week, 50+1 members.
- Fully coupled ocean wave model.
- Interim reanalysis (1979-current) is ongoing (T255L60, 4DVAR).

- **Basic requirements**

- Accommodate different applications.
- Parameterization needs to work over a wide range of spatial resolutions.
- Time steps are long (from 10 to 40 minutes); Numerics needs to be efficient and robust.
- Interactions between processes are important and should be considered in the design of the schemes.

# Importance of physical processes

## •General

- Tendencies from sub-grid processes are substantial and contribute to the evolution of the atmosphere even in the short range.
- Diabatic processes drive the general circulation.

## •Synoptic development

- Diabatic heating and friction influence synoptic development.

## •Weather parameters

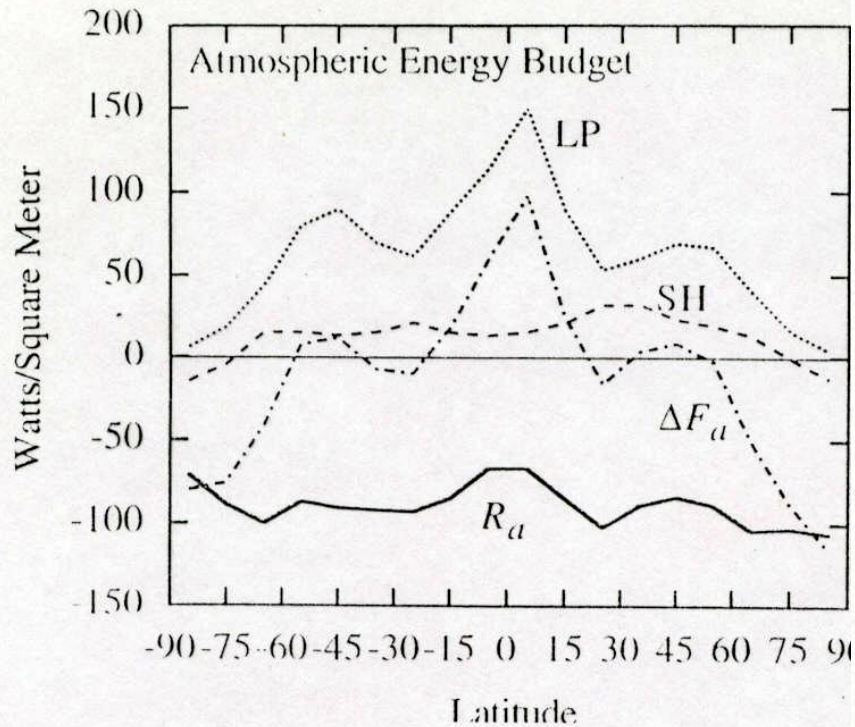
- Diurnal cycle
- Clouds, precipitation, fog
- Wind, gusts
- T and q at 2m level.

## •Data assimilation

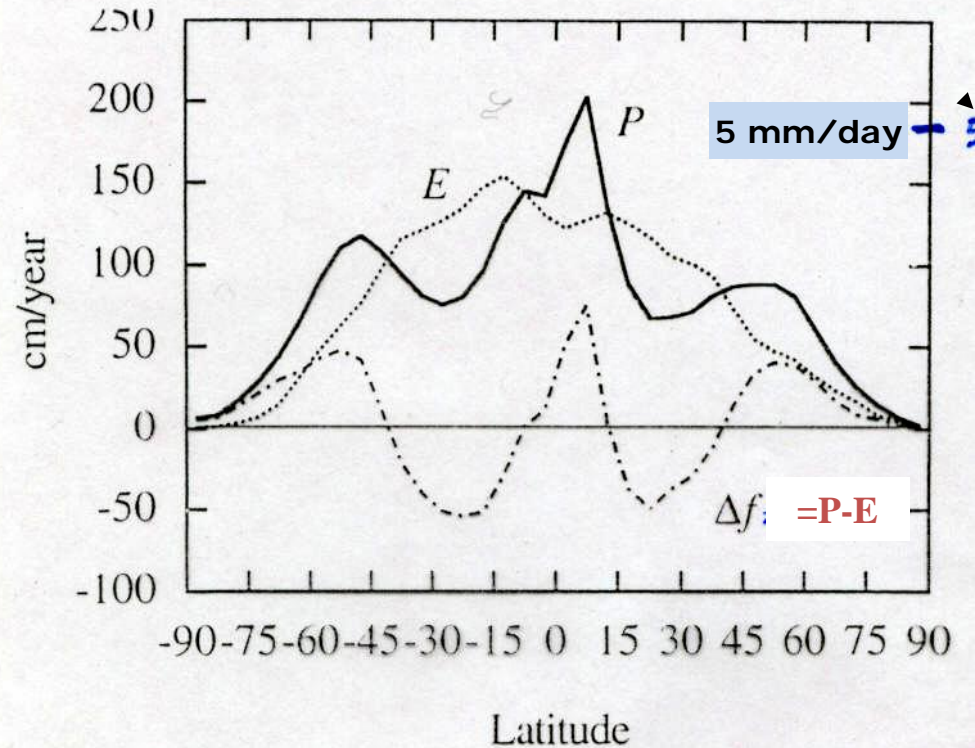
- Forward operators are needed for observations.

# Global energy and water budgets

## Energy



## Moisture



$$R_a + LP + SH = \Delta F_a$$

$R_a$  Net atmospheric radiative heating

$LP$  Heating due to latent heat release

$SH$  Surface sensible heat flux

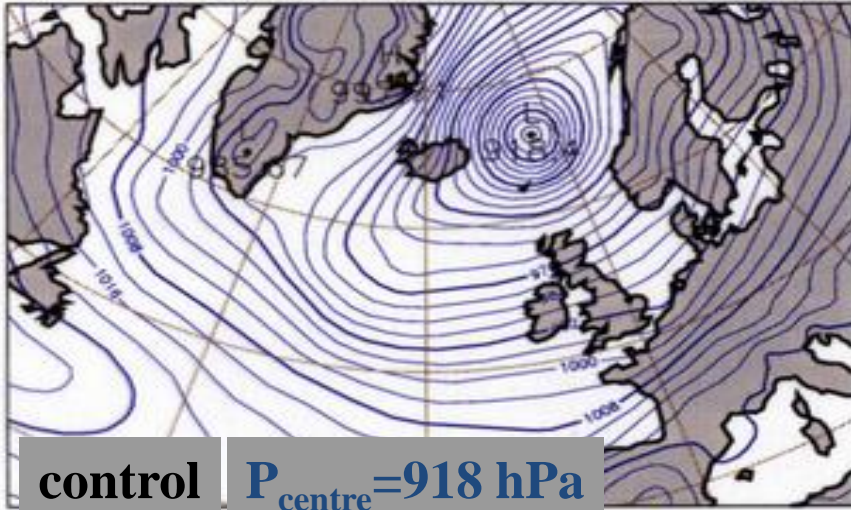
$\Delta F_a$  Horizontal energy flux divergence

$\Delta f$  Runoff

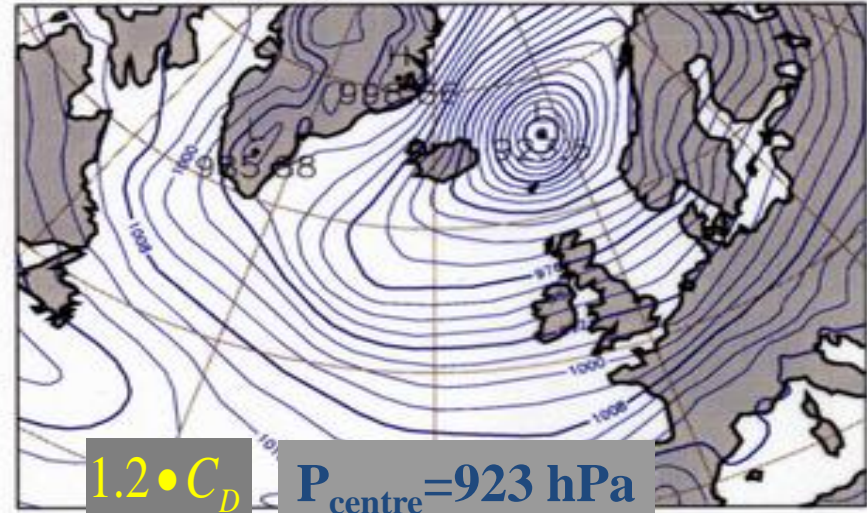


# Sensitivity of cyclone central pressure to surface drag

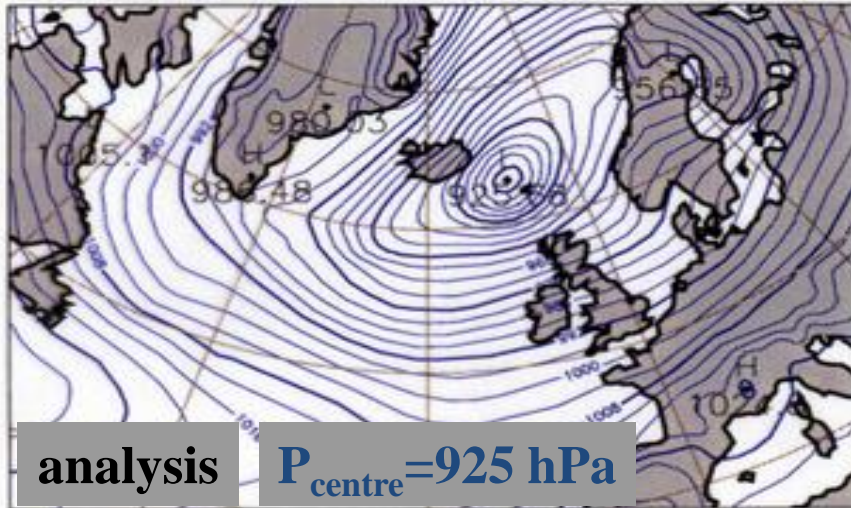
Pressure (zp0v)930109 48h to 48h by 24



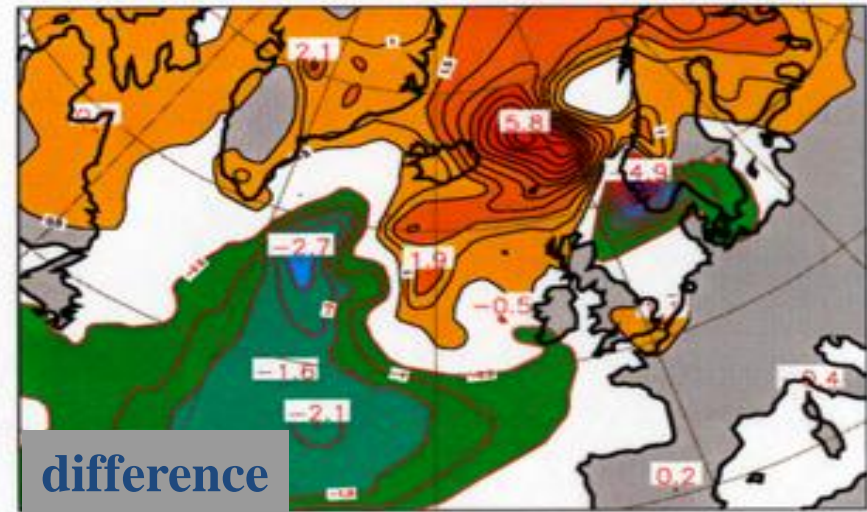
Pressure (zp4z)930109 48h to 48h by 24



Pressure (analysis)930109 48h to 48h by 24

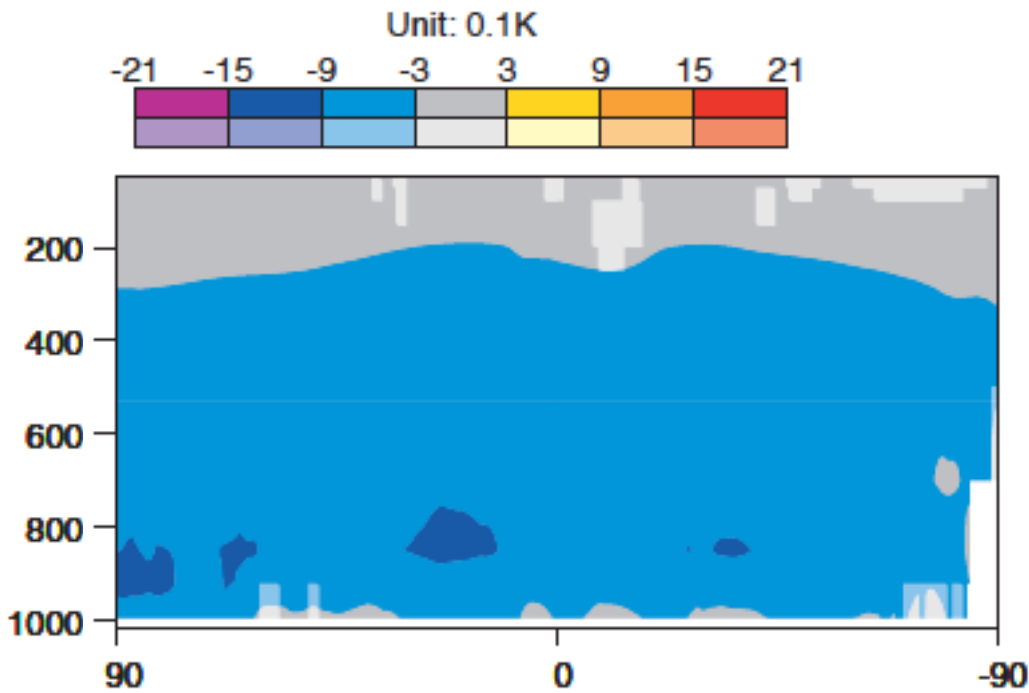


MSL Pres. Diff. 930109 48h to 48h by 24h zp4z - zp0v

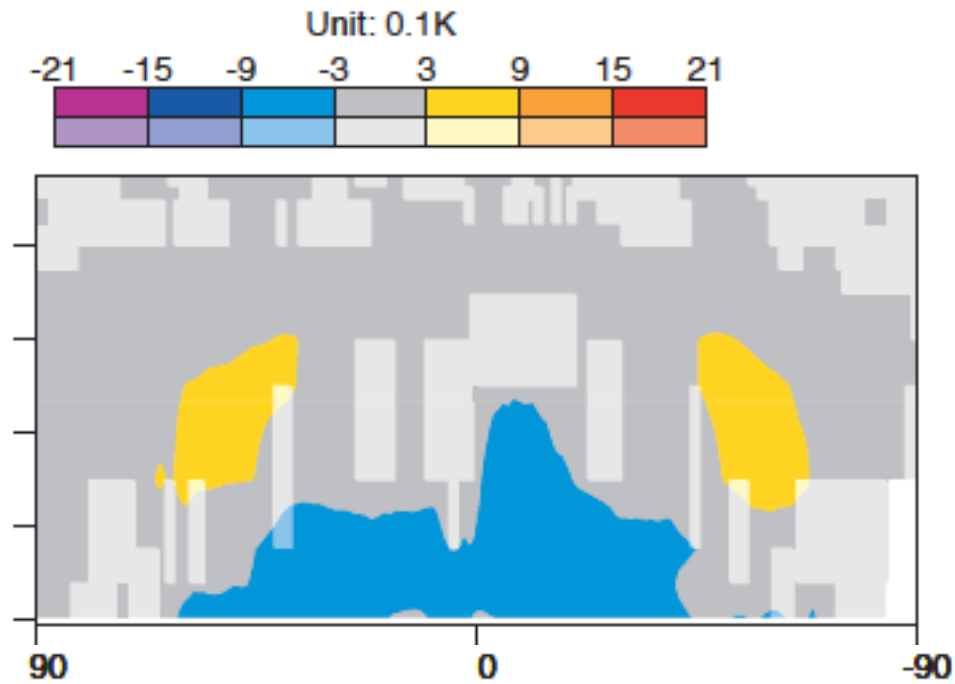


# T-tendencies over 12-hour data assimilation windows (K per 12 hours). Mean over DJF 2014.

Radiation



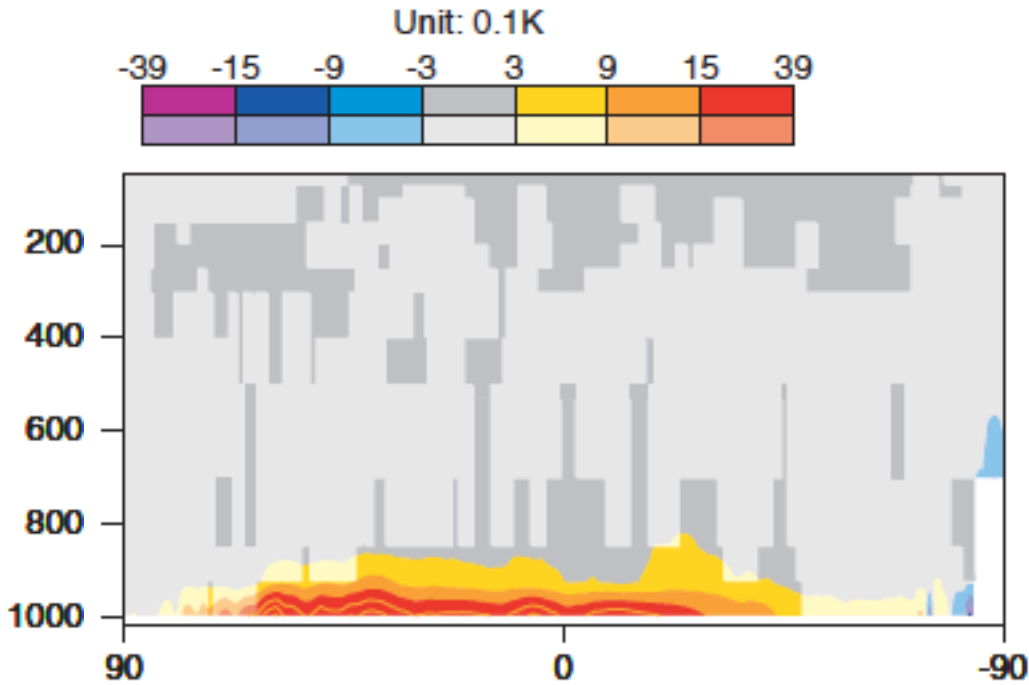
Cloud



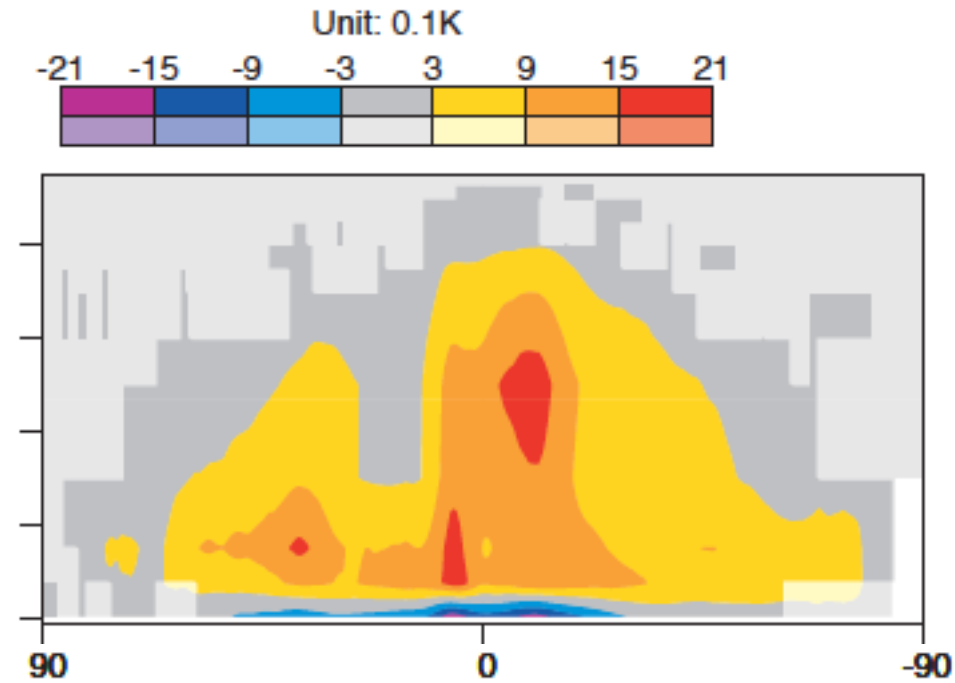
Deep colours = 5% significant.  
(Diagnostics Mark Rodwell)

# T-tendencies over 12-hour interval data assimilation window (K per 12 hours). Mean over DJF 2014.

Diffusion



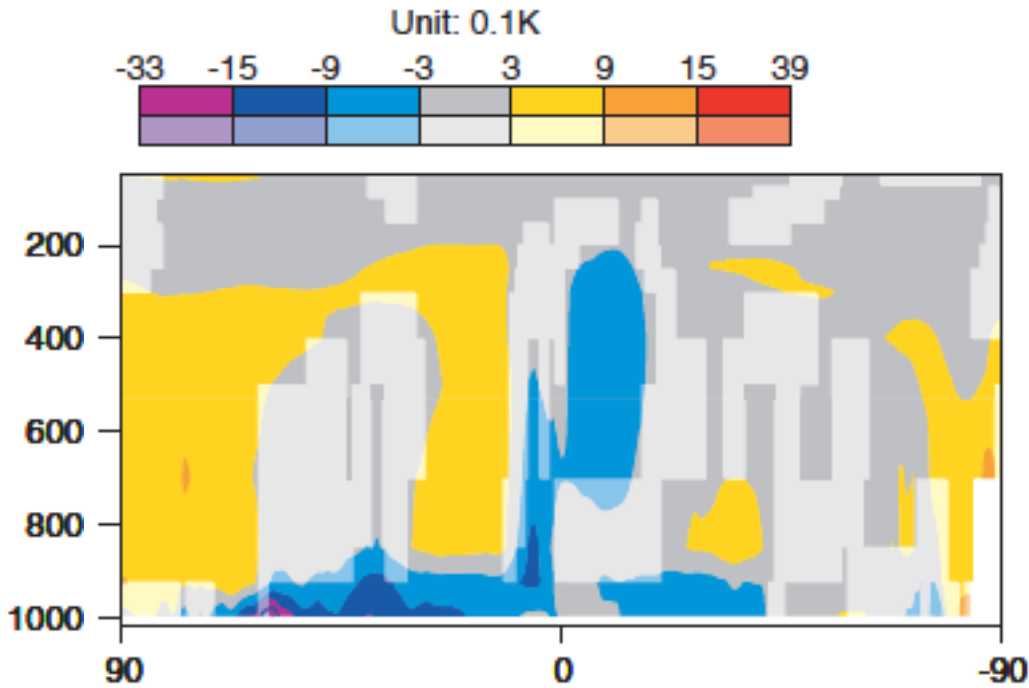
Convection



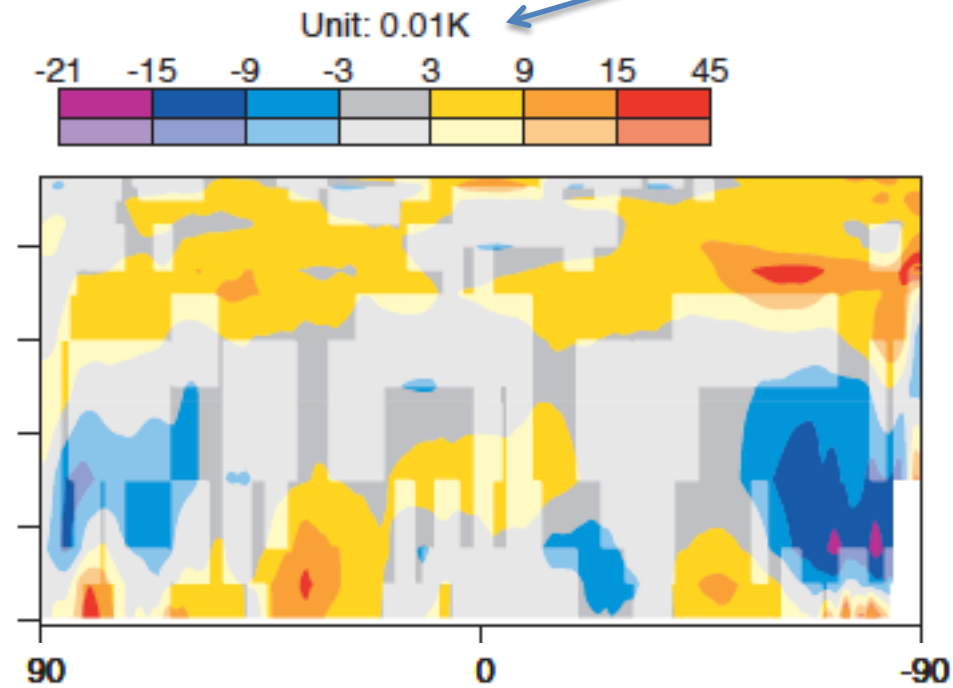
Deep colours = 5% significant.  
(Diagnostics Mark Rodwell)

# T-tendencies over 12-hour interval data assimilation window (K per 12 hours). Mean over DJF 2014.

## Dynamics



## Increment



Note change in scale

Deep colours = 5% significant.  
(Diagnostics Mark Rodwell)

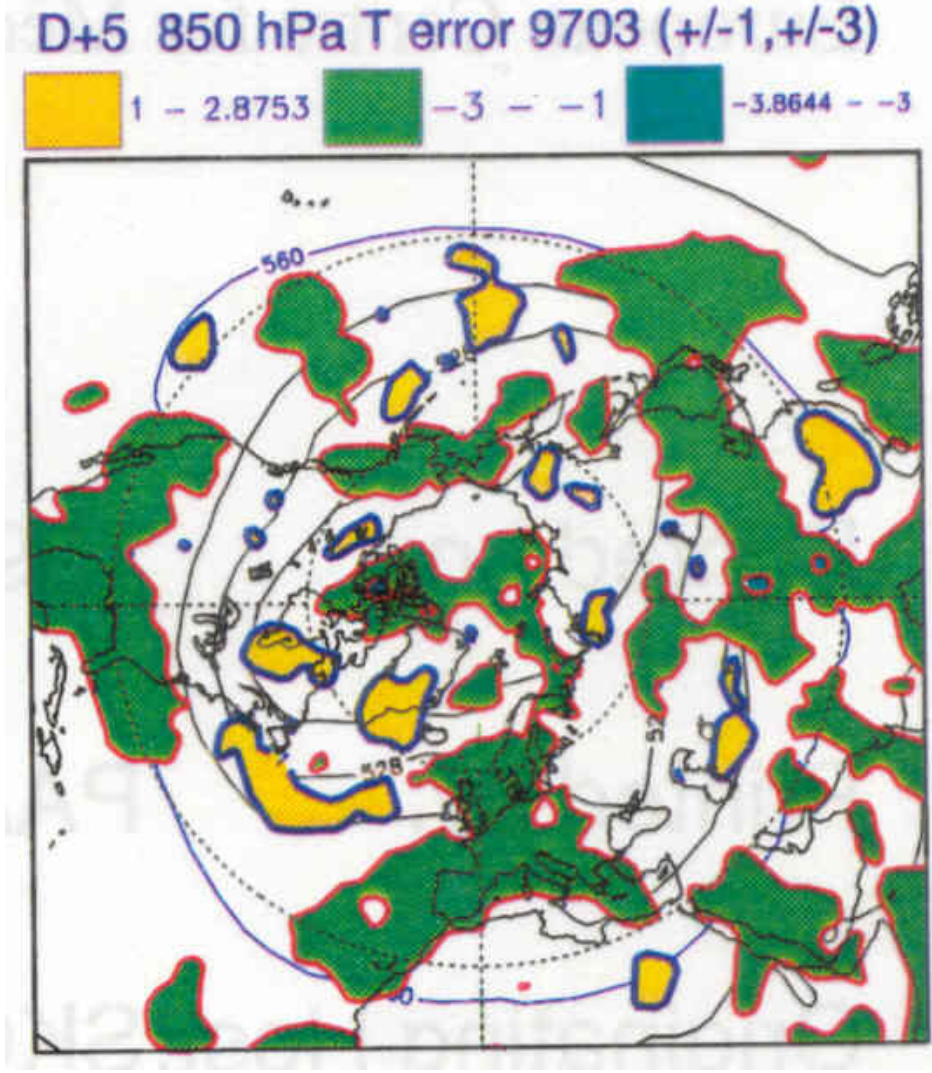
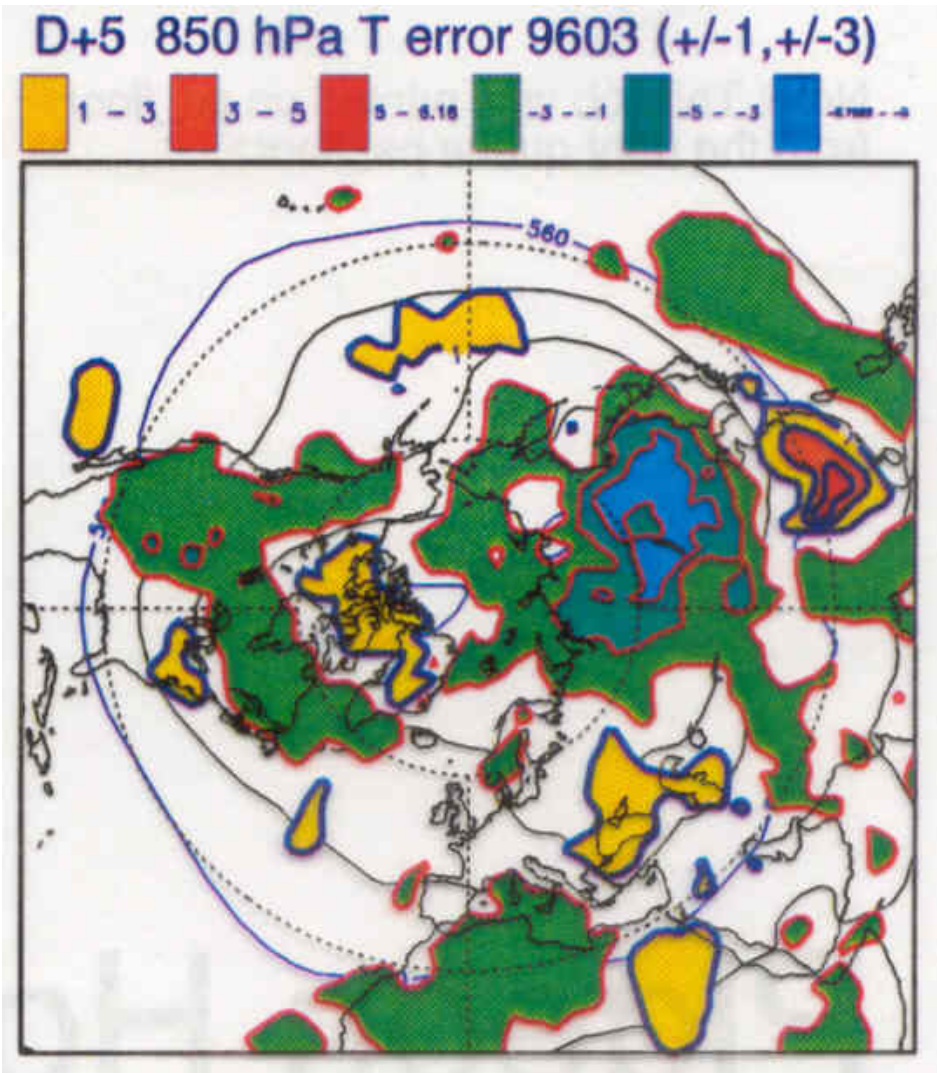


# Validation and diagnostics

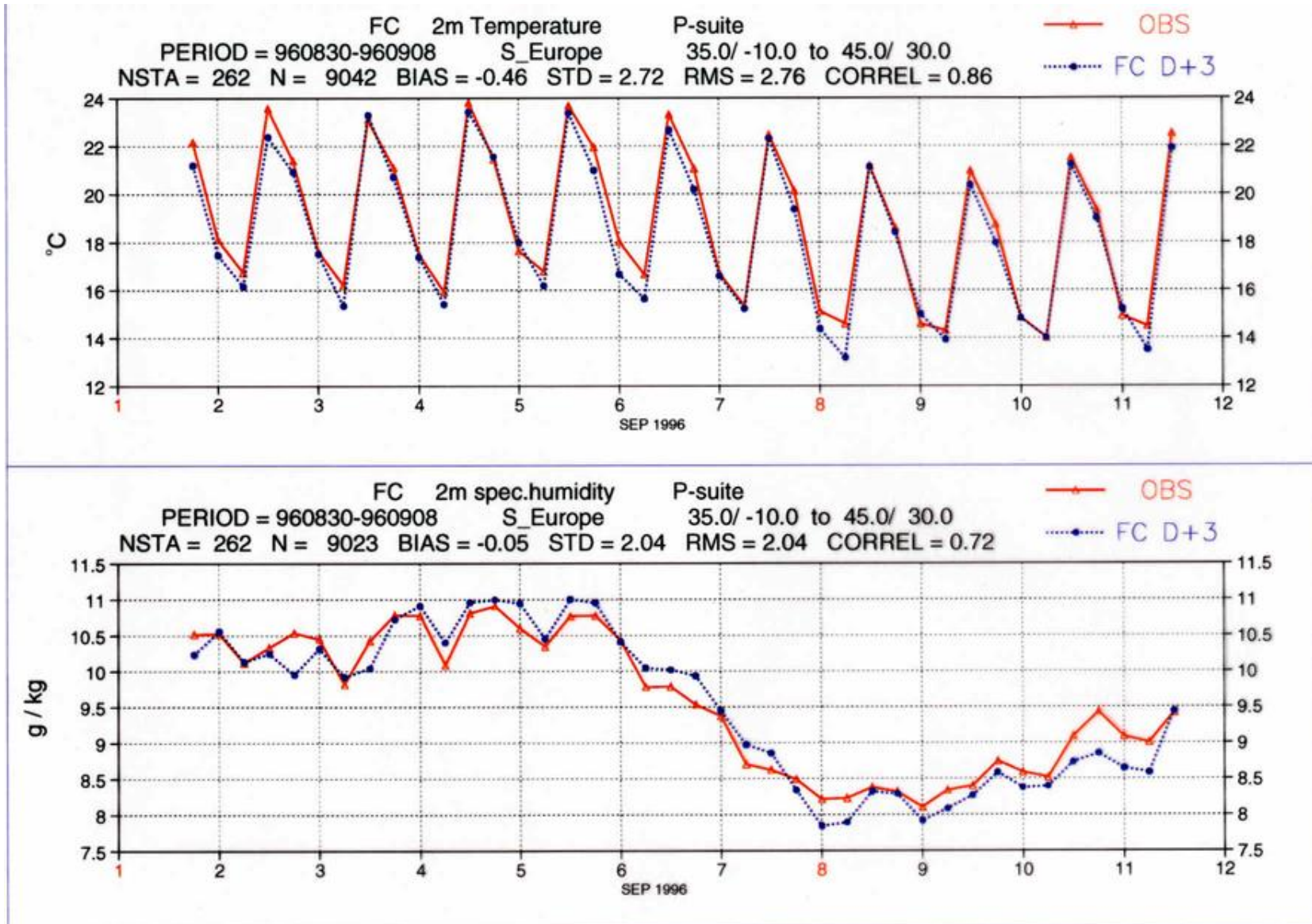
- **Compare with analysis**
  - daily verification
  - systematic errors e.g. from monthly averages
  - initial tendency diagnostics
- **Compare with operational data**
  - SYNOP' s
  - radio sondes
  - satellite
- **Climatological data**
  - CERES, ISCCP
  - ocean fluxes
- **Field experiments**
  - TOGA/COARE, PYREX, ARM, FIFE, ...



# Day-5 T850 errors



# Diurnal cycle of T/q at SYNOP stations averaged over Southern Europe (D+3 forecasts versus **obs**)

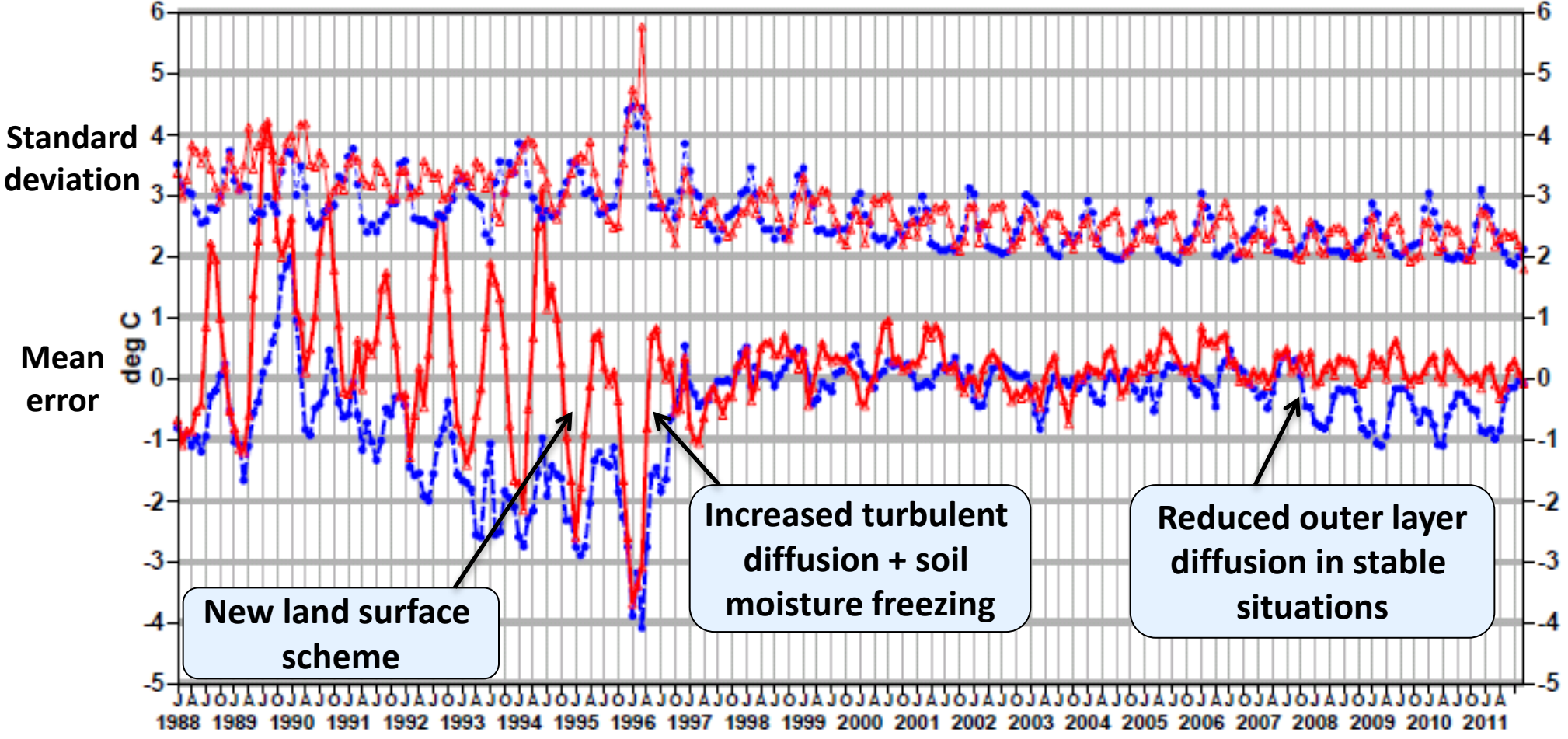




# History of temperature at screen level errors in ECMWF model (step 60/72)

Forecast error of 2 m Temperature [ deg C] Europe 30.0 -22.0 72.0 42.0

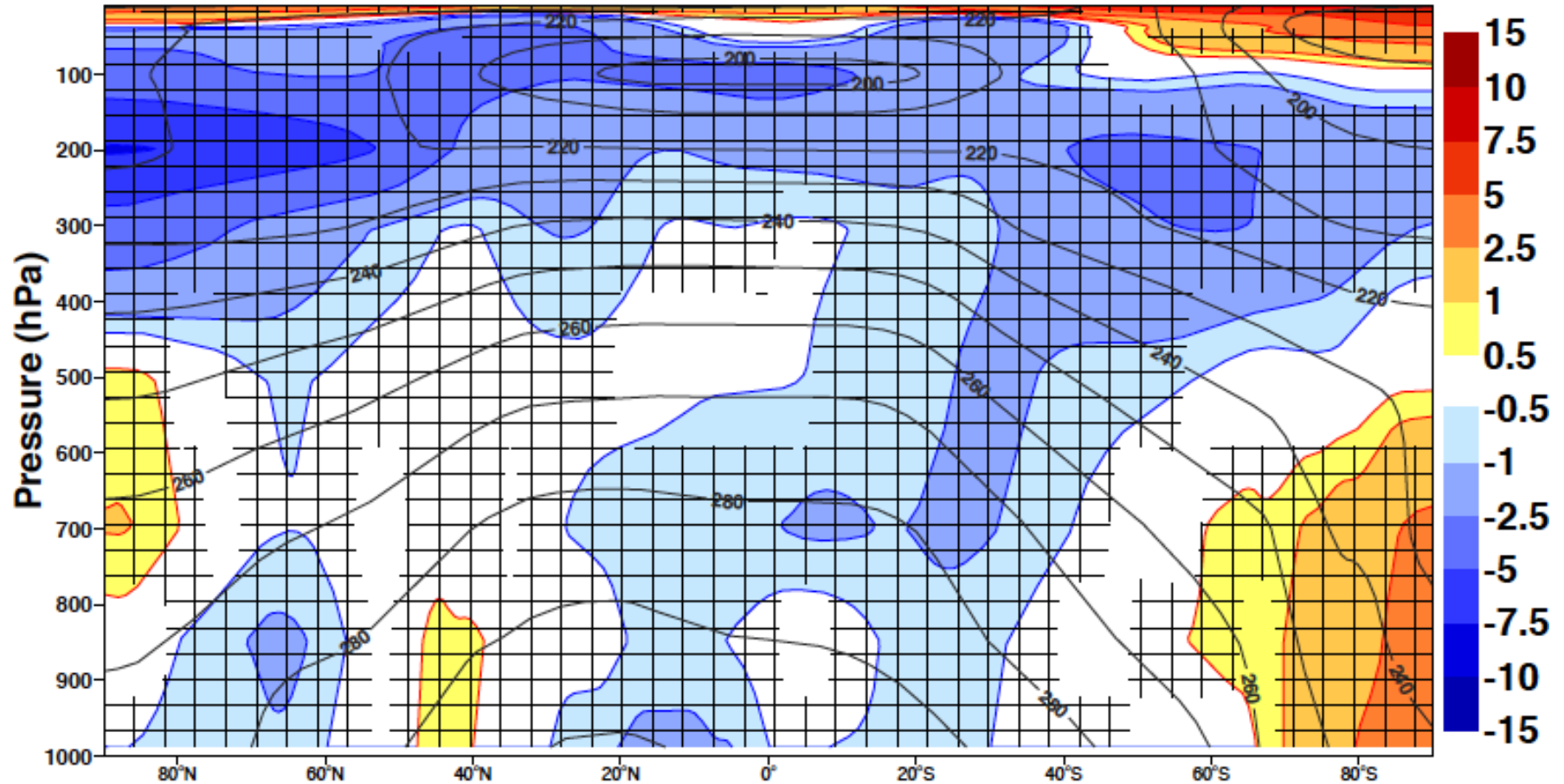
—●— bias 60h —▲— bias 72h - - -●- - - stdv 60h - - -▲- - - stdv 72h



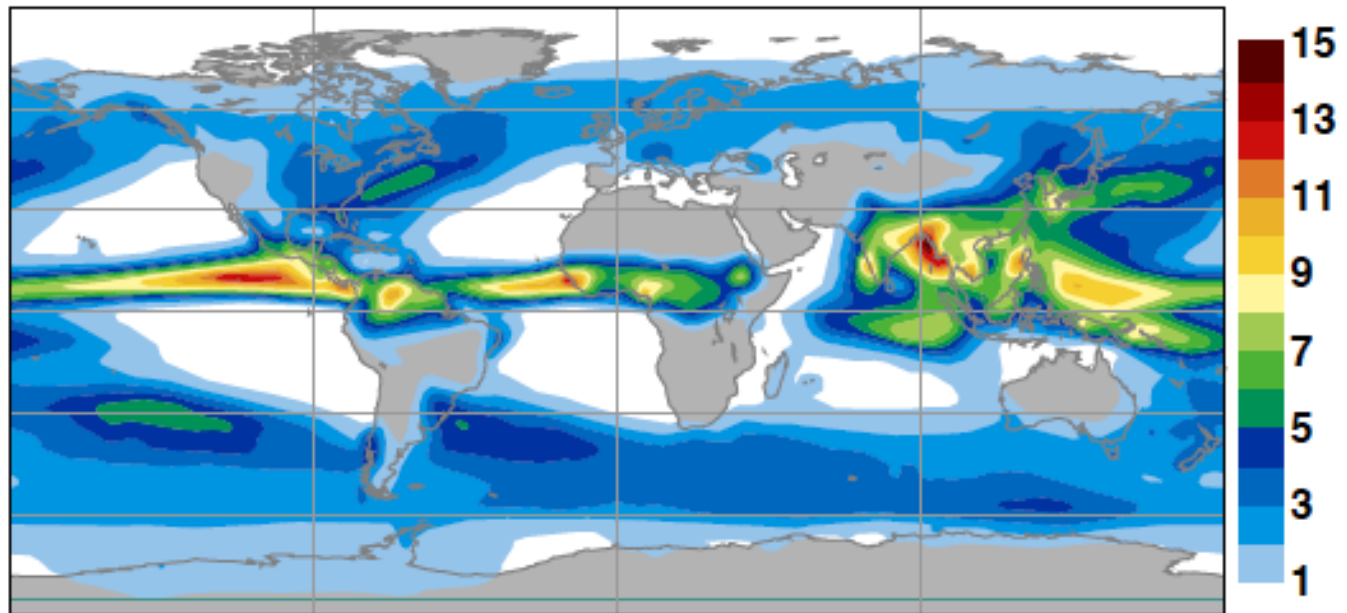
- Model temperature errors are influenced by many processes.
- Observations at process level are needed to disentangle their effect

# Zonal mean temperature bias of JJA model climate (37R3) versus ERA40

## Zonal Average T Difference fkgq-er40 (6-8 1962-2005)

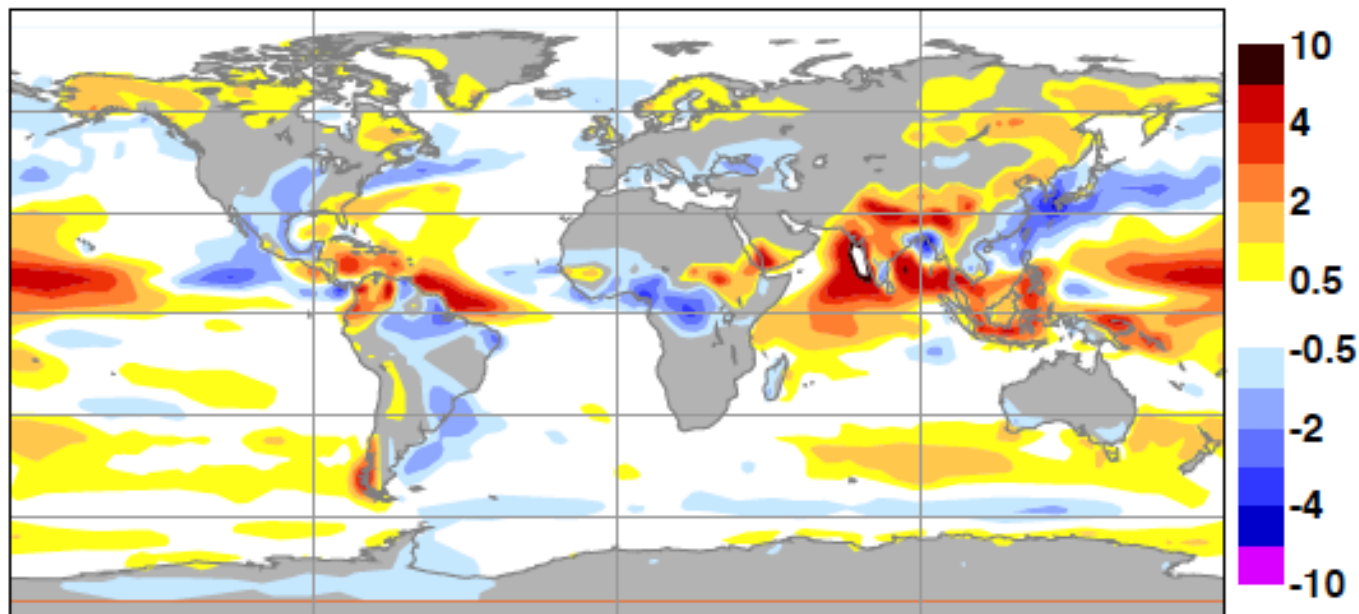


Precipitation GPCP (6-8 1962-2005)



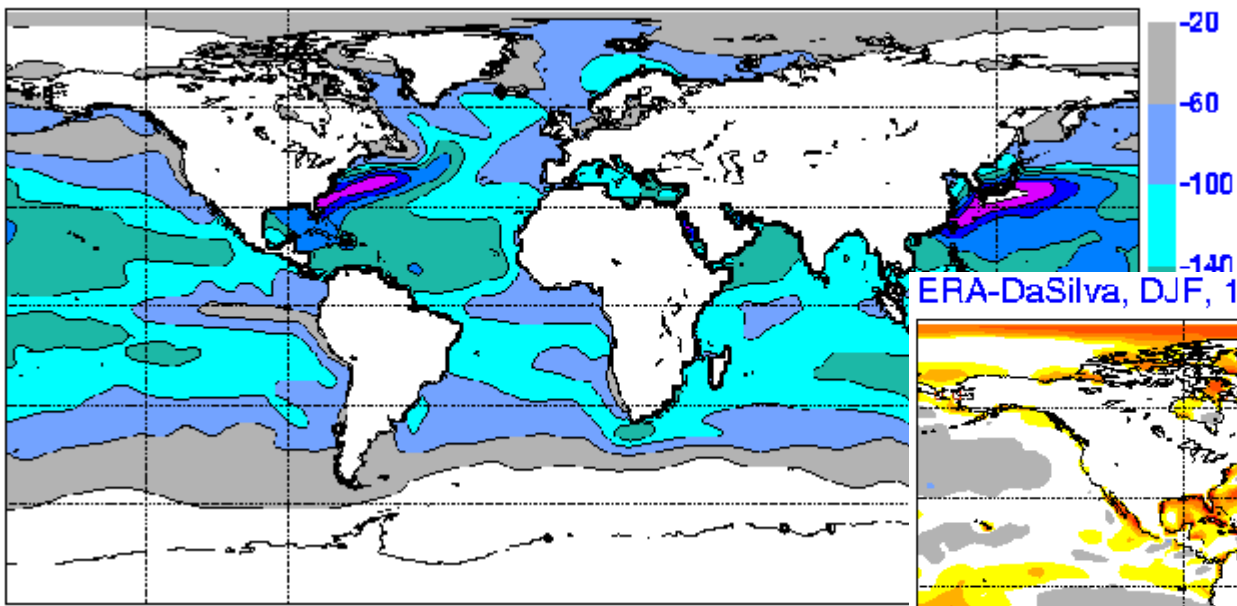
Precipitation in  
JJA model climate  
(37R3) versus  
GPCP

Precipitation fkgq-GPCP (6-8 1962-2005)

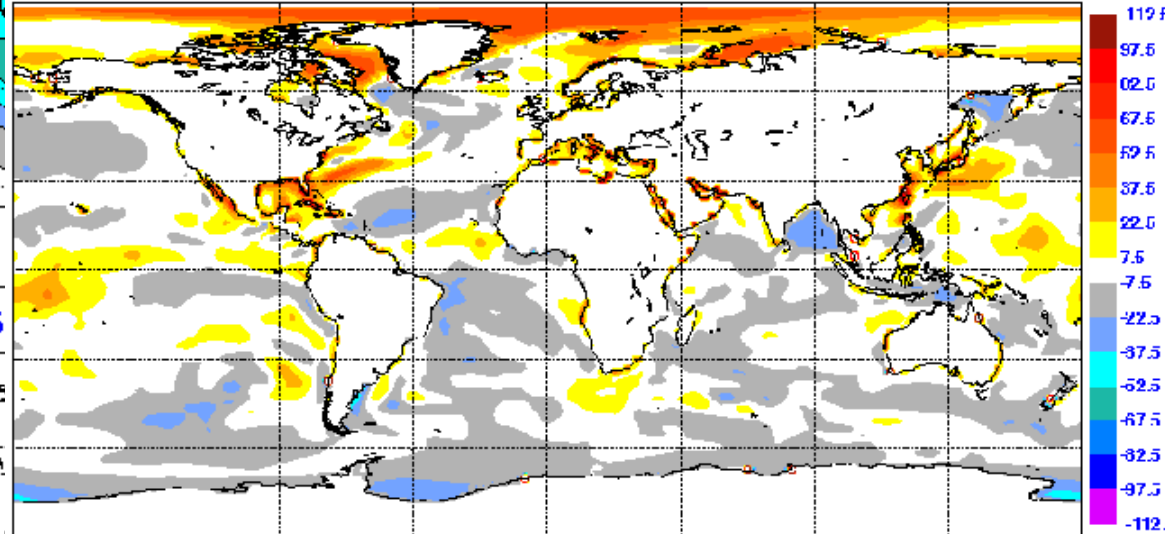


# Lat. Heat Flux-DJF (ERA\_40\_Step\_0\_6 vs. DaSilva climatology)

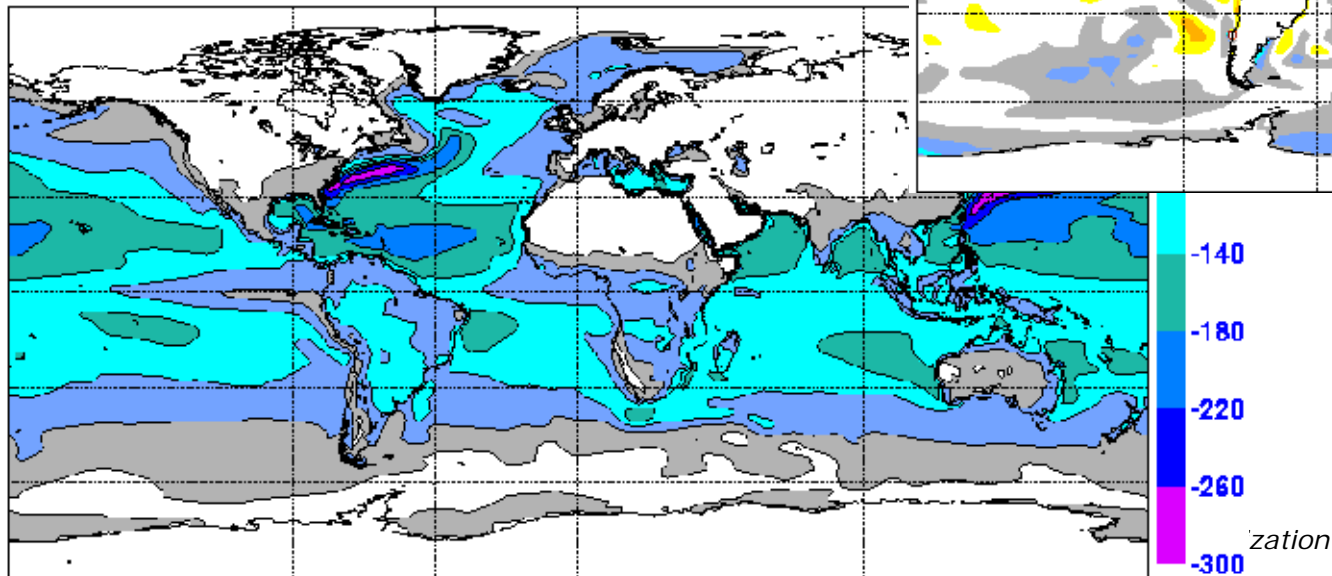
DaSilva clim., DJF; LH (W/m<sup>2</sup>); SeaAver=-71.8



ERA-DaSilva, DJF, 1986-1994; LH (W/m<sup>2</sup>), step=0-6 ; SeaAver=0.1



ERA Clim., DJF, 1986-1994; LH (W/m<sup>2</sup>), step=0-6 ; S

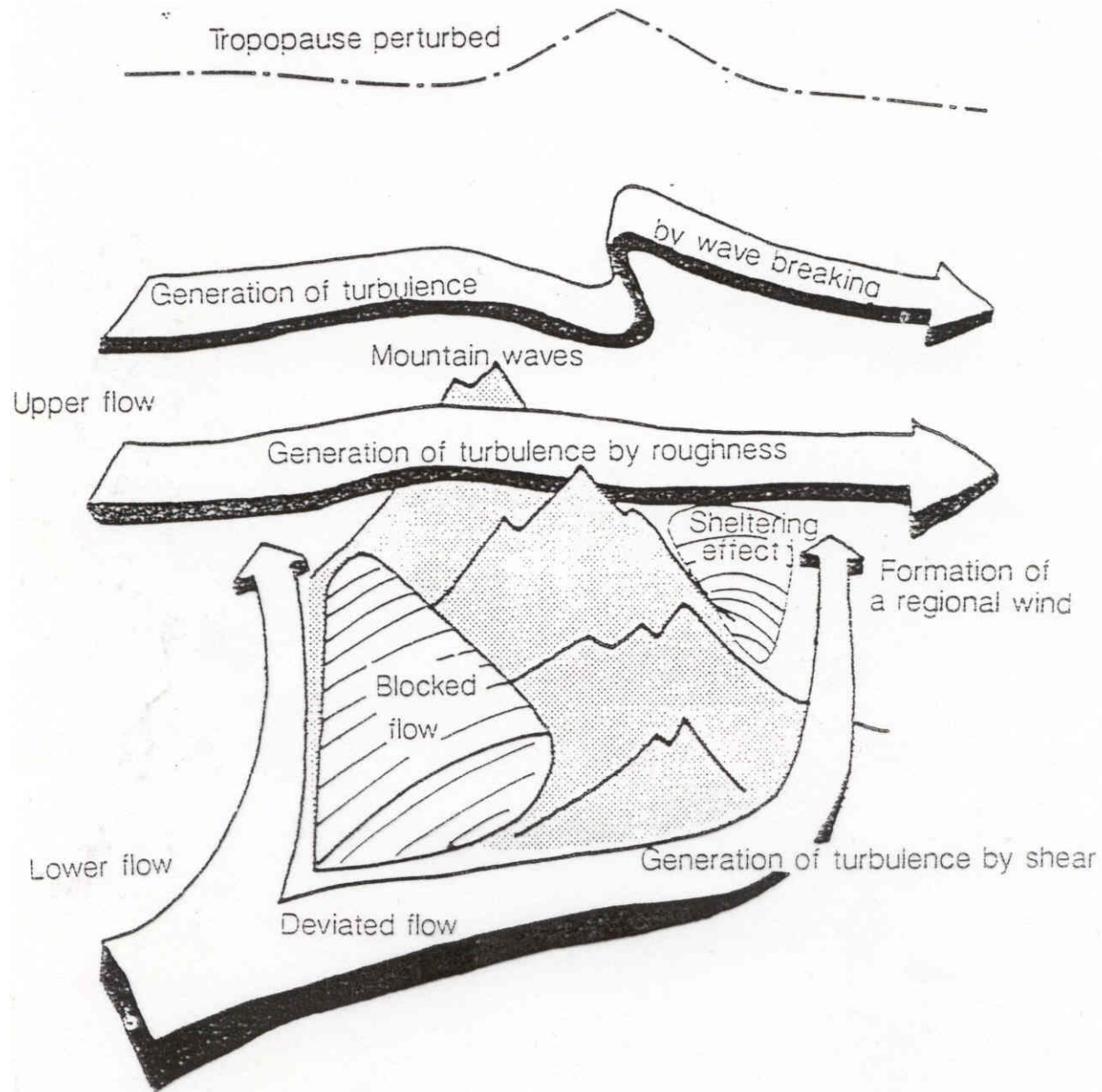


ERA40 model

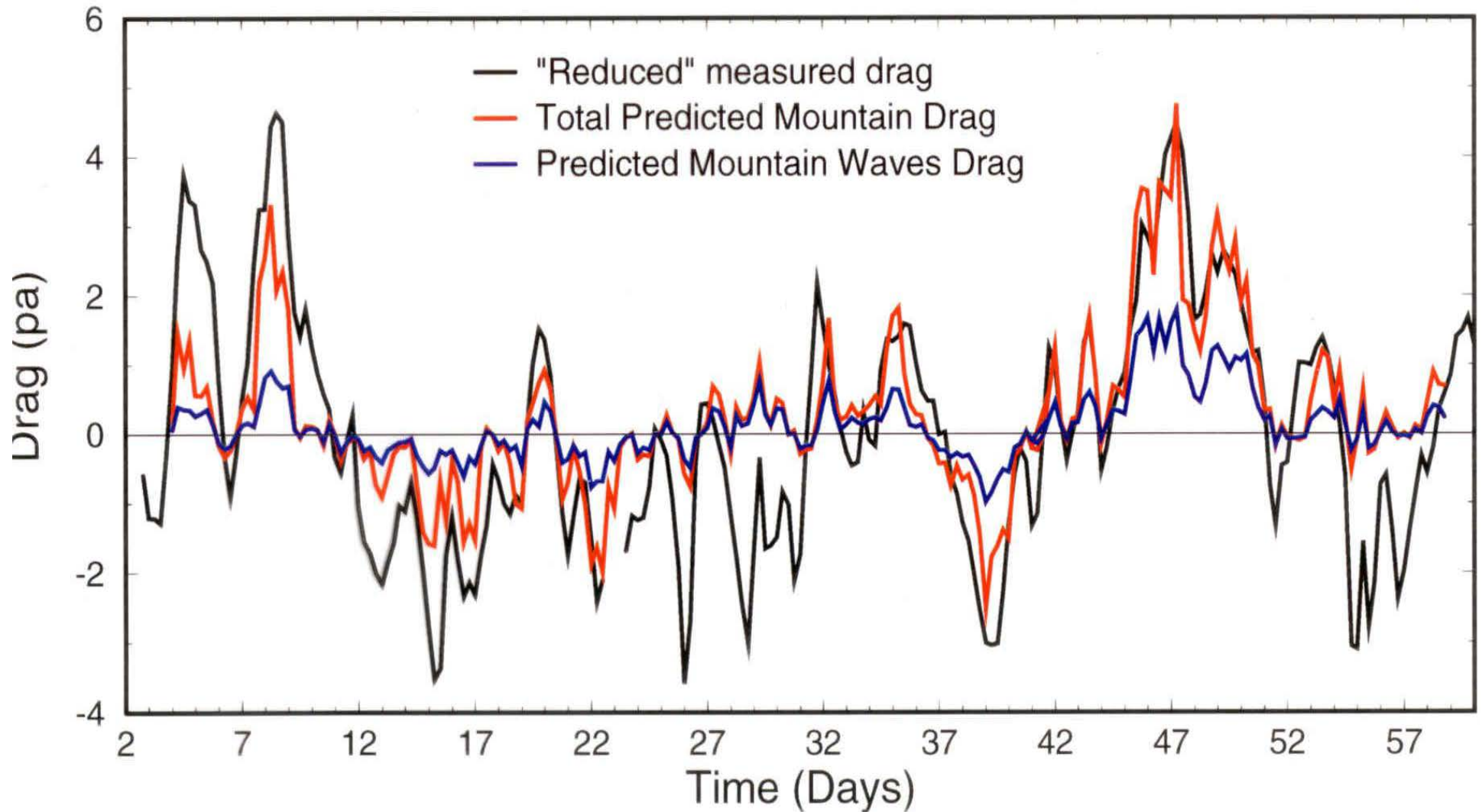
zation



# PYREX experiment

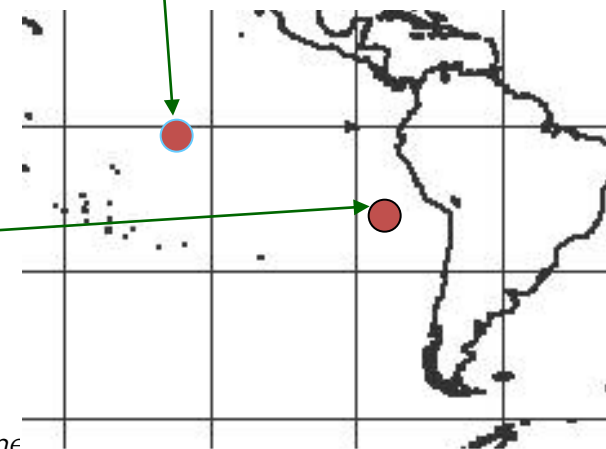
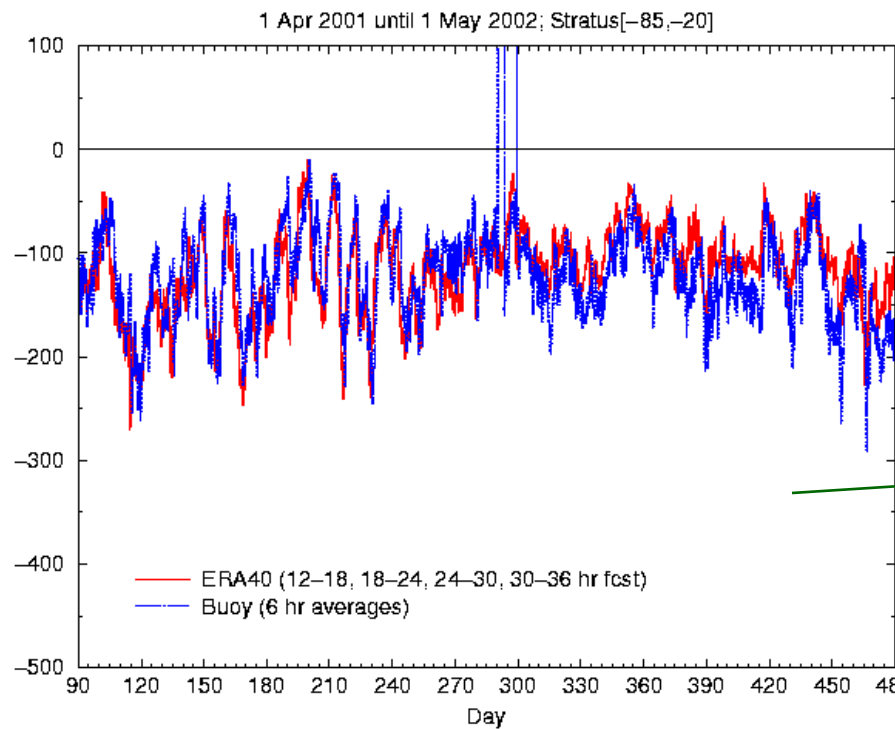
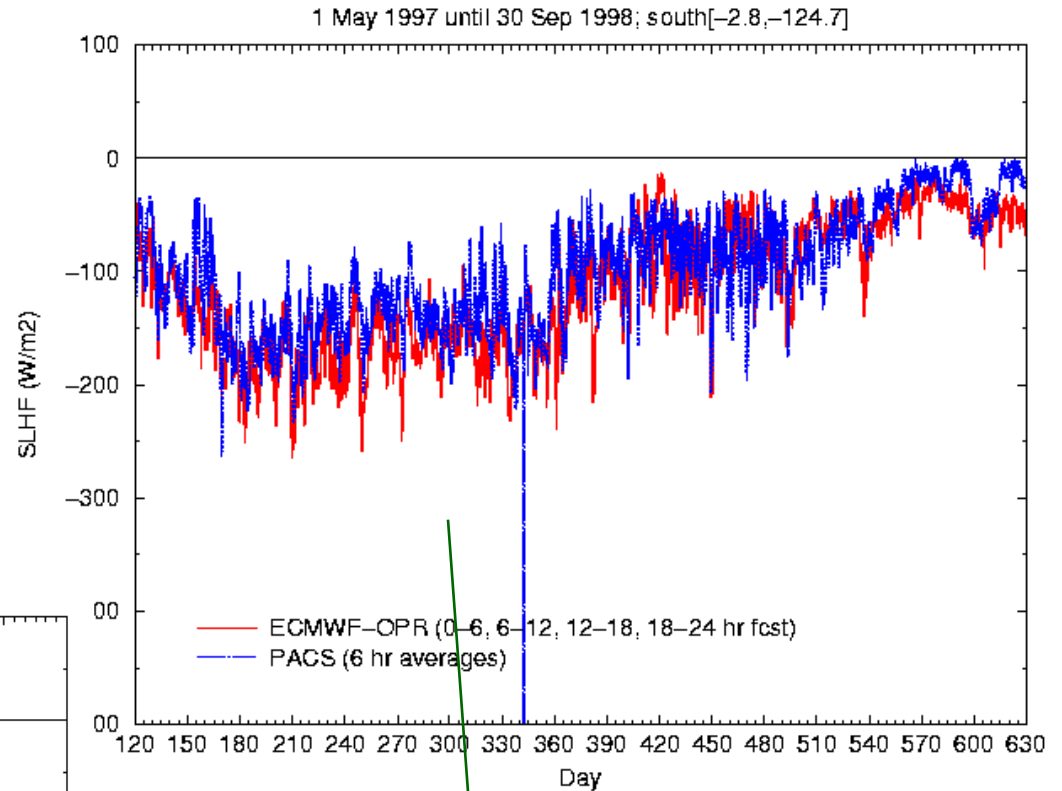


# PYREX experiment: model results

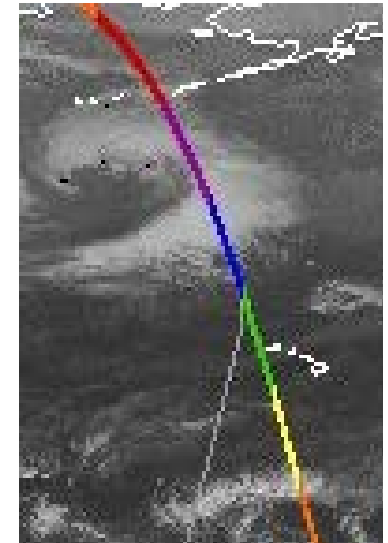
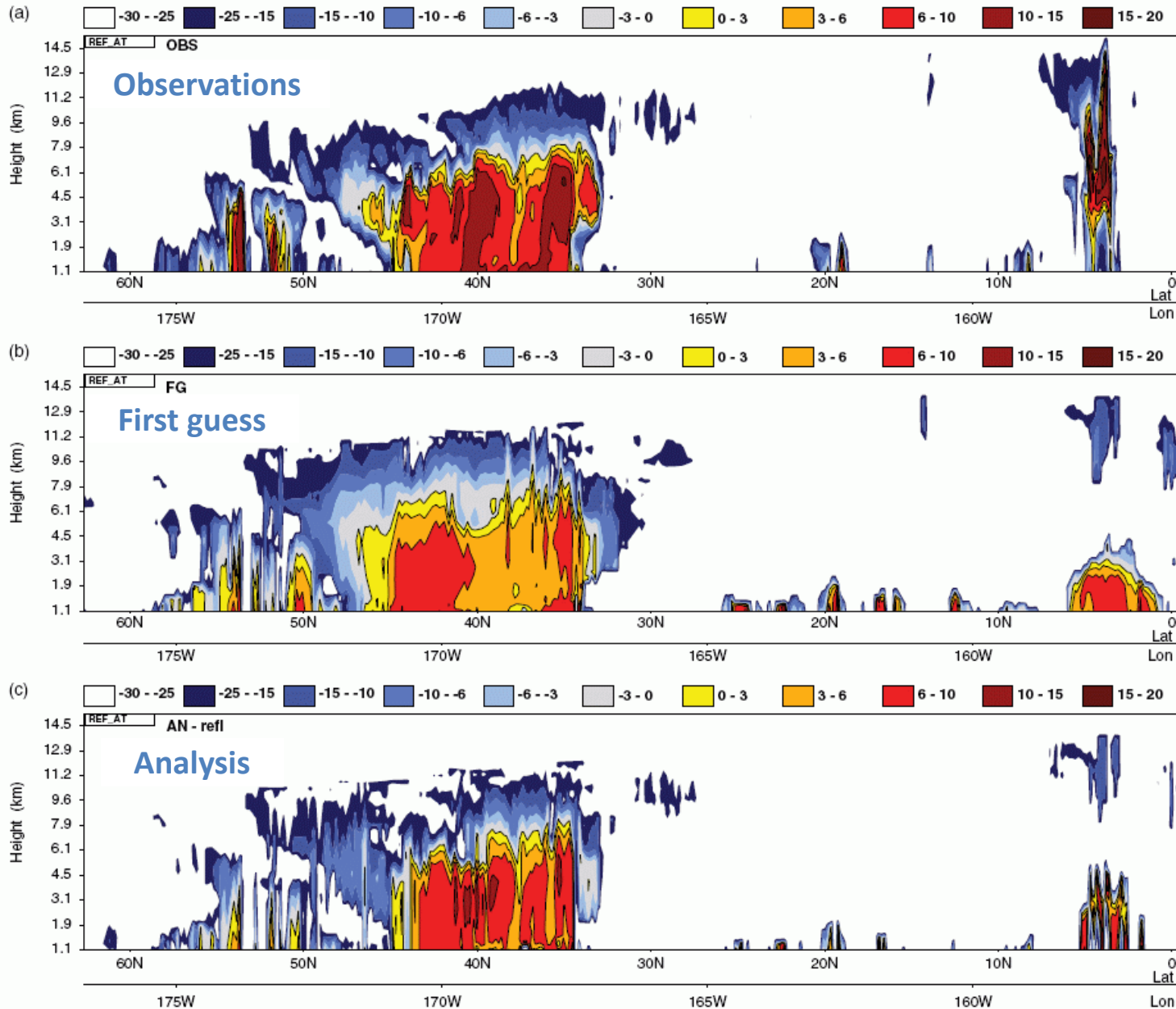




# Latent heat flux: ERA-40 vs. IMET buoy



# Data assimilation – 1D-Var of cloud radar reflectivity



20070123  
over Pacific

Observations:  
CloudSat cloud  
radar reflectivity

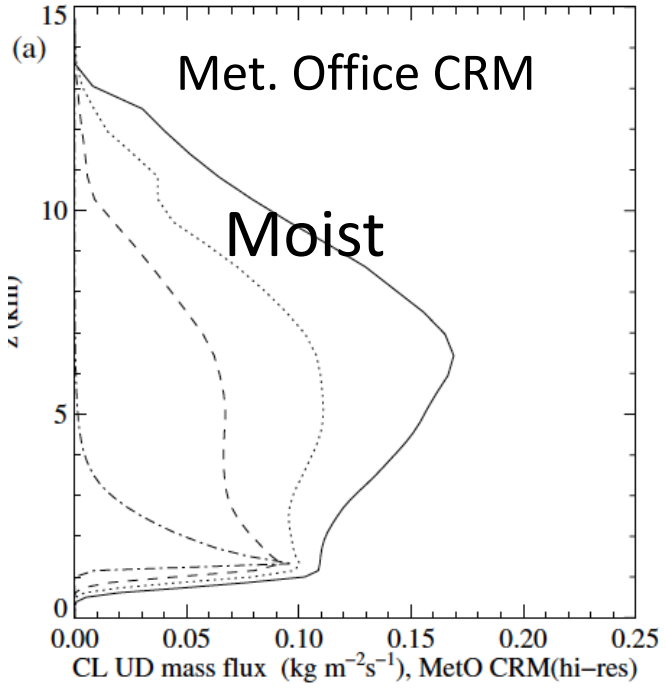
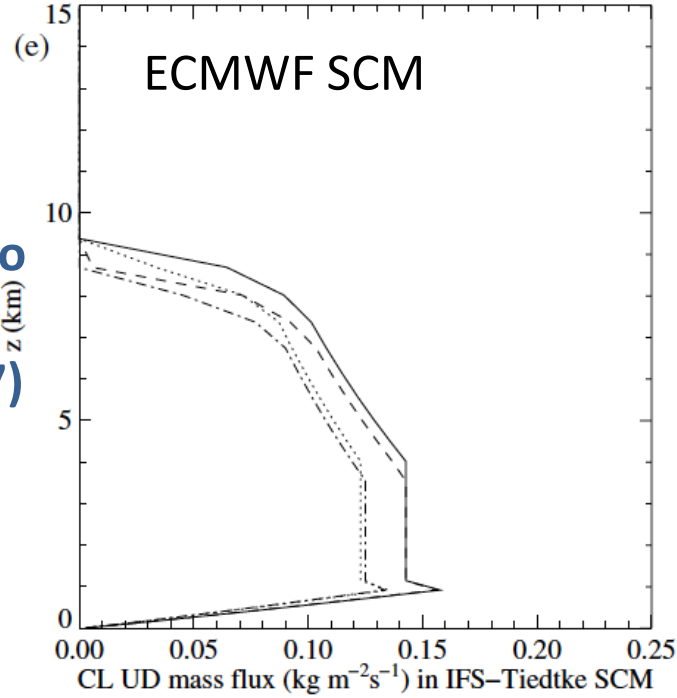
# Parameterization development strategy

- **Invent empirical relations (e.g. based on theory, similarity arguments or physical insight)**

To find parameters use:

- Theory (e.g. radiation)
  - Field data (e.g. GATE/TOGA/COARE for convection; PYREX for orographic drag; HAPEX/SEBEX/FLUXNET for land surface; Kansas for turbulence; ASTEX/Cloudsat for clouds; BOREAS for forest albedo)
  - Cloud resolving models (e.g. for clouds and convection)
  - Meso scale models (e.g. for subgrid orography)
  - Large eddy simulation (turbulence)
- **Test in stand alone or single column mode**
  - **Test in 3D mode with short range forecasts**
  - **Test in long integrations (model climate)**
  - **Consider interactions and optimize parameters**

The GCSS inter-comparison of CRM's and SCM's showed that most parameterizations have too little sensitivity to environment moisture (Derbyshire et al. 2007)



CY23R3 changes to convection parameterization (introduced Nov 2007) : stronger entrainment, also dependent on q, and variable CAPE reduction time scale (Bechtold et al. 2008).

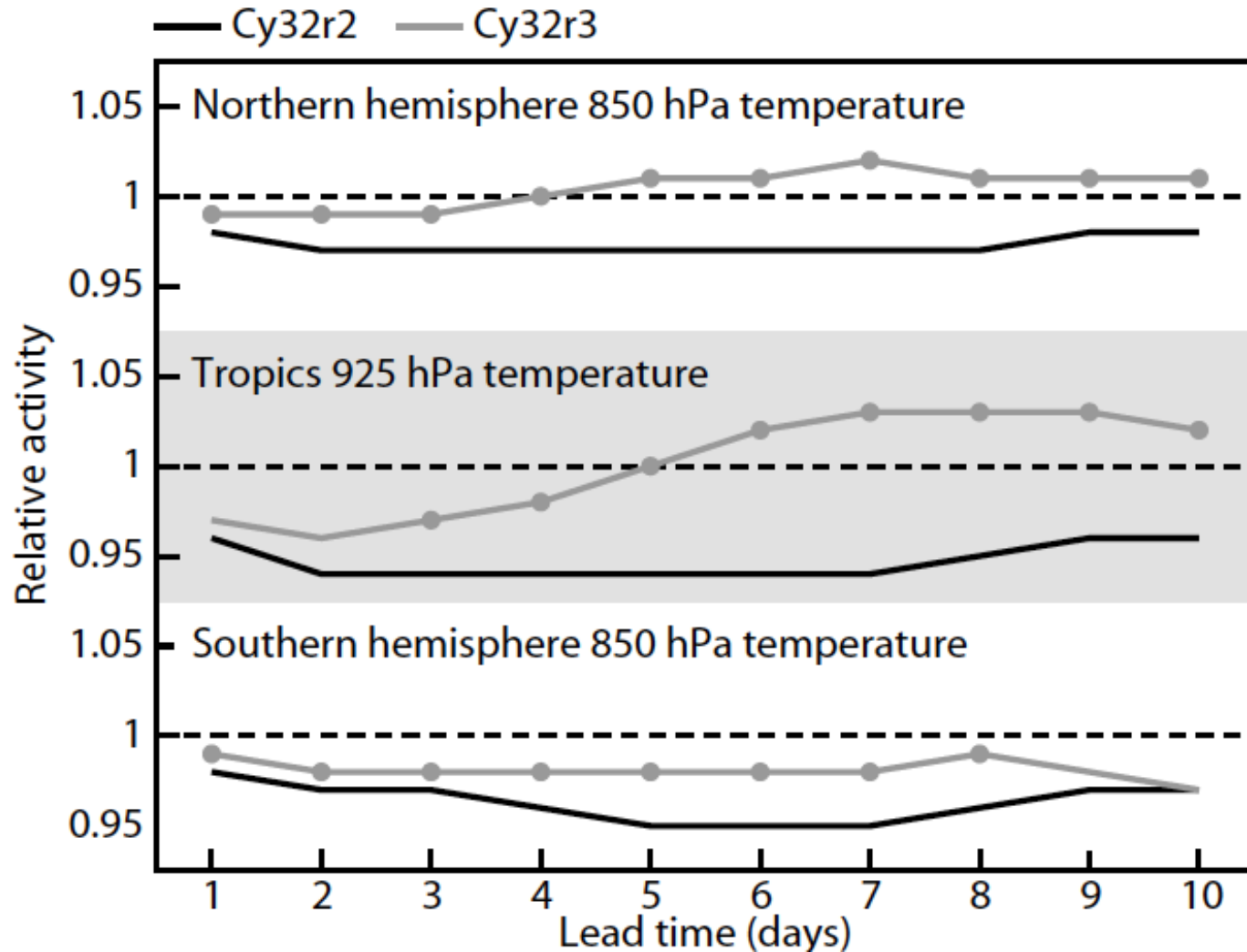
$$\frac{1}{M} \frac{\partial M}{\partial z} = \varepsilon - \delta \quad \varepsilon = \underbrace{c_0}_{turb} F_\varepsilon + \underbrace{c_1 \frac{\bar{q}_s - \bar{q}}{\bar{q}}}_{org, deep, buoy > 0} F_\varepsilon; \quad F_\varepsilon = \left( \frac{\bar{q}_s}{\bar{q}_{s,b}} \right)^2$$

$$\tau = \frac{H}{\bar{w}_u^H} \quad \alpha; \quad \alpha = 1 + \frac{264}{n}$$

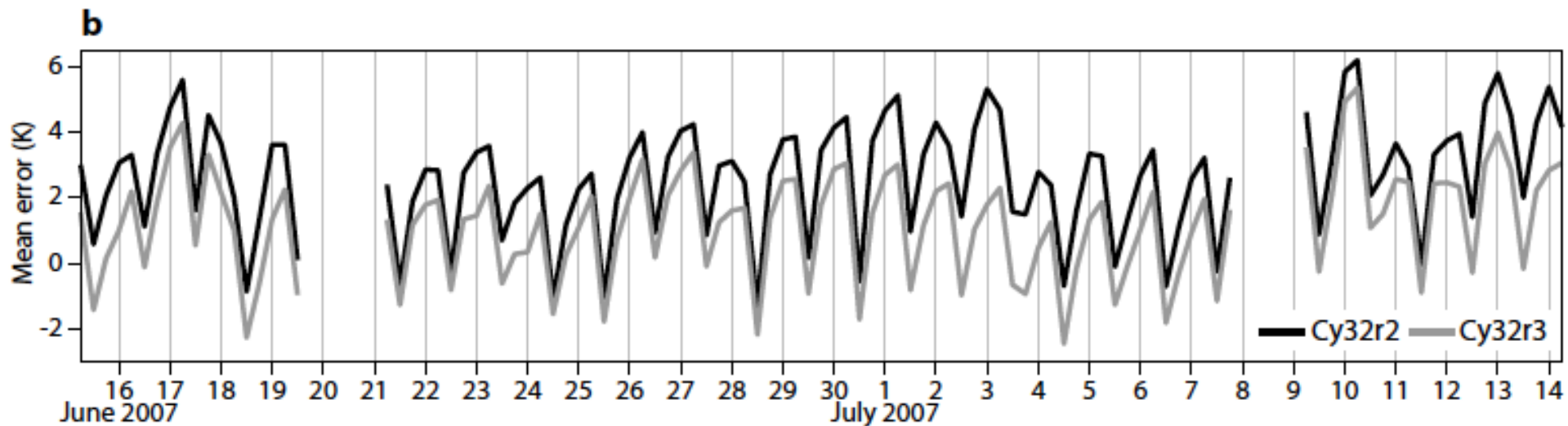
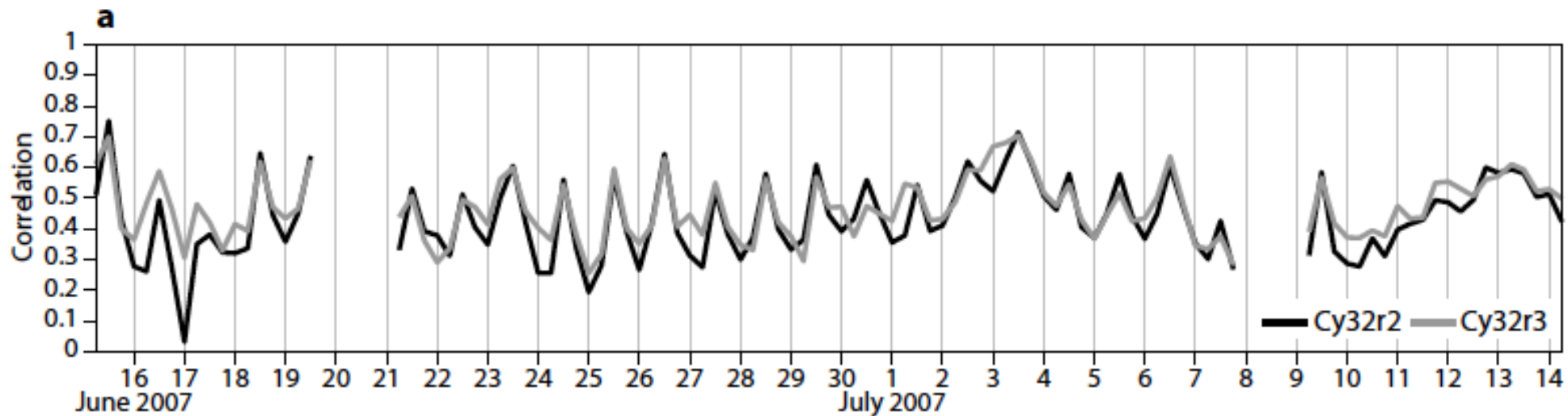
# Model activity in T799 10-day forecasts

Relative activity is model activity divided by activity in analysis

Activity is standard deviation of anomaly from ERA-40 based climatology



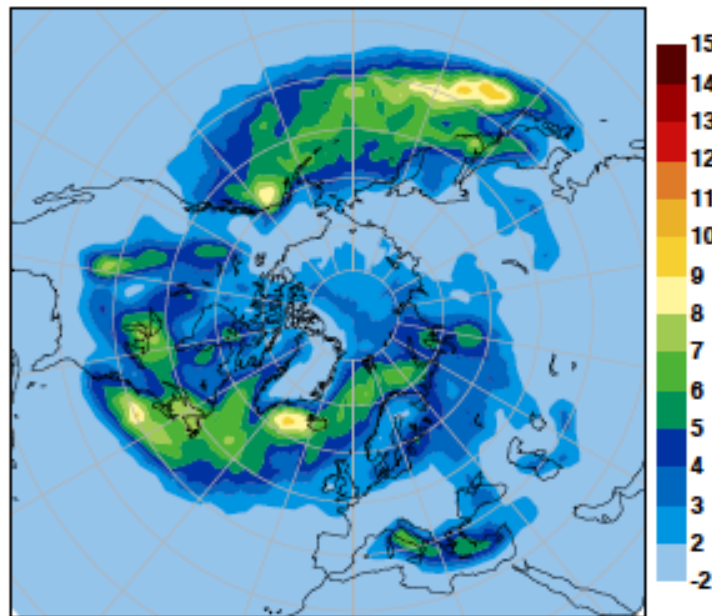
# Verification of brightness temperature of daily 6,12,18,24 hr forecasts with Meteosat observations.



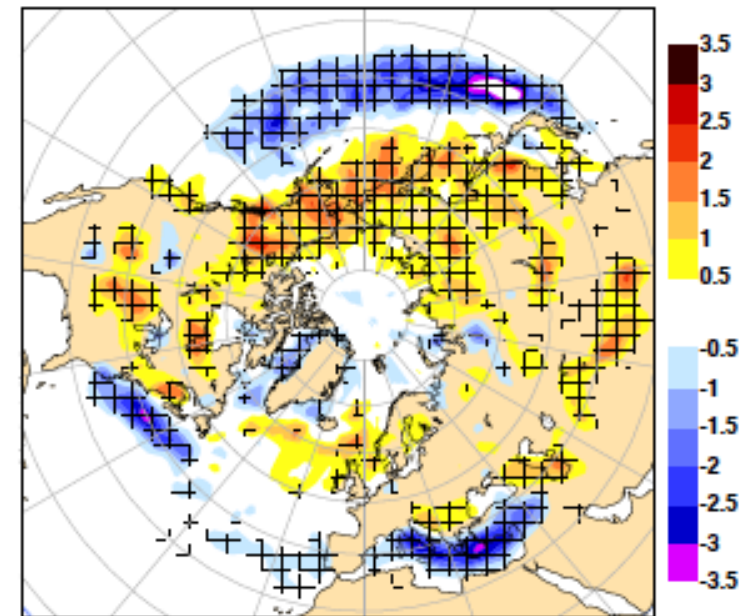


# Storm frequency statistics (Bechtold et al. 2007)

(a) Number of MSLP Minima (er40 DJFM 1962-2005)

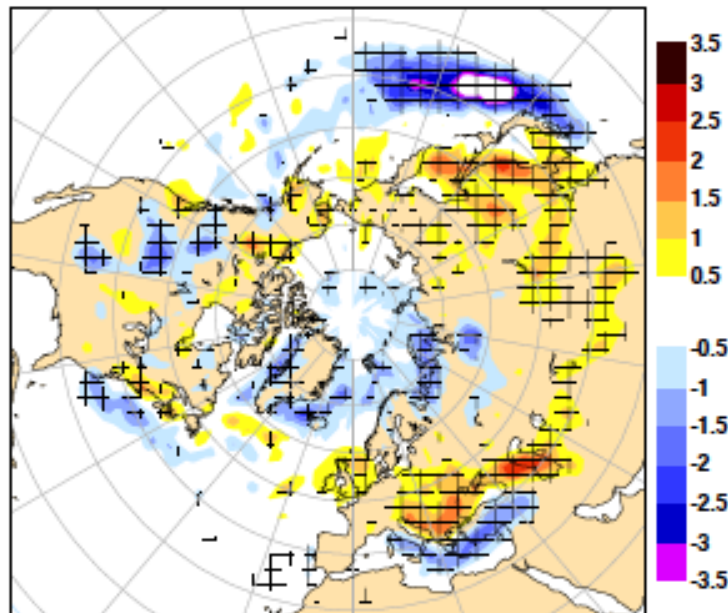


(b) Number of MSLP Minima (Cy32r2-er40 DJFM 1962-2005)

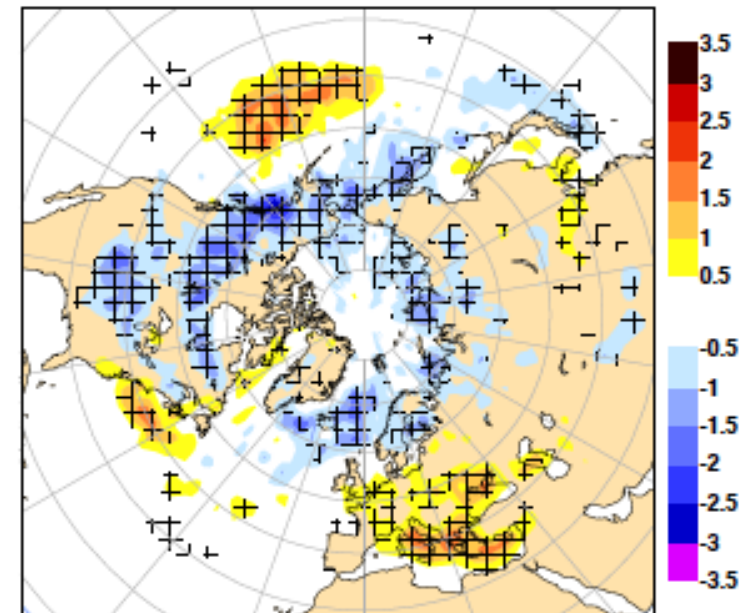


T159 13-month  
integrations from  
1962 to 2005

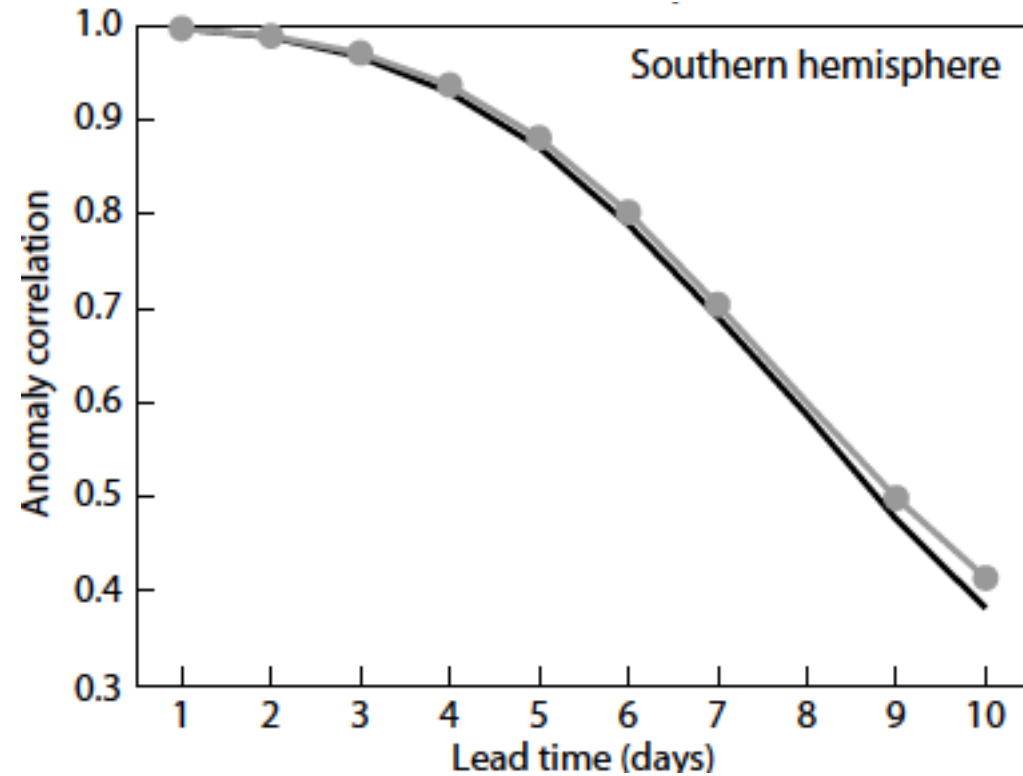
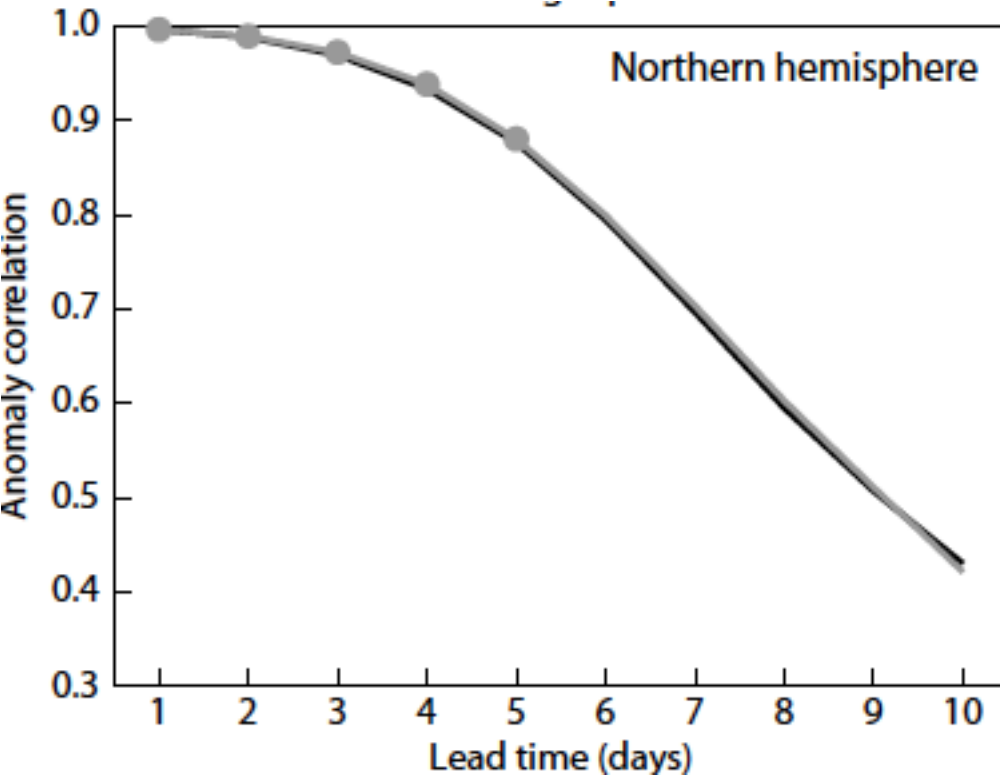
(c) Number of MSLP Minima (Cy32r3-er40 DJFM 1962-2005)



(d) Number of MSLP Minima (Cy32r3-Cy32r2 DJFM 1962-2005)



# Anomaly correlation of 500hPa height in T799 10-day forecasts



**Modest improvement in model performance in spite of increased activity**



# Concluding remarks

**Enjoy the course**

**and**

**Do not hesitate to  
ask questions**

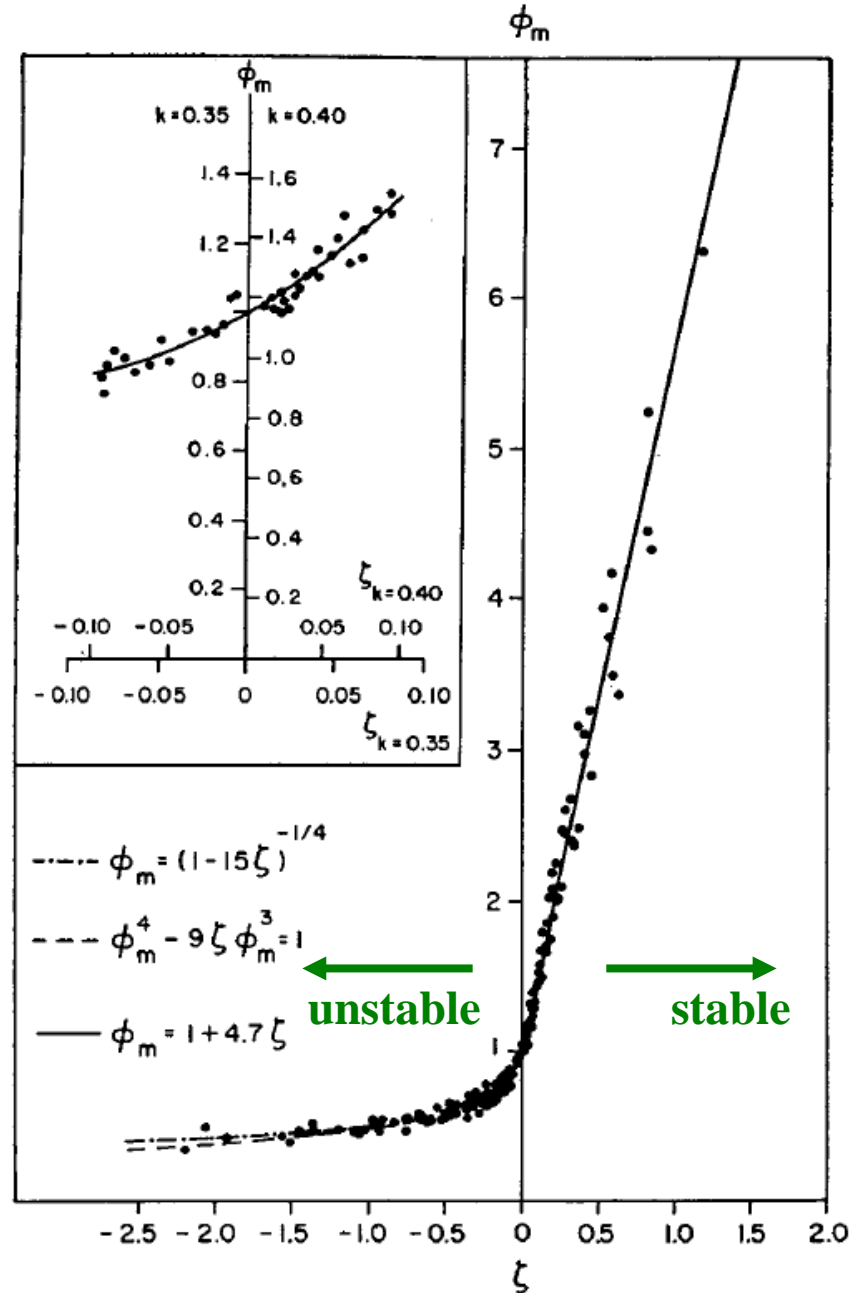
# Measure turbulent diffusion coefficients

Parameterization should be simple:

- Clear scale separation
- Solid scaling relation between fluxes and profiles

$$K_m = \frac{ku_* z}{\phi_m(z/L)}$$

Businger et al. (1971)



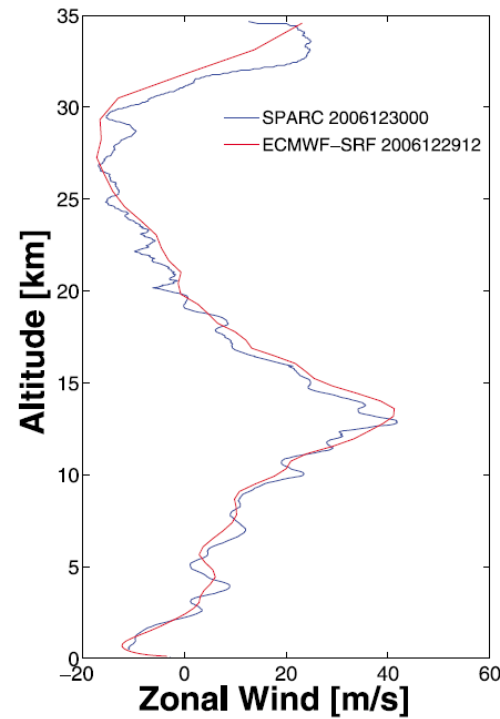
## But in practise

- The atmosphere has a lot of meso-scale variability, which is missing in the ECMWF model.
- Houchi et al. (2010) analyse a large volume of radio sonde data and conclude that the ECMWF model underestimates shear by a factor 2.5
- This might be the background of “long tail formulations”, which makes the uncertainty large

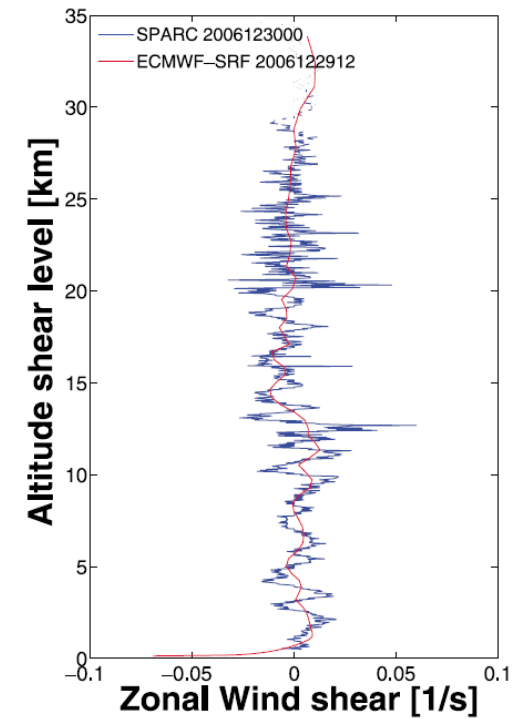
## And how to handle the heterogeneous surface boundary condition ?

Concepts are well established:

- Use “effective roughness” ( Mason, 1988); Grant and Mason, 1990; Wood and Mason, 1991)
- Turbulent Orographic Form Drag TOFD (Wood et al., 2001; Beljaars et al. 2004)
- The uncertainty in the coefficients that characterise the landscape and the sub-grid orography is large



Houchi et al. (2010)



Llanthony valley, S. Wales

# Changes implemented in 40R1 building on Sandu et al., 2013

Turbulence closure for stable conditions:  $K_{M,H} = \left| \frac{\partial U}{\partial Z} \right| l^2 f_{M,H}(R_i), \quad \frac{1}{l} = \frac{1}{k_z} + \frac{1}{\lambda}$

## Up to 38R2

- long tails near surface, short tails above PBL
- $\lambda = 150\text{m}$
- non-resolved shear term, with a maximum at 850hPa



## From 40R1

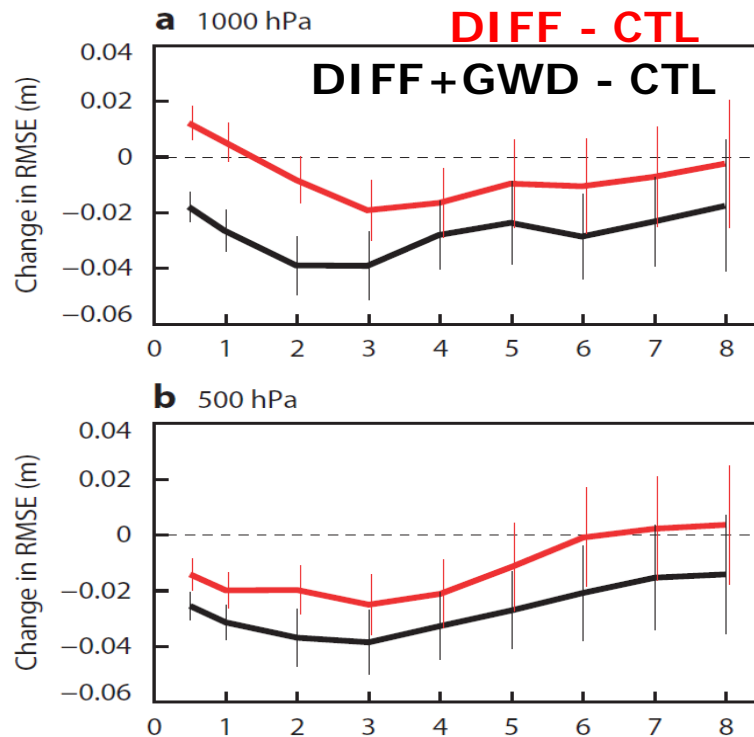
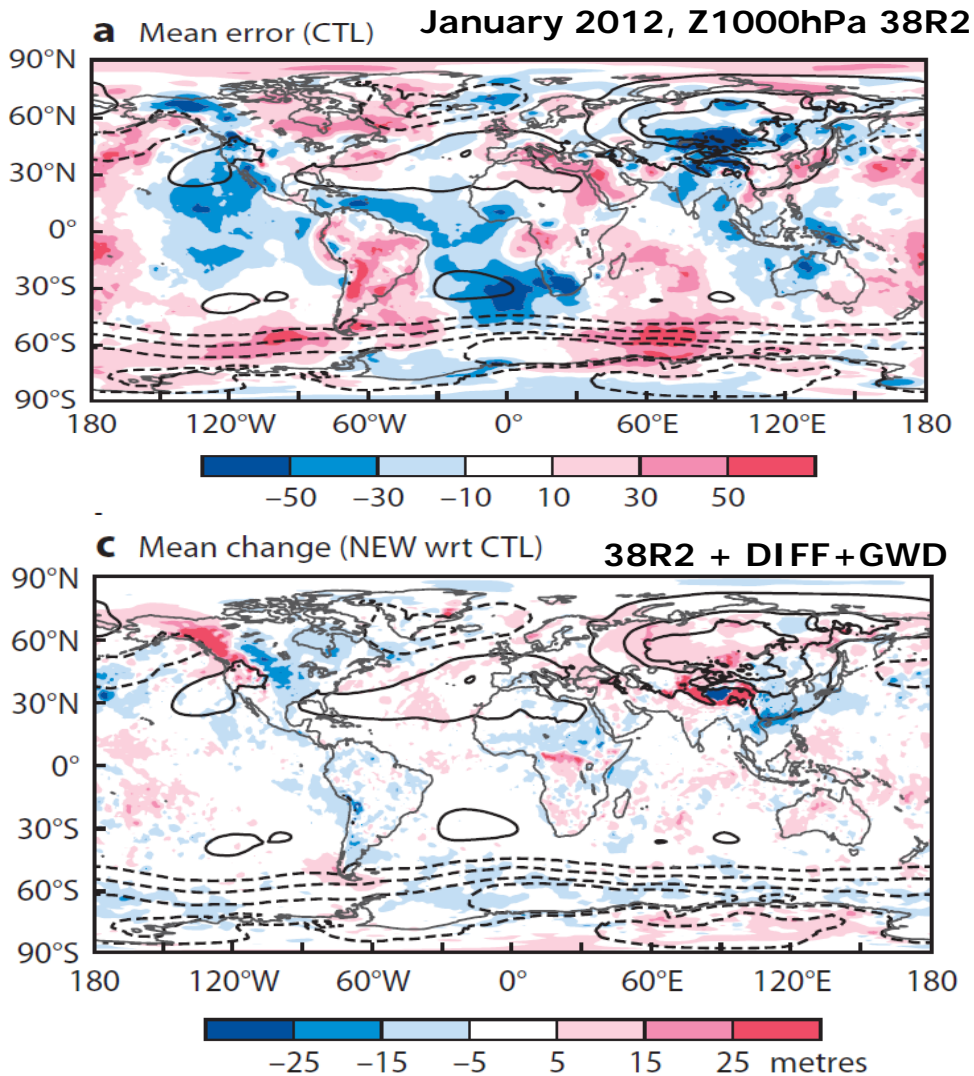
- long tails everywhere
- $\lambda = 10\%$  PBL height in stable boundary layers
- $\lambda = 30\text{ m}$  in free shear layers



Increase in drag over orography

**Consequence: net reduction in diffusion in stable boundary layers, not much change in free-shear layers, except at 850 hPa**

# Predictive skill since cycle 40r1

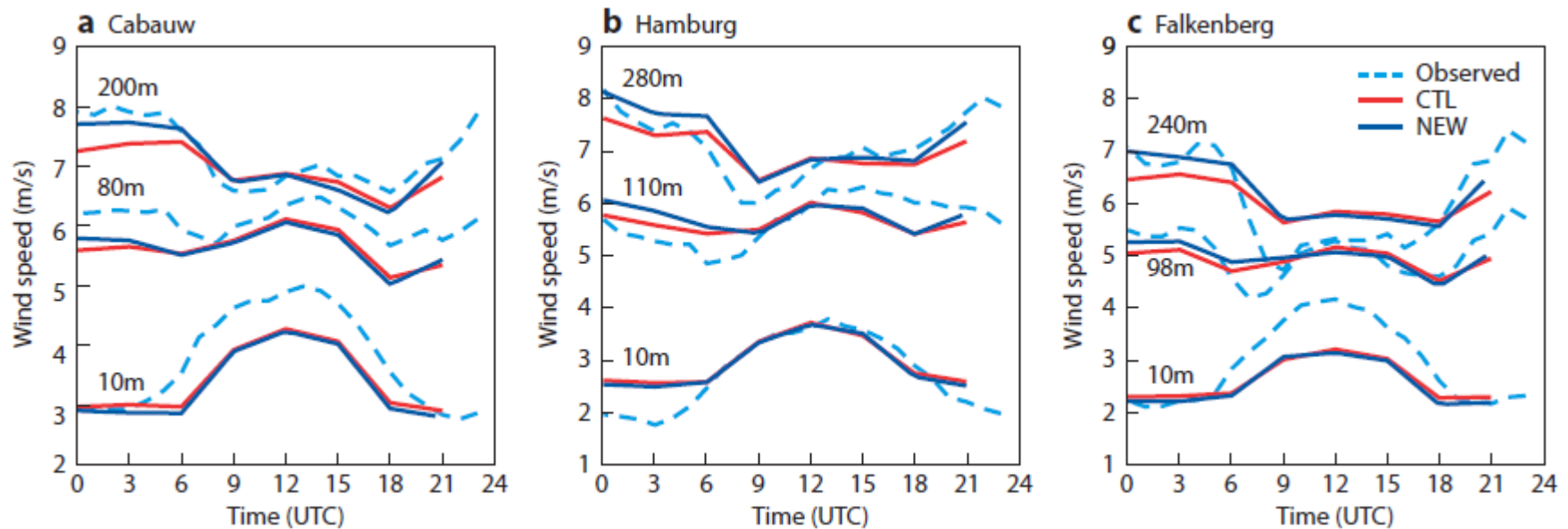


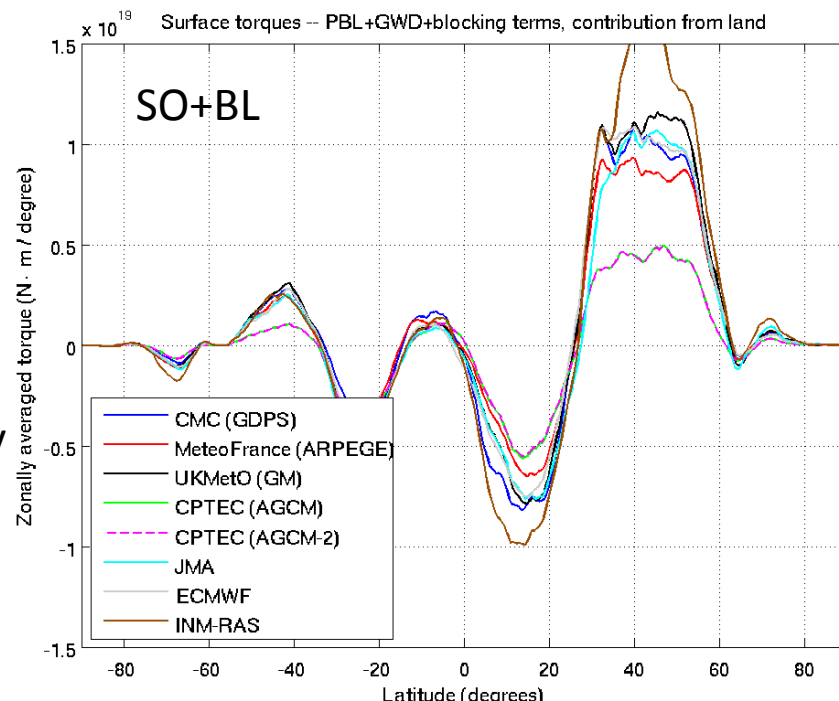
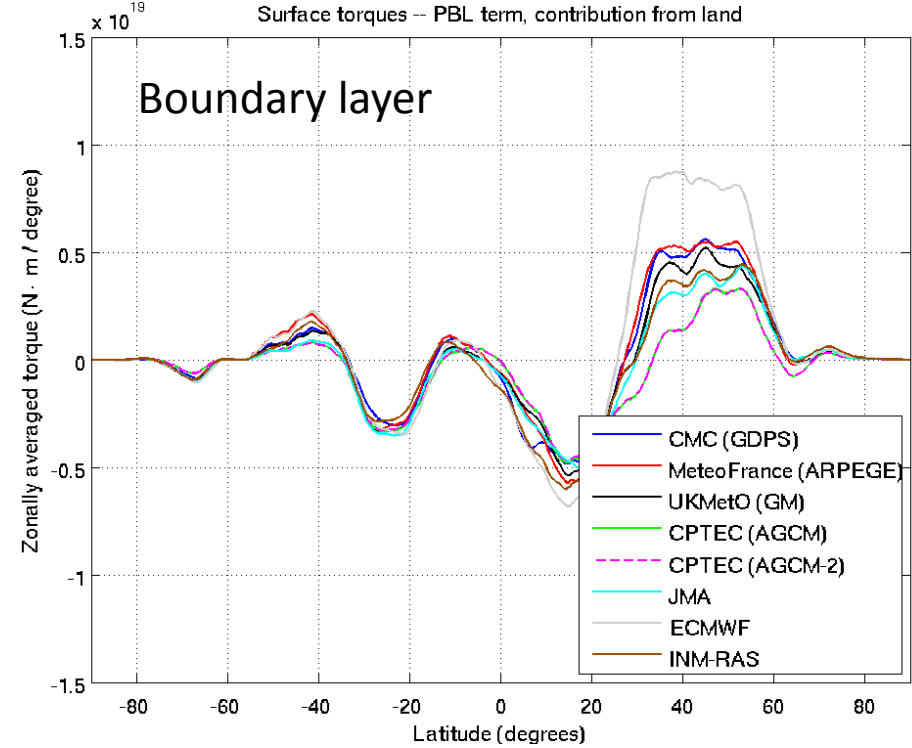
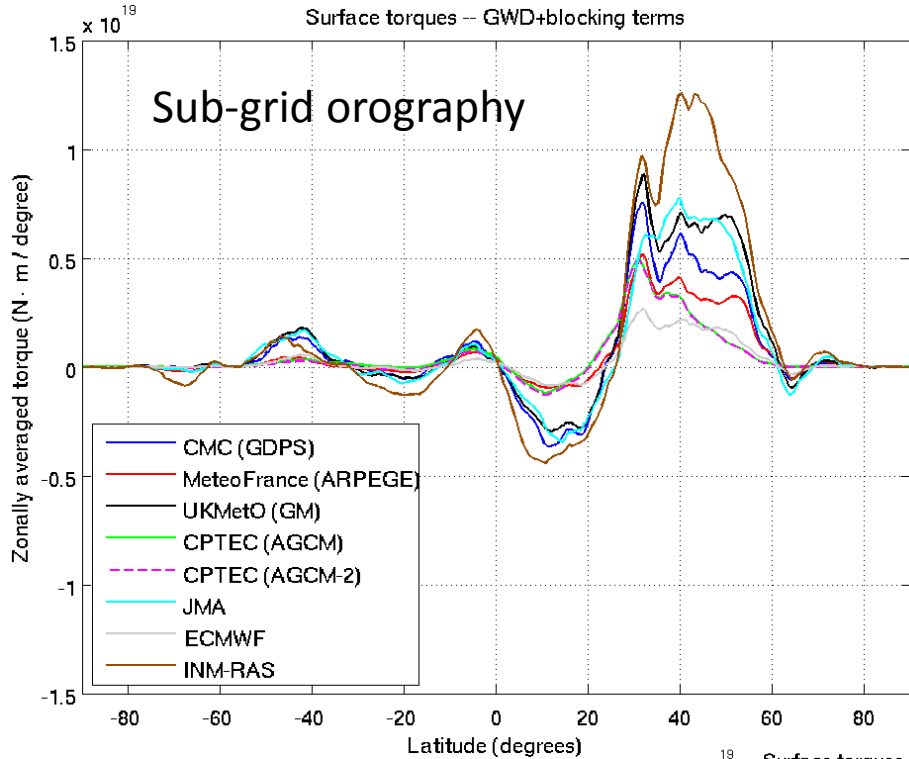
- Change to orographic drag affects planetary waves, anticyclones (e.g. too weak over EA)
- The improvement in averaged NH scores mostly located over E. Asia, NA

(I. Sandu; Newsletter, 138)

# Impact of diffusion / sub-grid orography changes

- Reduction of wind direction bias over Europe by  $3^\circ$  in winter,  $1^\circ$  in summer (out of  $10^\circ$ )
- Improvement in low level jets
- Improvement of the large-scale performance of the model in winter N Hemisphere
- Deterioration of tropical wind scores (against own analysis, not against observations!)





## WGNE/DRAG project (Ayrton Zadra)

Comparison of surface torque over land from different models for January 2012



# East-west surface stress averaged over 6-hr interval of daily forecasts in January 2012

## 6-12 UTC

## 18-24 UTC

EC

EC

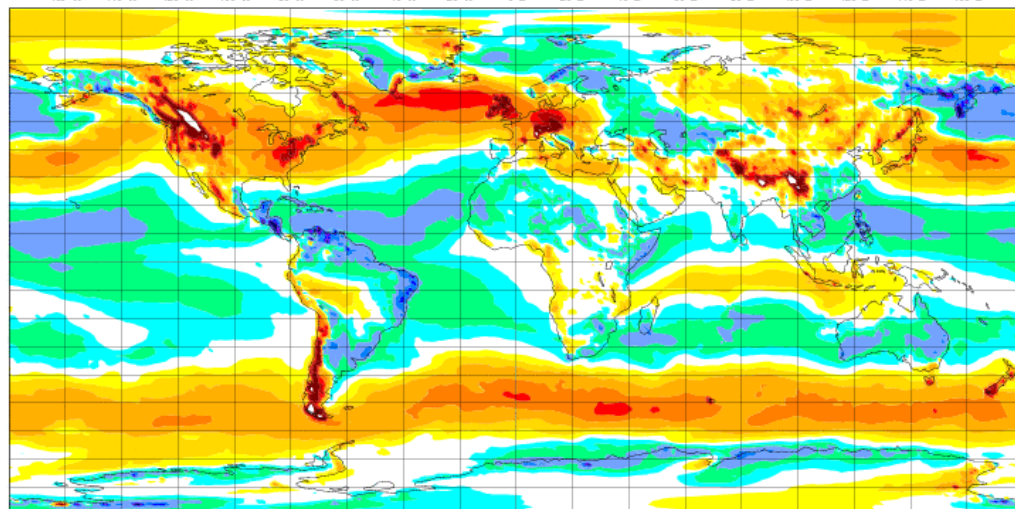
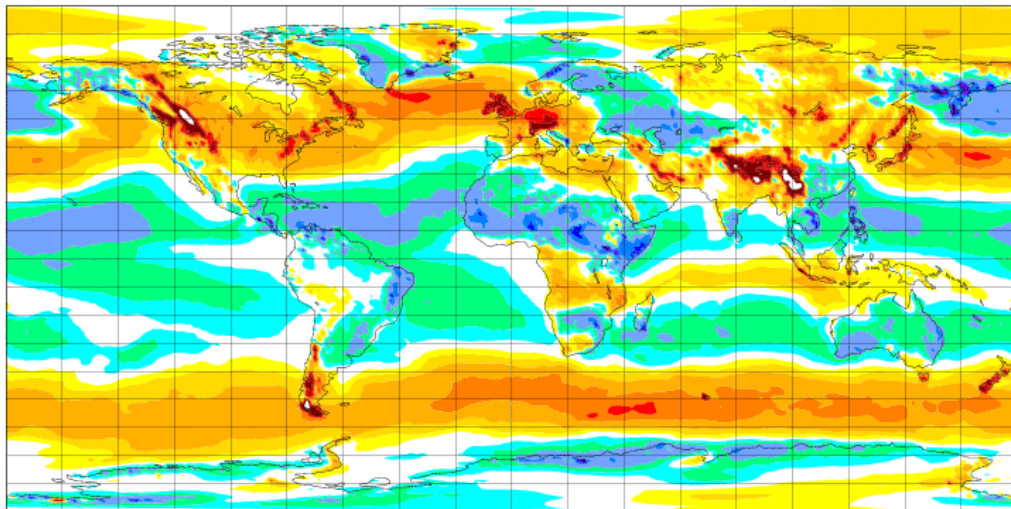
Sunday 01 January 2012 00 UTC ECMWF Forecast VT: Sunday 01 January 2012 12 UTC surface East-West surface stress

Sunday 01 January 2012 00 UTC ECMWF Forecast VT: Monday 02 January 2012 00 UTC surface East-West surface stress



160°W 140°W 120°W 100°W 80°W 60°W 40°W 20°W 0°E 20°E 40°E 60°E 80°E 100°E 120°E 140°E 160°E

160°W 140°W 120°W 100°W 80°W 60°W 40°W 20°W 0°E 20°E 40°E 60°E 80°E 100°E 120°E 140°E 160°E



MO

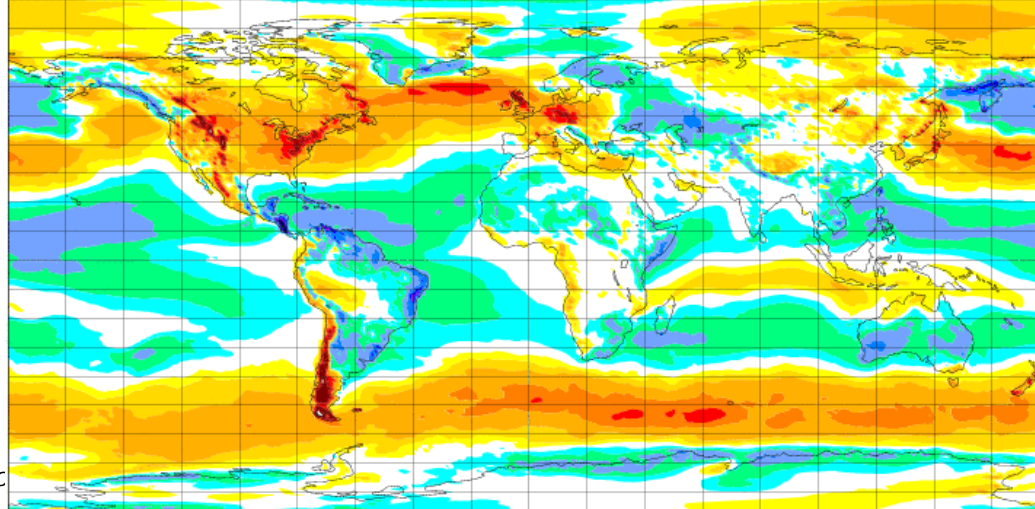
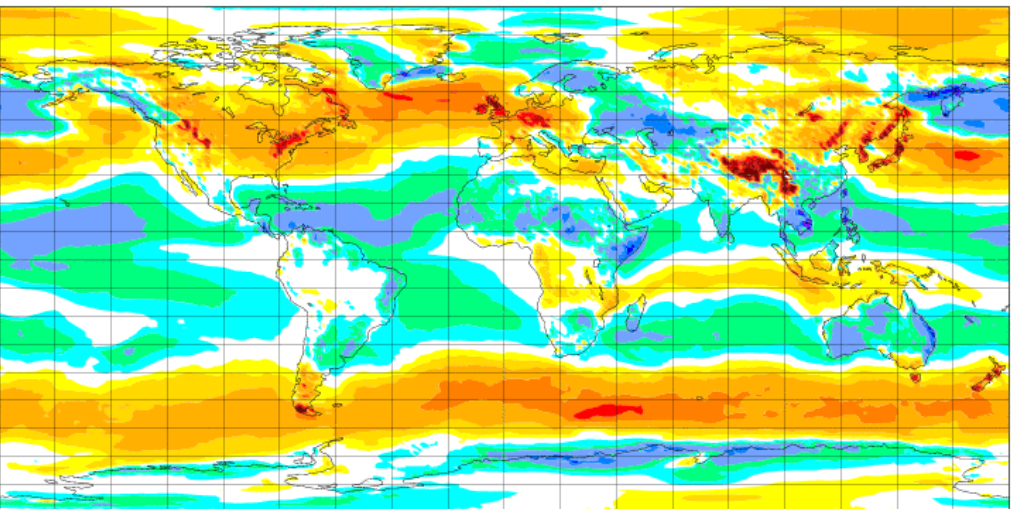
MO

UK 0 Base Time: Friday 31 August 2012 12 UTC Temperature



160°W 140°W 120°W 100°W 80°W 60°W 40°W 20°W 0°E 20°E 40°E 60°E 80°E 100°E 120°E 140°E 160°E

160°W 140°W 120°W 100°W 80°W 60°W 40°W 20°W 0°E 20°E 40°E 60°E 80°E 100°E 120°E 140°E 160°E



f.c



# Concluding remarks

**Enjoy the course**

**and**

**Do not hesitate to  
ask questions**